

Advanced Topics Data Science and AI

Automated Planning and

Acting

Nondeterministic Models

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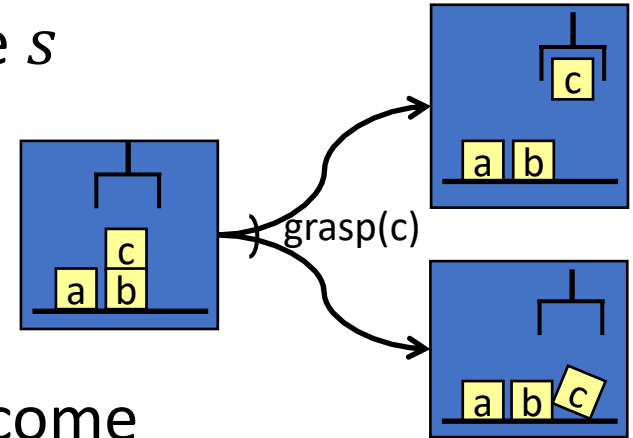
Content

1. Planning and Acting with **Deterministic** Models
2. Planning and Acting with **Refinement** Methods
3. Planning and Acting with **Temporal** Models
4. Planning and Acting with **Nondeterministic** Models
 - a. Planning Problem
 - b. And/Or Graph Search
 - c. Determinisation
 - d. Online Approaches
5. Making Simple Decisions
6. Making Complex Decisions
7. Planning and Acting with **Probabilistic** Models
8. Provably Beneficial AI
 - Other: open world, perceiving, learning
 - If time permits

Motivation

- We have assumed action a in state s has just one possible outcome

- $\gamma(s, a)$



- Often more than one possible outcome
 - Unintended outcomes
 - Exogenous events
 - Inherent uncertainty



Outline per the Book

5.2 Planning Problem

- Planning domains
- Plans as policies
- Planning problems and solutions

5.3 And/Or Graph Search

- Planning by forward search

5.5 Determinisation Techniques

- Guided planning for safe solutions
- Planning for safe solutions by determinisation

5.6 Online Approaches

- Lookahead
- Lookahead by Determinisation
- Lookahead with a bounded number of steps

Nondeterministic Planning Domains

- Planning domain: 3-tuple (S, A, γ)
 - S and A – finite sets of states and actions
 - $\gamma : S \times A \rightarrow 2^S$
- $\gamma(s, a) = \{\text{all possible “next states” after applying action } a \text{ in state } s\}$
 - a is **applicable** in state s iff $\gamma(s, a) \neq \emptyset$
- $\text{Applicable}(s) = \{\text{all actions applicable in } s\} = \{a \in A \mid \gamma(s, a) \neq \emptyset\}$
- One action representation:
 - n mutually exclusive “effects” lists
 - **Problem:** n may be combinatorially large
 - Suppose a can cause any possible combination of effects e_1, e_2, \dots, e_k
 - Need $\text{eff}_1, \text{eff}_2, \dots, \text{eff}_{2^k}$
 - One for for each combination
 - Section 5.4: a way to alleviate this
 - For now, ignore most of that
 - states, actions \Leftrightarrow nodes, edges in a graph

$$\begin{array}{l} a(z_1, \dots, z_k) \\ \text{pre: } p_1, \dots, p_m \\ \text{eff}_1: e_{11}, e_{12}, \dots \\ \text{eff}_2: e_{21}, e_{22}, \dots \\ \vdots \\ \text{eff}_n: e_{n1}, e_{n2}, \dots \end{array}$$

