
Einführung in Web und Data Science

Community Analysis

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Today's lecture

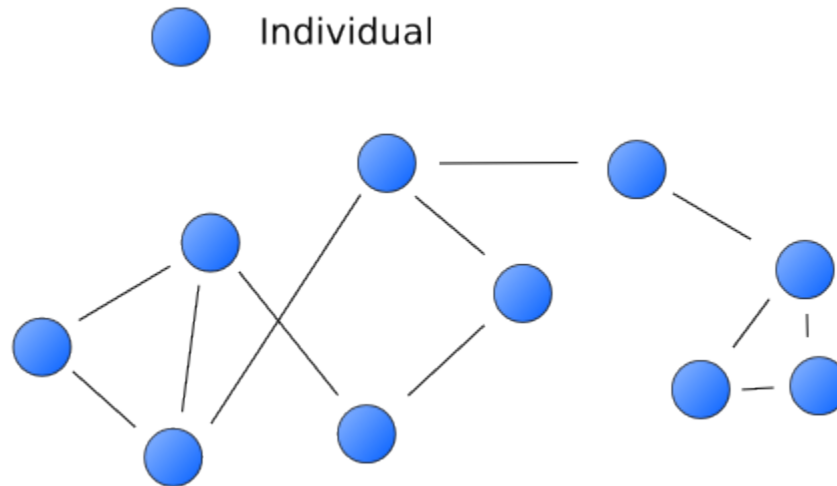
- Social Network Analysis
- Anchor text
- Link analysis for ranking
 - PageRank and variants
 - Hyperlink-Induced Topic Search (HITS)

Acknowledgements

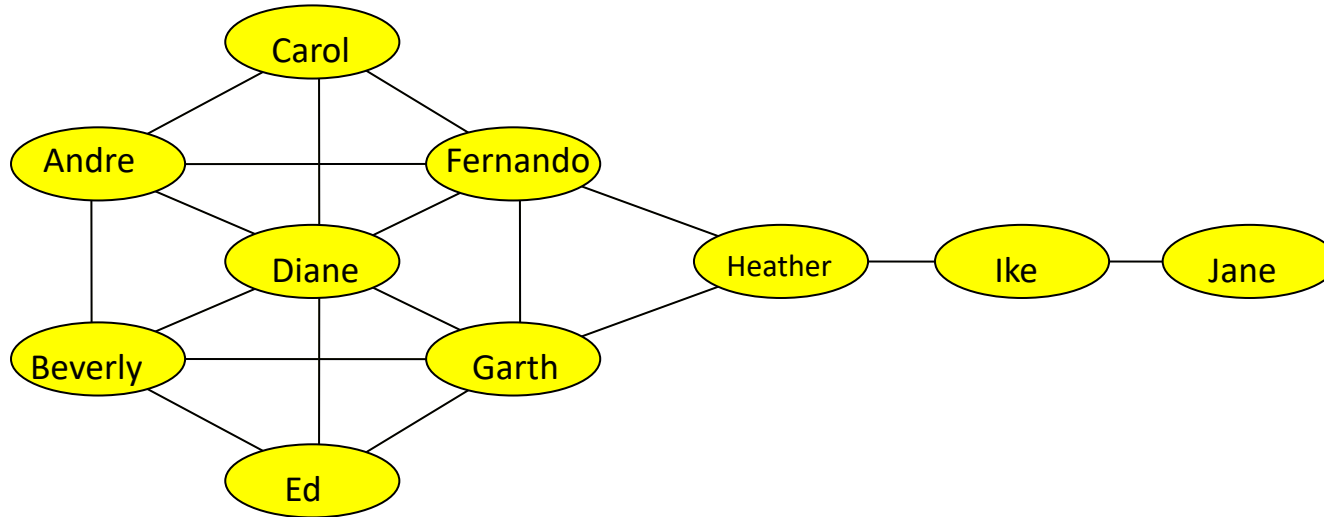
- Slides are based on material provided for
*CS276A, Stanford Univ.,
Text Information Retrieval, Mining, and Exploitation
Chr. Manning, P. Raghavan, H. Schütze*
- Thanks also to other lecturers who provided their teaching material on the web

Social Network Analysis (SNA)

- Mapping and measuring of **relationships and flows** between people, groups, organizations, computers or other information/knowledge processing **entities**.
- The **nodes** in the network are the people and groups while the **links** show relationships or flows between the nodes.



Kite Network



- Who are **connectors** or **hubs** in the network?
- Who has **control over what flows** in the network?
- Who has best **visibility of what is happening** in the network?
- Who are **peripheral players**? Are they important?

Measures

1. Degree Centrality:

The number of direct connections a node has. What really matters is where those connections lead to and how they connect the otherwise unconnected.

$$C_D(n_i) = d(n_i)$$

$$C'_D(n_i) = \frac{d(n_i)}{g-1}$$

2. Betweenness Centrality:

A node with high betweenness has great influence over what flows in the network indicating important links and single points of failure.

$$C_B(n_i) = \sum_{j < k} g_{jk}(n_i) / g_{jk}$$

$$C'_B(n_i) = \frac{C_B(n_i)}{(g-1)(g-2)/2}$$

3. Closeness Centrality:

The measure of closeness of a node to everyone else.

Determined by the sum of the length of the [shortest paths](#) between the node and all other nodes in the graph.