Nondeterministic Planning Domains

- For deterministic planning problems, search space was a graph

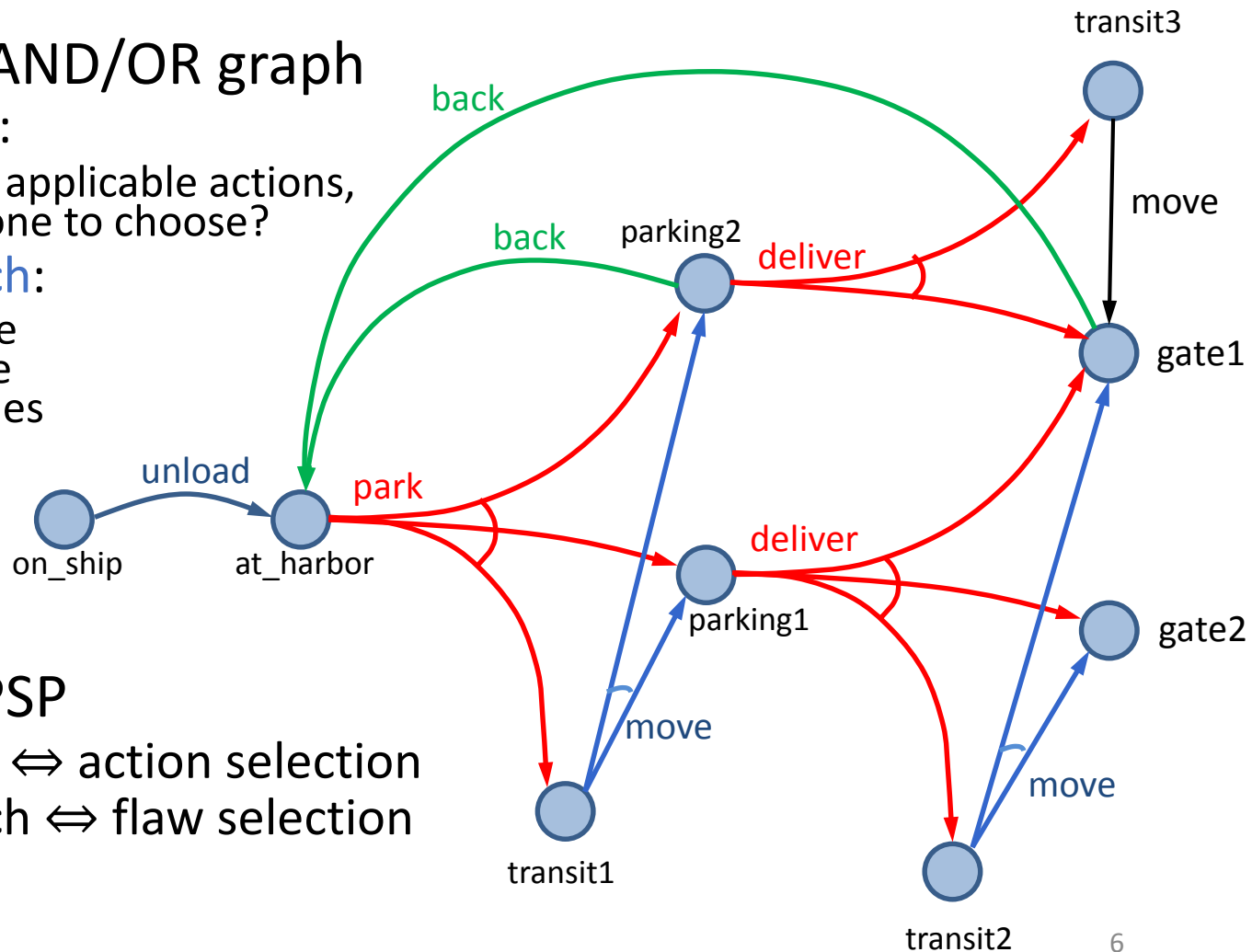
- Now it's an AND/OR graph

- **OR branch:**

- Several applicable actions, which one to choose?

- **AND branch:**

- Multiple possible outcomes
 - Must handle all of them

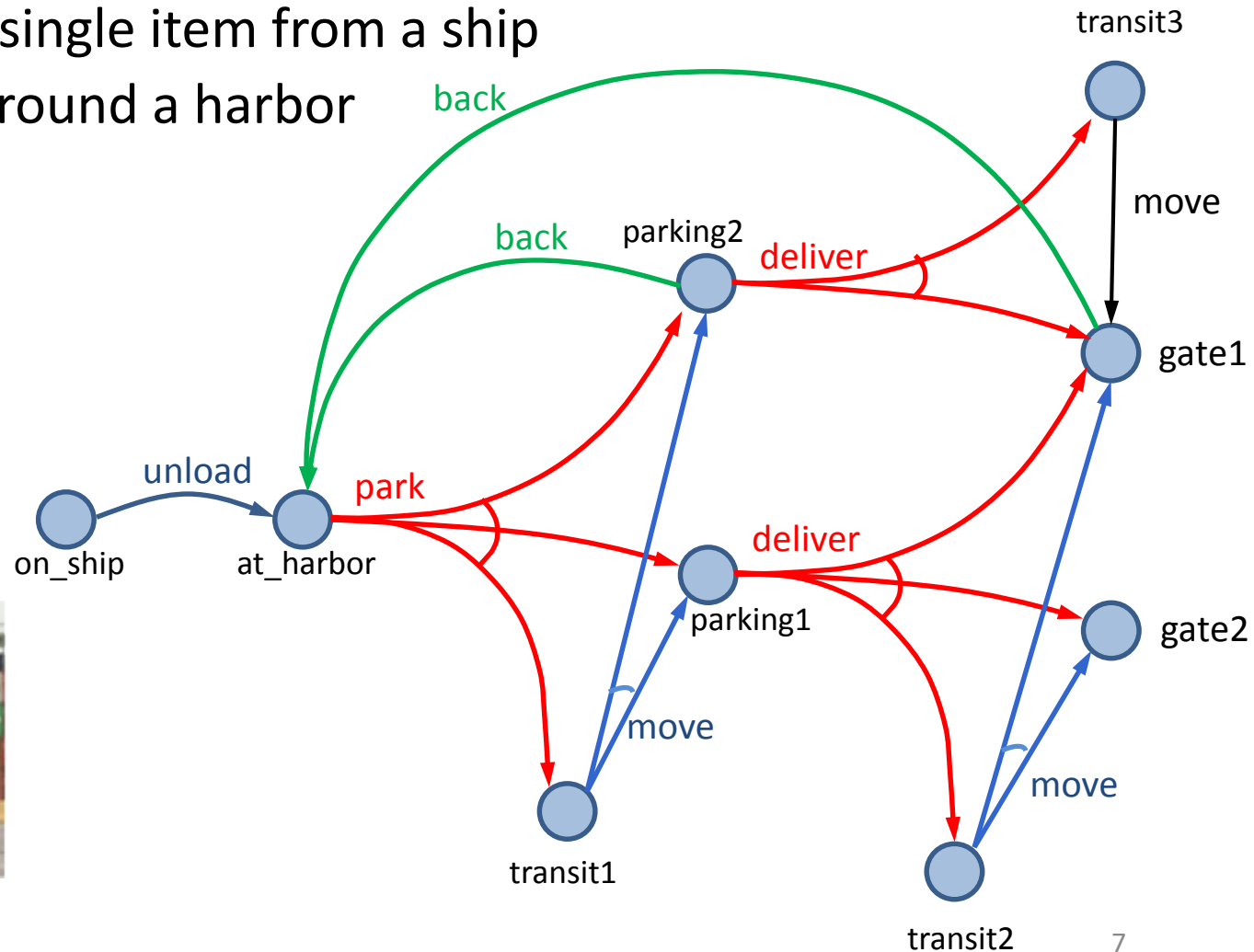


- Analogy to PSP

- *OR* branch \Leftrightarrow action selection
 - *AND* branch \Leftrightarrow flaw selection

Example

- Very simple harbor management domain
 - Unload a single item from a ship
 - Move it around a harbor