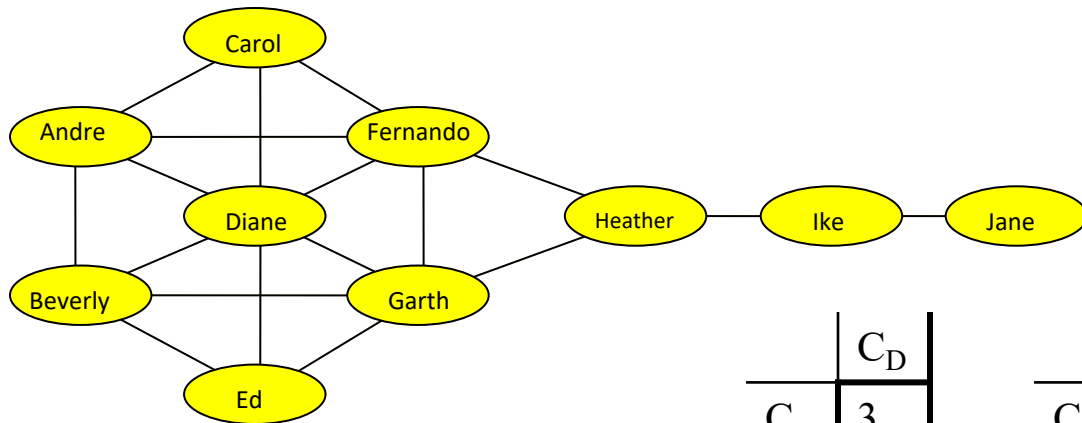
$$C_C(n_i) = \left[\sum_{j=1}^g d(n_i, n_j) \right]^{-1}$$

$$C'_C(n_i) = \frac{g-1}{\sum_{j=1}^g d(n_i, n_j)} = (g-1)C_C(n_i)$$

Legend

- g = size of graph (number of nodes)
- $d(.)$ = (in)degree
- g_{jk} = number of minimal paths between nodes j and k
- $g_{jk}(n)$ = number of minimal paths between nodes j and k that contain n
- $(g-1)(g-2)/2$ = number of potential paths
 $\sum_{x=1}^u x = (u+1)u/2$ für $u=(g-2)$
- $d(.,.)$ = distance between two nodes

Example: Kite-Network



$$C_B(n_i) = \sum_{j < k} g_{jk}(n_i) / g_{jk}$$

$$C_C(n_i) = \left[\sum_{j=1}^g d(n_i, n_j) \right]^{-1}$$

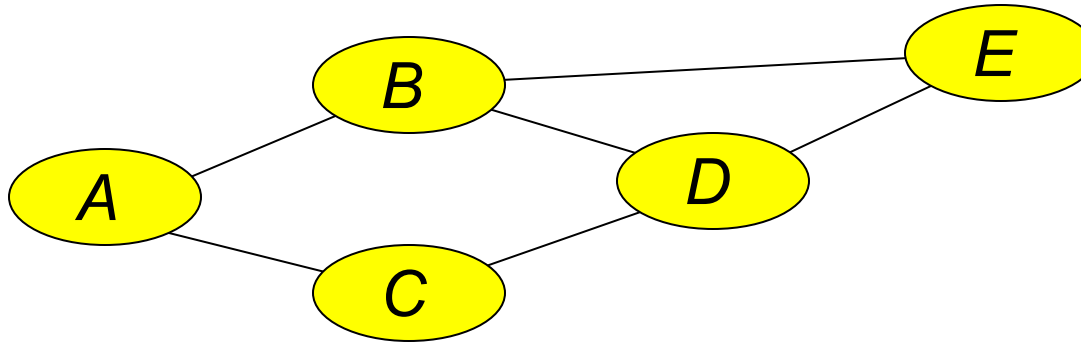
$$C_D(n_i) = d(n_i)$$

	C_D
C	3
A	4
F	5
D	6
B	4
G	5
E	3
H	3
I	2
J	1

	C	A	F	D	B	G	E	H	I	J
C	0	1	1	1	0	0	0	0	0	0
A	1	0	1	1	1	0	0	0	0	0
F	1	1	0	1	0	1	0	1	0	0
D	1	1	1	0	1	1	1	0	0	0
B	0	1	0	1	0	1	1	0	0	0
G	0	0	1	1	1	0	1	1	0	0
E	0	0	0	1	1	1	0	0	0	0
H	0	0	1	0	0	1	0	0	1	0
I	0	0	0	0	0	0	0	1	0	1
J	0	0	0	0	0	0	0	0	1	0

Example

$$C_B(n_i) = \sum_{j < k} g_{jk}(n_i) / g_{jk} \quad C_C(n_i) = \left[\sum_{j=1}^g d(n_i, n_j) \right]^{-1} \quad C_D(n_i) = d(n_i)$$