Example

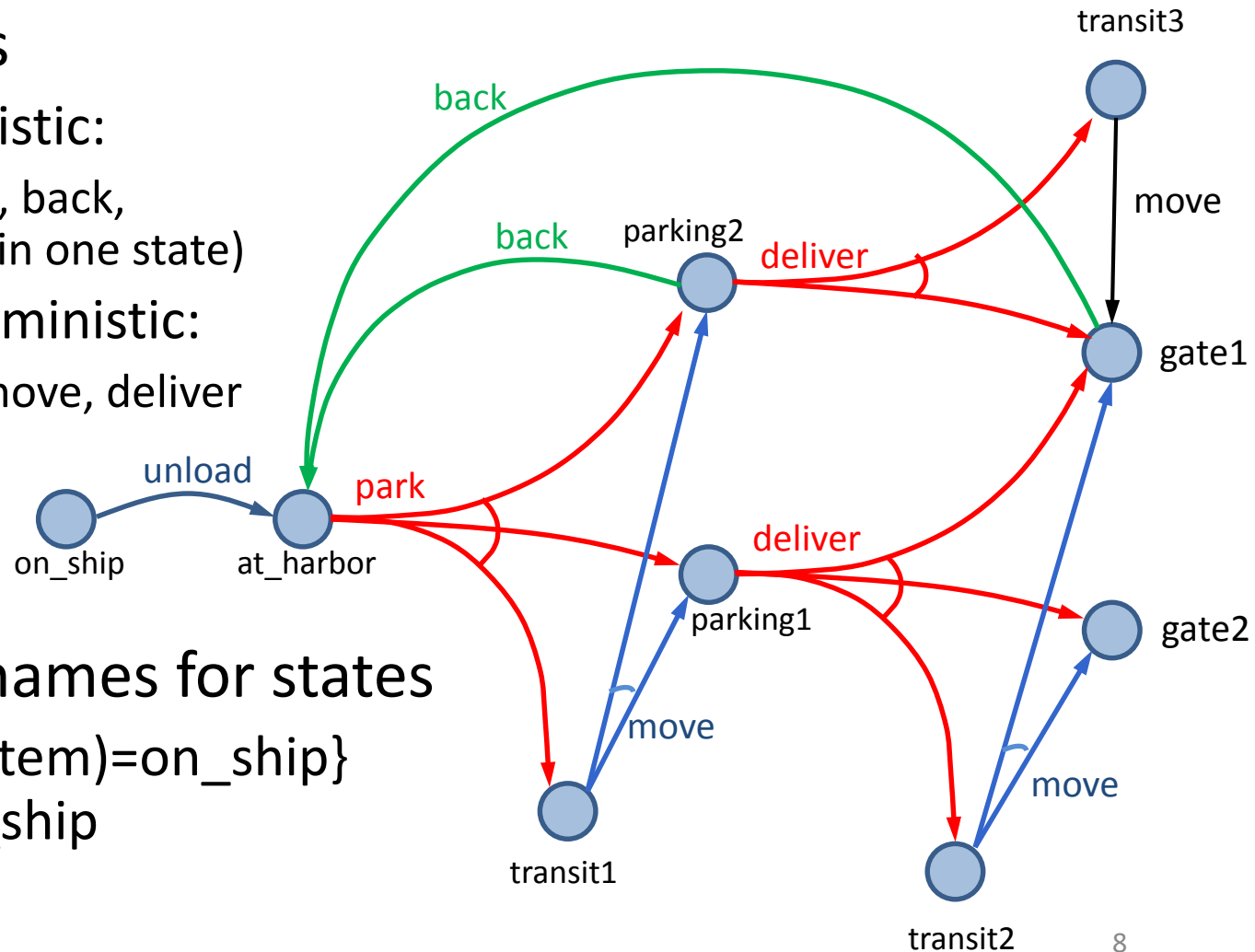
- One state variable: $\text{pos}(\text{item})$

- Five actions

- Deterministic:
 - unload, back, (move in one state)
- Nondeterministic:
 - park, move, deliver