	A	B	C	D	E
A	0	1	1	0	0
B	1	0	0	1	1
C	1	0	0	1	0
D	0	1	1	0	1
E	0	1	0	1	0

Adjacency

	C_B	C_C	C_D
A	1	1/6	2
B	3	1/5	3
C	1	1/6	2
D	3	1/5	3
E	0	1/6	2

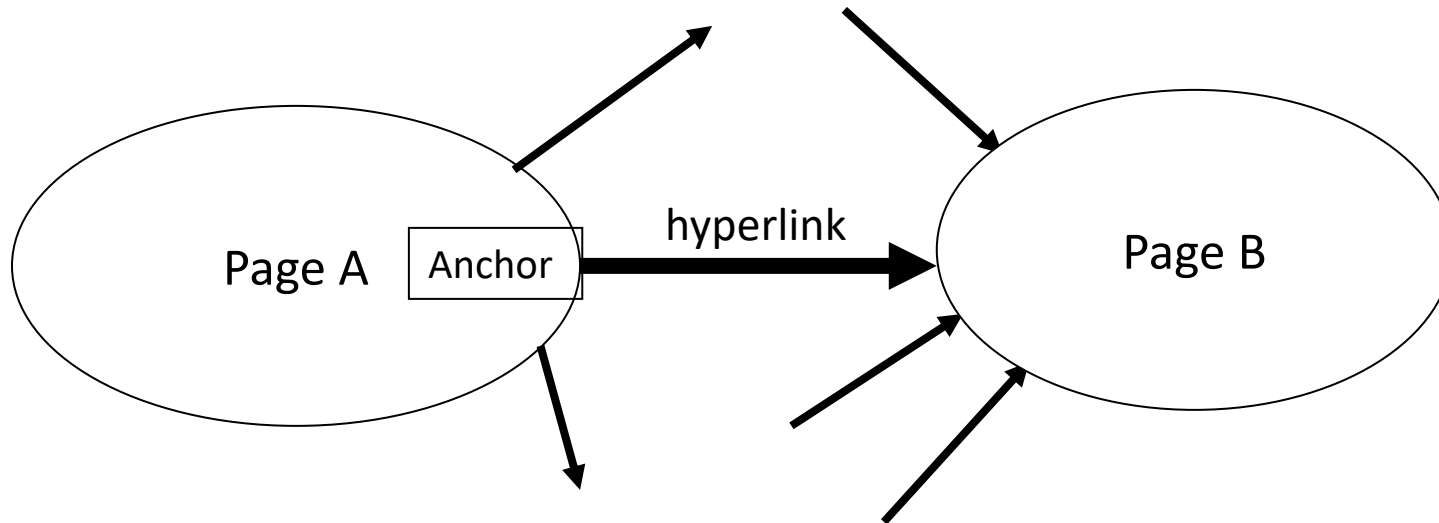
	A	B	C	D	E
A	0	1	1	2	2
B	1	0	2	1	1
C	1	2	0	1	2
D	2	1	1	0	1
E	2	1	2	1	0

Distance

	A	B	C	D	E
A	0	A	A	BC	B
B	B	0	AD	B	B
C	C	AD	0	C	D
D	BC	D	D	0	D
E	B	E	D	E	0

Paths

The Web as a Directed Graph

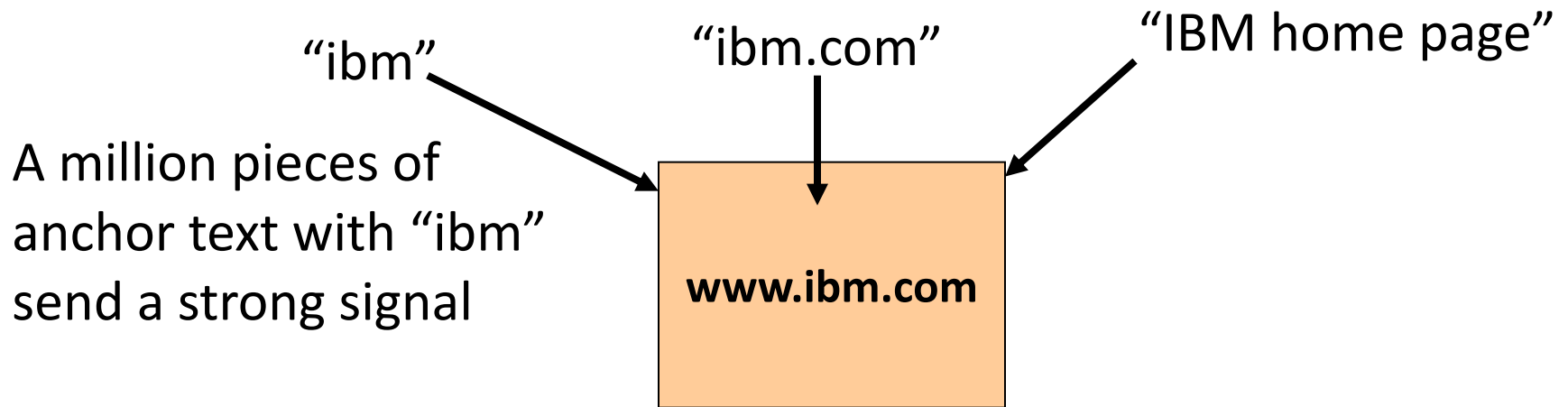


Assumption 1: A hyperlink between pages denotes author perceived relevance (quality signal)

Assumption 2: The anchor of the hyperlink describes the target page (textual context)