- Simplified names for states

- For $\{\text{pos}(\text{item})=\text{on_ship}\}$ write on_ship



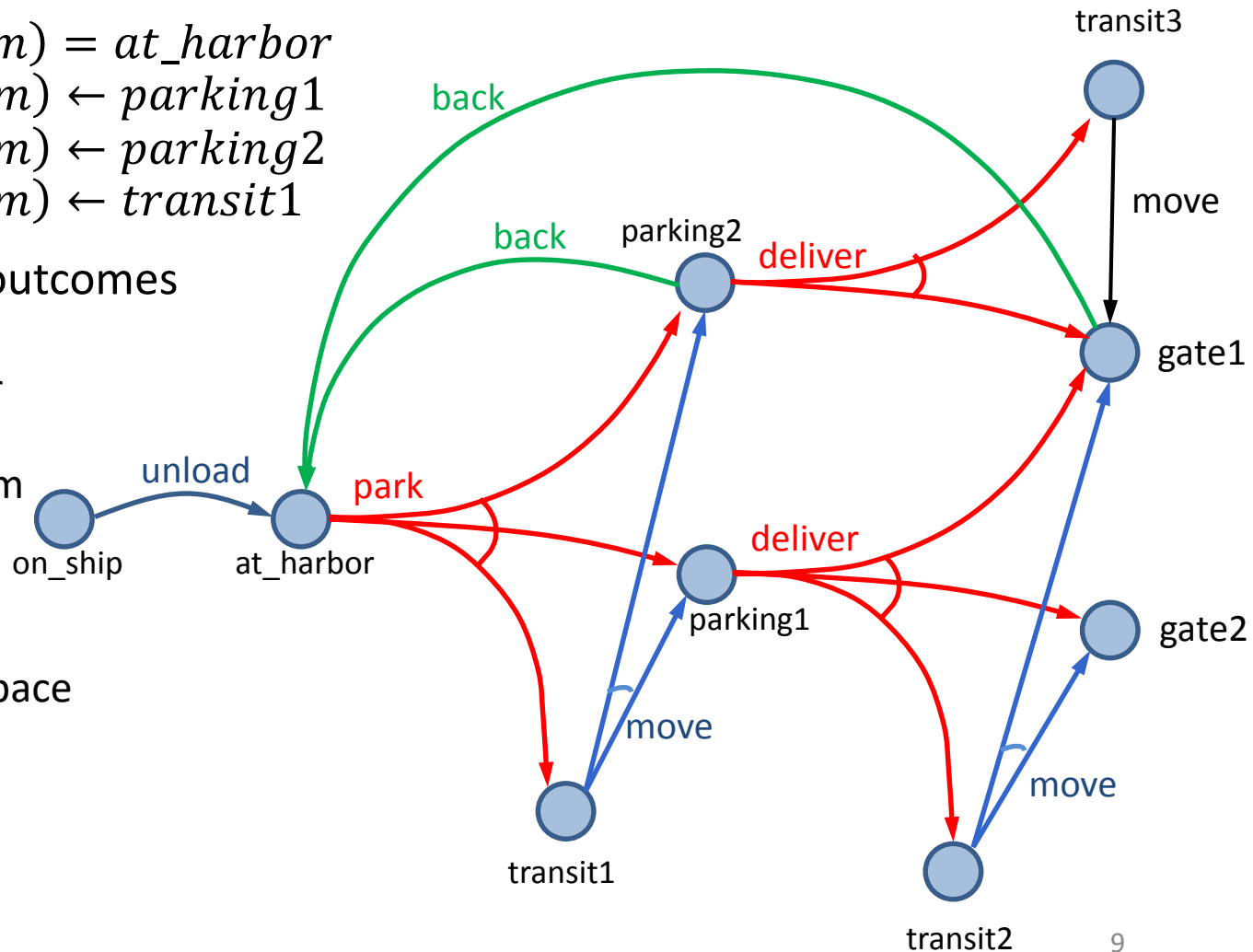
Actions

- Action:
park

pre: $pos(item) = at_harbor$
 eff₁: $pos(item) \leftarrow parking1$
 eff₂: $pos(item) \leftarrow parking2$
 eff₃: $pos(item) \leftarrow transit1$

- Three possible outcomes

- Put item in *parking1* or *parking2* if one of them has space or
- in *transit1* if there is no parking space