Anchor Text

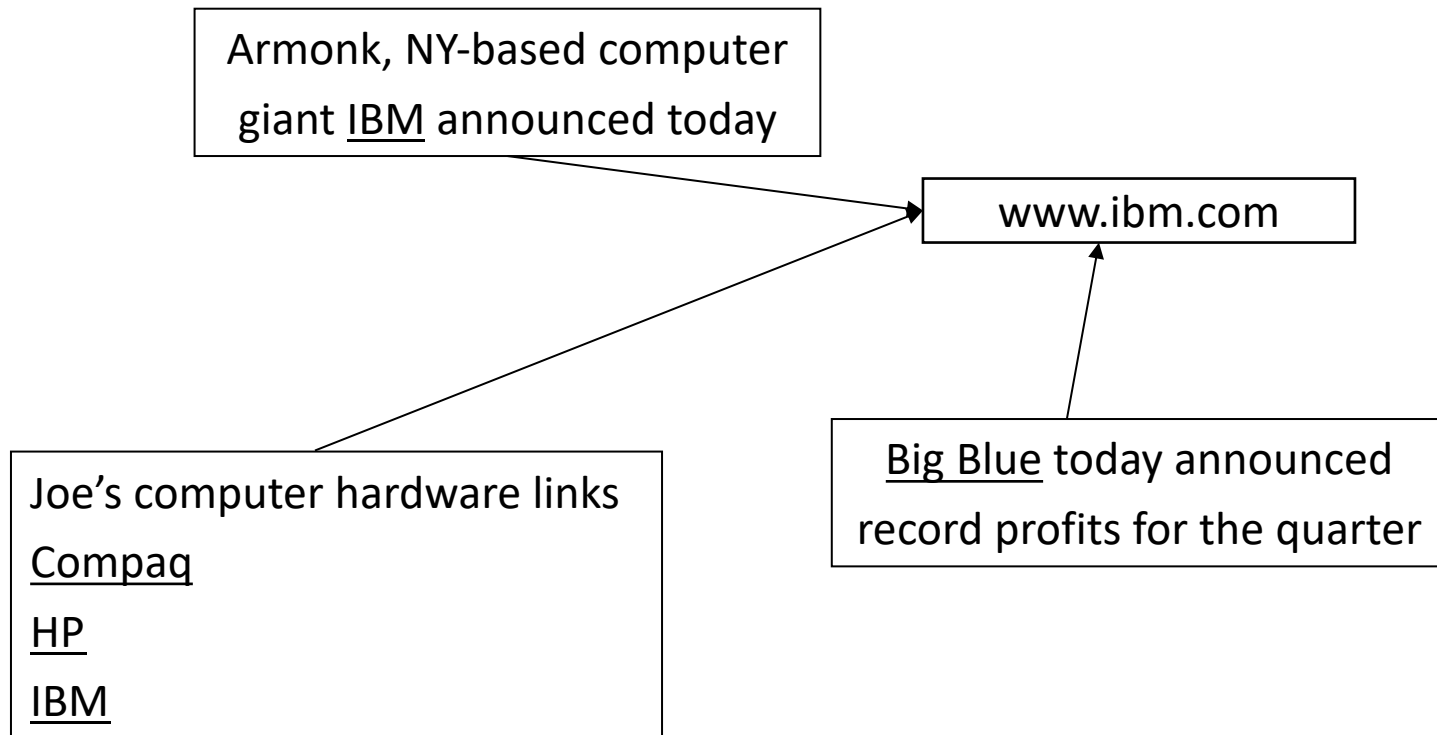
- For **IBM** how to distinguish between:
 - IBM's home page (mostly graphical)
 - IBM's copyright page (high term freq. for 'ibm')
 - Rival's spam page (arbitrarily high term freq.)



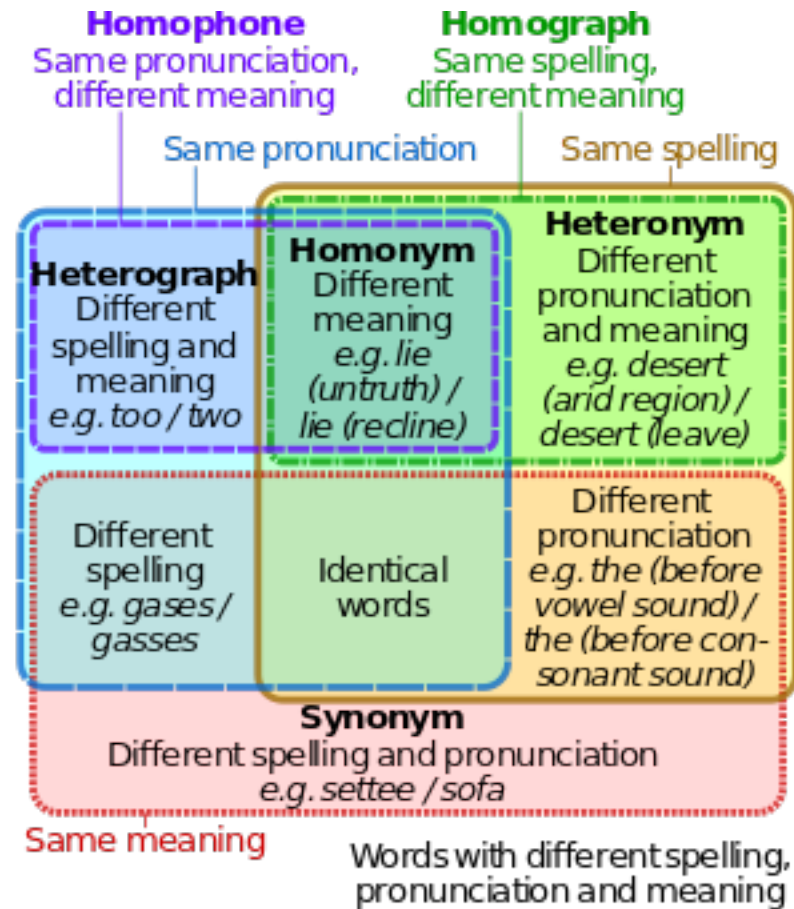
Oliver A. McBryan. GENVL and WWW: Tools for Taming the Web. Research explained at First International Conference on the World Wide Web. CERN, Geneva (Switzerland), May 25-26-27 **1994**
(WWW=World Wide Web Worm, first search engine for the web)

Indexing anchor text

- When indexing a document D , include anchor text from links pointing to D .

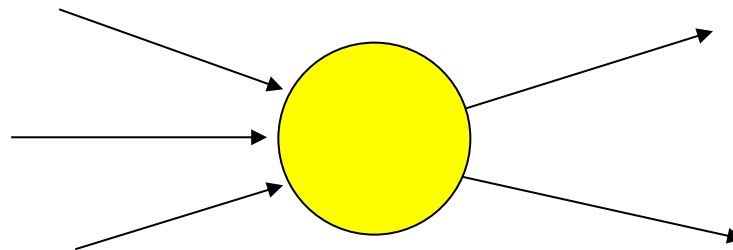


The Web as a Resource for NLP




The Web as a Resource for Ranking

- First generation: using **link counts** as simple measures of **popularity**.
- Two basic suggestions:
 - Undirected popularity:
 - Each page gets a score = the number of in-links plus the number of out-links ($3+2=5$).
 - Directed popularity:
 - Score of a page = number of its in-links (3).



Query processing

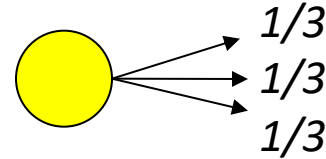
- First retrieve all pages matching the text query (say ***venture capital***).
- Order these by their link popularity (either variant on the previous page).



How to organize for
"Search Engine
Optimization"?

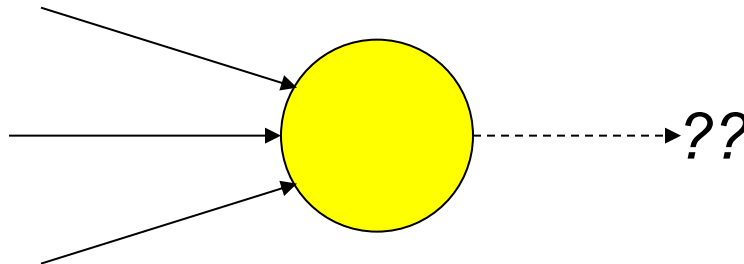
PageRank scoring

- Imagine a browser doing a random walk on web pages:
 - Start at a random page
 - At each step, go out of the current page along one of the links on that page, equiprobably
- Each page has a long-term visit rate - use this as the page's score



Not quite enough

- The web is full of dead-ends.
 - Random walk can get stuck in dead-ends.
 - Makes no sense to talk about long-term visit rates.



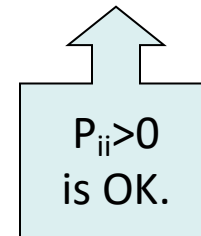
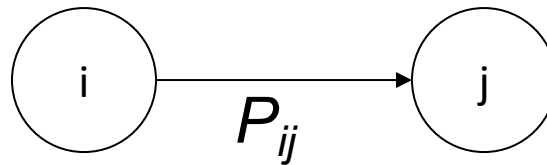
Teleporting / damping

- At a dead end, jump to a random web page.
- At any non-dead end, with probability 10%, jump to a random web page.
 - With remaining probability (90%), go out on a random link.
 - 10% - a parameter.
- There is a long-term rate at which any page is visited.
 - How do we compute this visit rate?

Markov chains

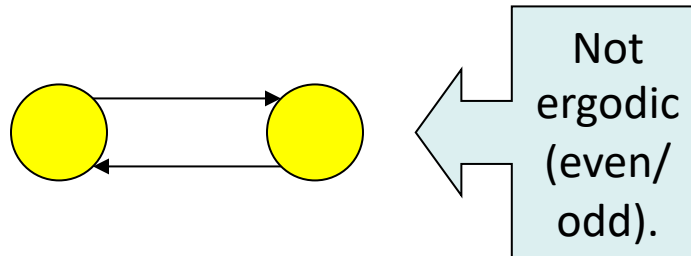
- A Markov chain consists of n states, plus an $n \times n$ transition matrix \mathbf{P} .
- At each step, we are in exactly one of the states.
- For $1 \leq i, j \leq n$, the matrix entry P_{ij} tells us the relative frequency of j being the next state, given we are currently in state i .

$$\sum_{j=1}^n P_{ij} = 1.$$



Ergodic Markov chains

- A Markov chain is ergodic if
 - you have a path from any state to any other (reducibility)
 - returns to states occur at irregular times (aperiodicity)
 - For any start state, after a finite transient time T_0 , the probability of being in any state at a fixed time $T > T_0$ is nonzero. (positive recurrence)



Ergodic Markov chains

- For any ergodic Markov chain, there is a unique long-term visit rate for each state.
 - *"Steady-state" distribution.*
- Over a long time-period, we visit each state in proportion to this rate.
- It doesn't matter where we start.

State vectors

- A (row) vector (state vector) $\mathbf{x} = (x_1, \dots, x_n)$ tells us where the walk is at any point.
- E.g., (000...1...000) means we're in state i .

1 i n

More generally, the vector $\mathbf{x} = (x_1, \dots, x_n)$ means the walk is in state i with relative frequency x_i .

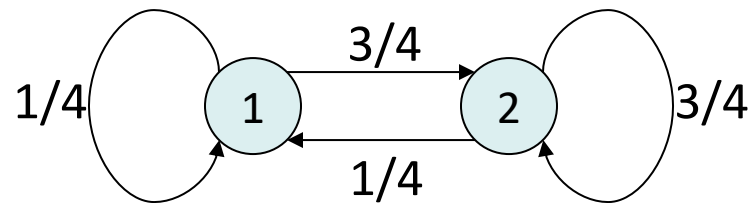
$$\sum_{i=1}^n x_i = 1.$$

Change in state vector

- If the state vector is $\mathbf{x} = (x_1, \dots, x_n)$ at this step, what is it at the next step?
- Recall that row i of the transition matrix \mathbf{P} tells us where we go next from state i
- So from \mathbf{x} , our next state is distributed as \mathbf{xP} .

Steady state example

- The steady state looks like a vector of probabilities $\mathbf{a} = (a_1, \dots, a_n)$:
 - a_i is the relative frequency that we are in state i .

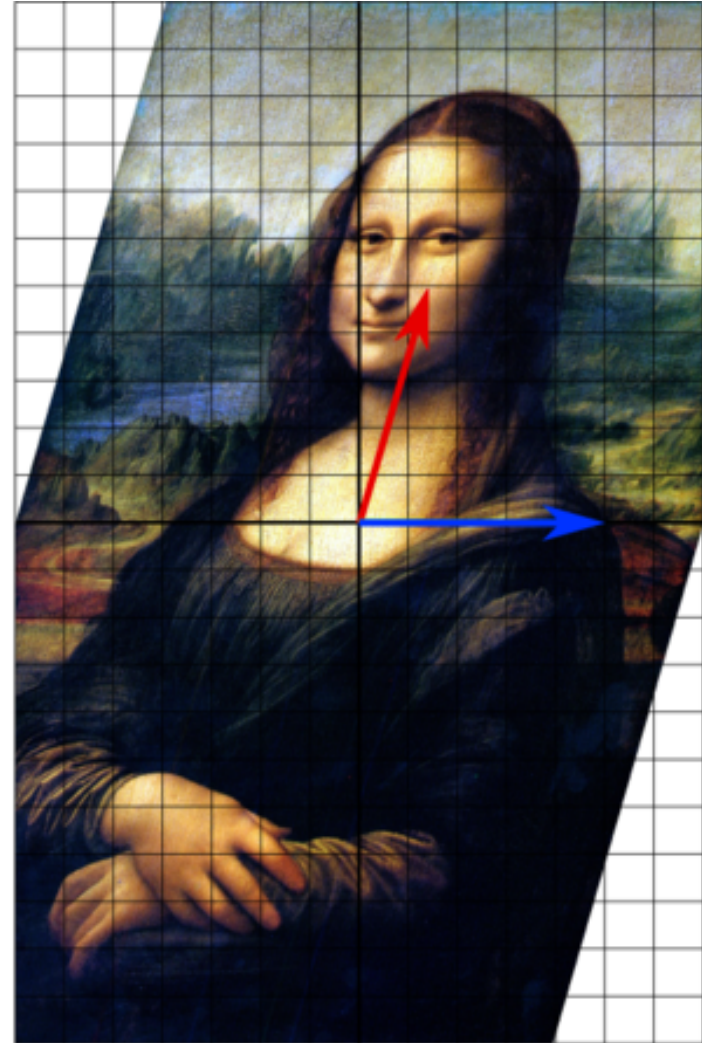
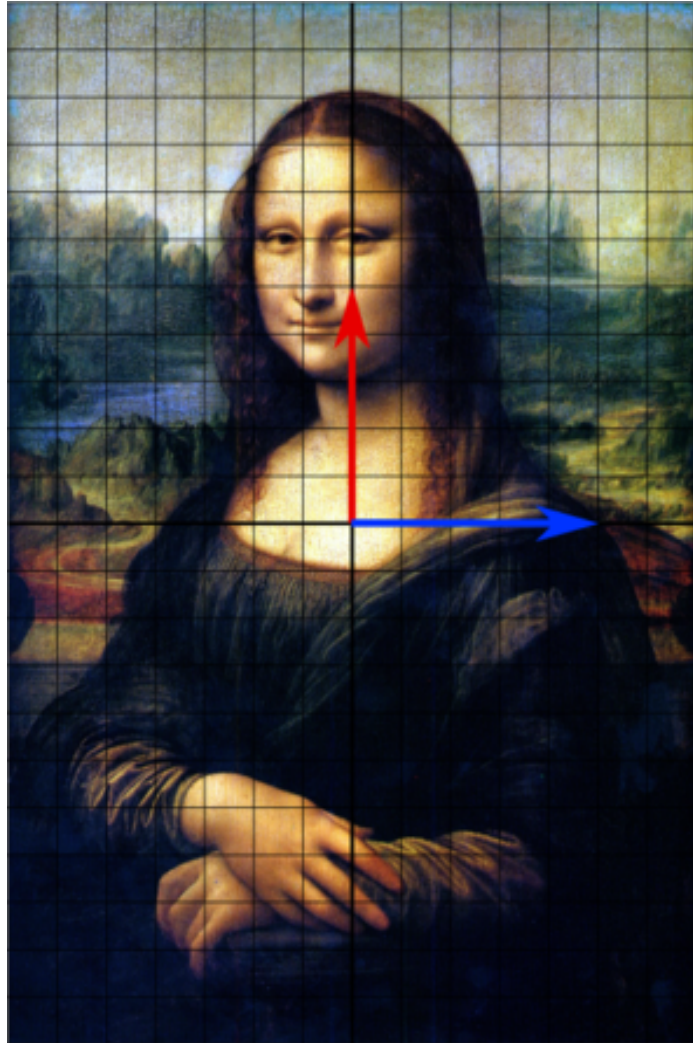


For this example, $a_1=1/4$ and $a_2=3/4$.

How do we compute this vector?

- Let $\mathbf{a} = (a_1, \dots, a_n)$ denote the row vector of steady-state rates.
- If we our current position is described by \mathbf{a} , then the next step is described as \mathbf{aP} .
- But \mathbf{a} is the steady state, so $\mathbf{a} = \mathbf{aP}$.
- Solving this matrix equation gives us \mathbf{a} .
 - So \mathbf{a} is the (left) eigenvector for \mathbf{P} .
 - (Corresponds to the “principal” eigenvector of \mathbf{P} with the largest eigenvalue)
 - Transition matrices always have largest eigenvalue 1.

Eigenvectors and Eigenvalues $Mx = \lambda x$



One way of computing \mathbf{a}

- Recall, regardless of where we start, we eventually reach the steady state \mathbf{a} .
- Start with any distribution (say $\mathbf{x}=(10\dots0)$).
- After one step, we're at \mathbf{xP} ;
- after two steps at \mathbf{xP}^2 , then \mathbf{xP}^3 and so on.
- “Eventually” means for “large” k , $\mathbf{xP}^k = \mathbf{a}$.
- Algorithm: multiply \mathbf{x} by increasing powers of \mathbf{P} until the product looks stable.

PageRank Summary

- Preprocessing:
 - Given graph of links, build matrix \mathbf{P}
 - From it compute \mathbf{a}
 - The entry a_i is a number between 0 and 1: the pagerank of page i .
- Query processing:
 - Retrieve pages meeting query
 - Rank them by their pagerank
 - Order is *query-independent*
- A variant of PageRank is used in Google, but also many other clever heuristics

PageRank: Issues and Variants

- How realistic is the random surfer model?
 - What if we modeled the back button?
 - Surfer behavior sharply skewed towards short paths
 - Search engines, bookmarks & directories make jumps non-random
- Biased Surfer Models
 - Weight edge traversal probabilities based on match with topic/query (non-uniform edge selection)
 - Bias jumps to pages on topic (e.g., based on personal bookmarks & categories of interest)

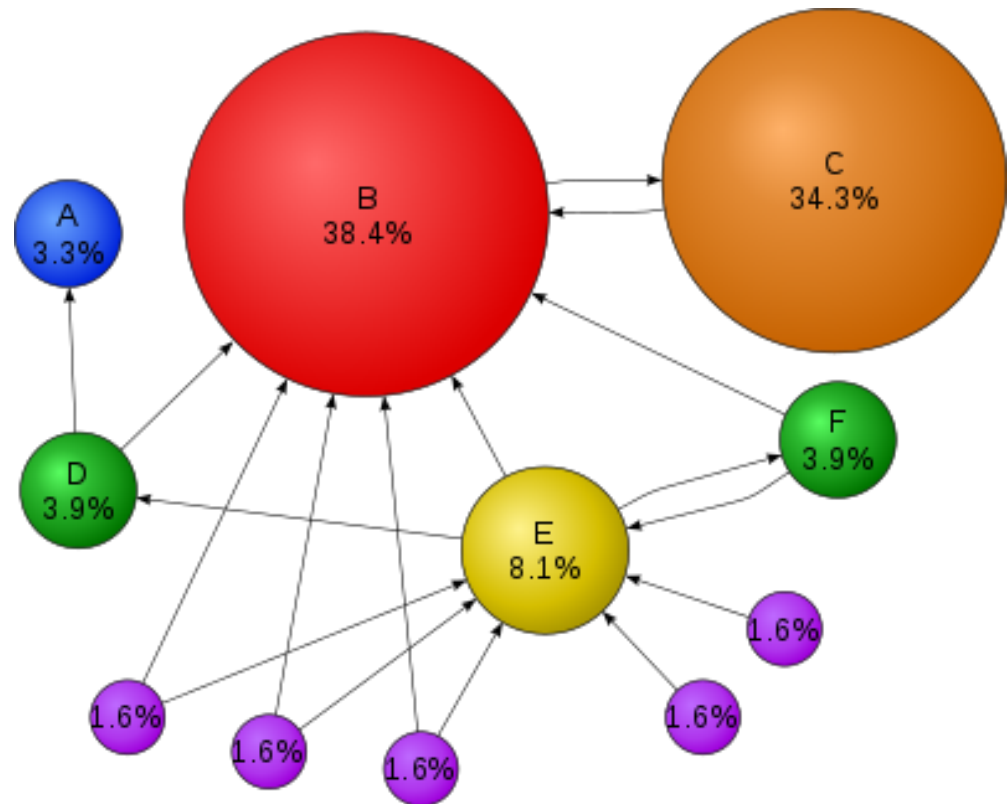
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Google PageRank

- Links are also weighted according to the importance of the source node
 - Page C has a higher PageRank than Page E, even though there are fewer links to C; the one link to C comes from an important page and hence is of high value.



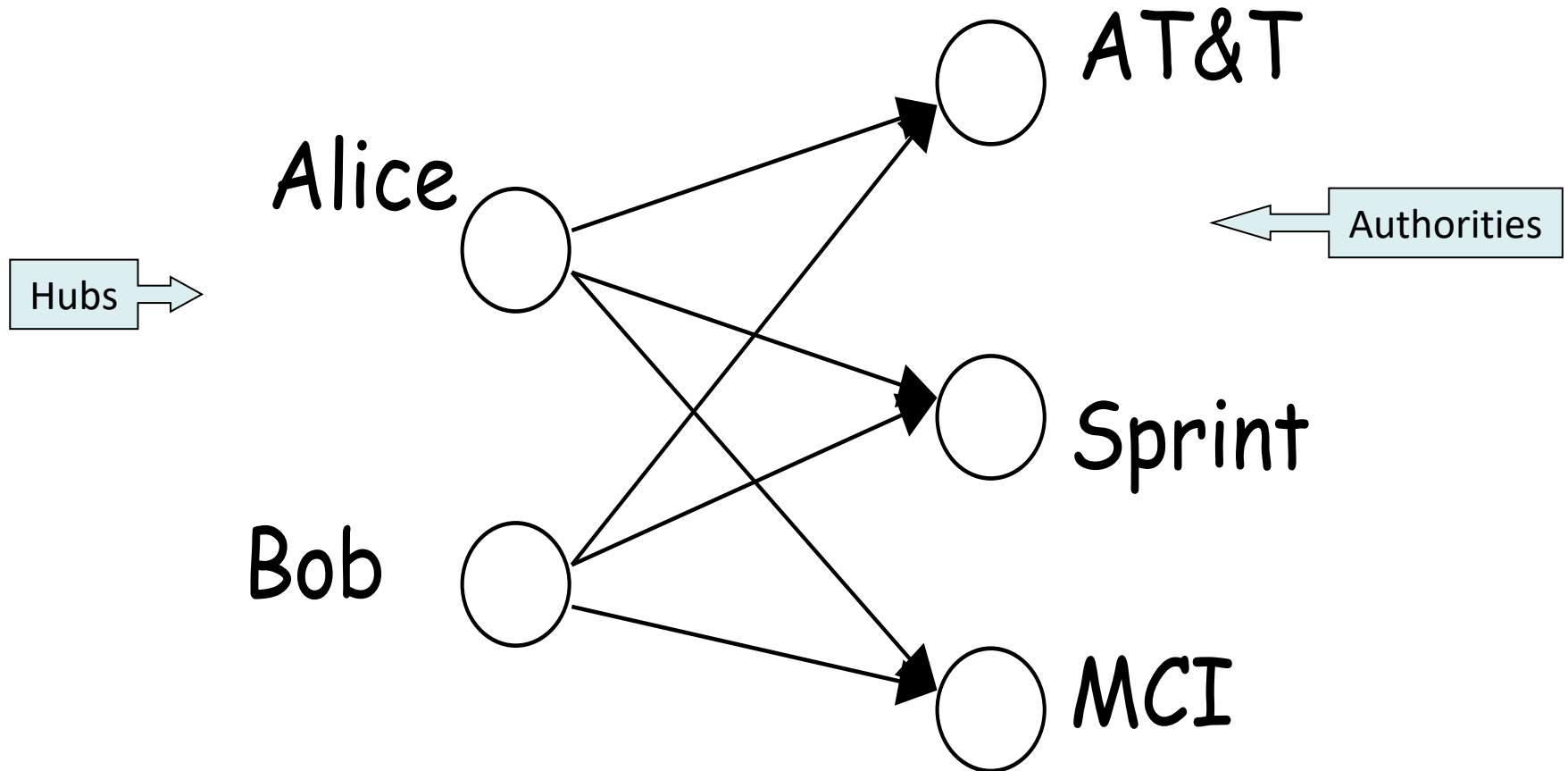
Hyperlink-Induced Topic Search (HITS)

- In response to a query, instead of an ordered list of pages each meeting the query, find two sets of inter-related pages:
 - **Hub pages** are good lists of links on a subject
 - e.g., “Bob’s list of cancer-related links.”
 - **Authority pages** occur recurrently on good hubs for the subject
- Best suited for “broad topic” queries rather than for page-finding queries

Hubs and Authorities

- Thus, a good **hub** page for a topic *points to many authoritative* pages for that topic
- A good **authority** page for a topic is *pointed to by many good hubs* for that topic
- Circular definition - will turn this into an iterative computation

The hope



Long distance telephone companies

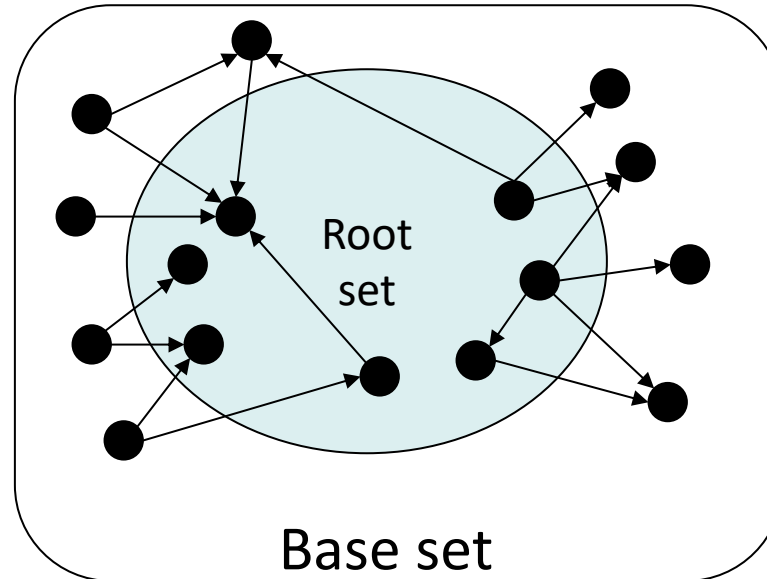
High-level scheme

- Extract from the web a base set of pages that *could* be good hubs or authorities
- From these, identify a small set of top hub and authority pages;
→ iterative algorithm

Base set

- Given text query (say “**browser**”), use a text index to get all pages containing “**browser**”
 - Call this the **root set** of pages
- Add in any page that either
 - points to a page in the root set, or
 - is pointed to by a page in the root set
- Call this the **base set**

Visualization



Assembling the base set

- Root set typically 200-1000 nodes
- Base set may have up to 5000 nodes
- How do you find the base set nodes?
 - Follow out-links by parsing root set pages
 - Get in-links (and out-links) from a connectivity server
 - Actually, suffices to text-index strings of the form **href=“URL”** to get in-links to URL

Distilling hubs and authorities

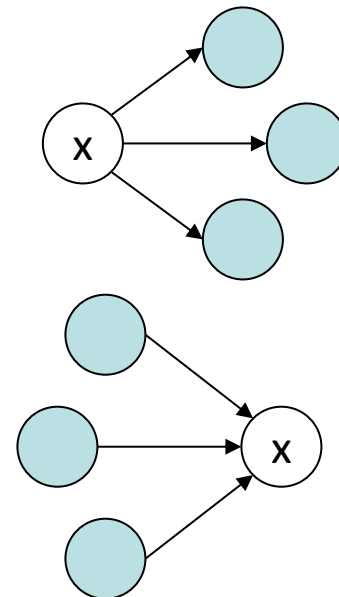
Compute, for each page x in the base set, a **hub score** $h(x)$ and an **authority score** $a(x)$

- Initialize: for all x , $h(x) \leftarrow 1$; $a(x) \leftarrow 1$;
- Iteratively update all $h(x)$, $a(x)$;

$$h(x) \leftarrow \sum_{x \mapsto y} a(y)$$

$$a(x) \leftarrow \sum_{y \mapsto x} h(y)$$

- After iterations output pages with
 - highest $h()$ scores as top hubs
 - highest $a()$ scores as top authorities



Scaling

- To prevent the $h()$ and $a()$ values from getting too big, can scale down after each iteration
- Scaling factor doesn't really matter:
 - we only care about the *relative* values of the scores

How many iterations?

- Claim: relative values of scores will converge after a few iterations:
 - In fact, suitably scaled, $h()$ and $a()$ scores settle into a steady state!
- We only require the **relative orders** of the $h()$ and $a()$ scores - not their absolute values
- In practice, ~5 iterations get you close to stability