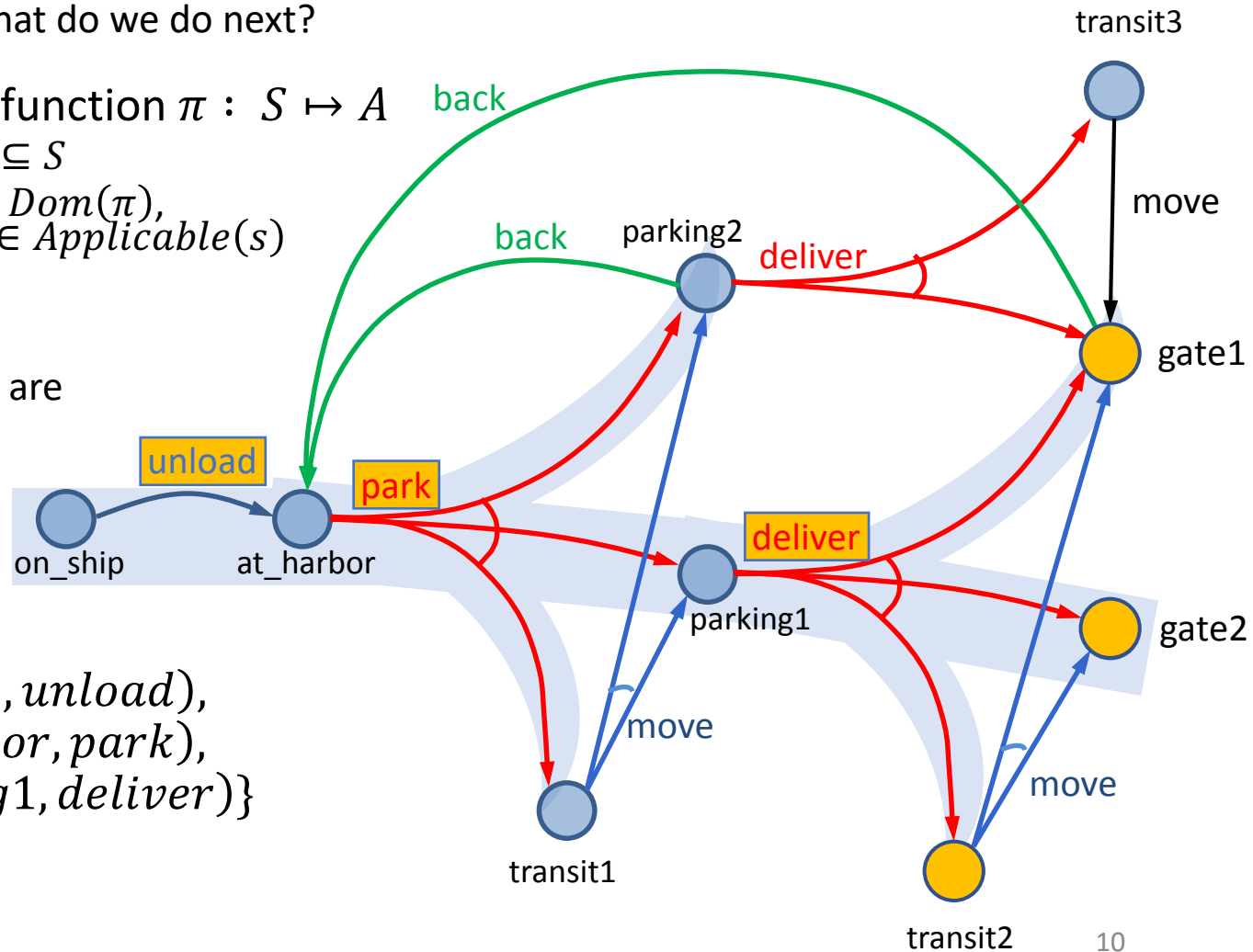
Plans Policies

- Need something more general than a sequence of actions
 - After park, what do we do next?

- **Policy:** a *partial* function $\pi : S \mapsto A$
 - i.e., $Dom(\pi) \subseteq S$
 - For every $s \in Dom(\pi)$, require $\pi(s) \in Applicable(s)$

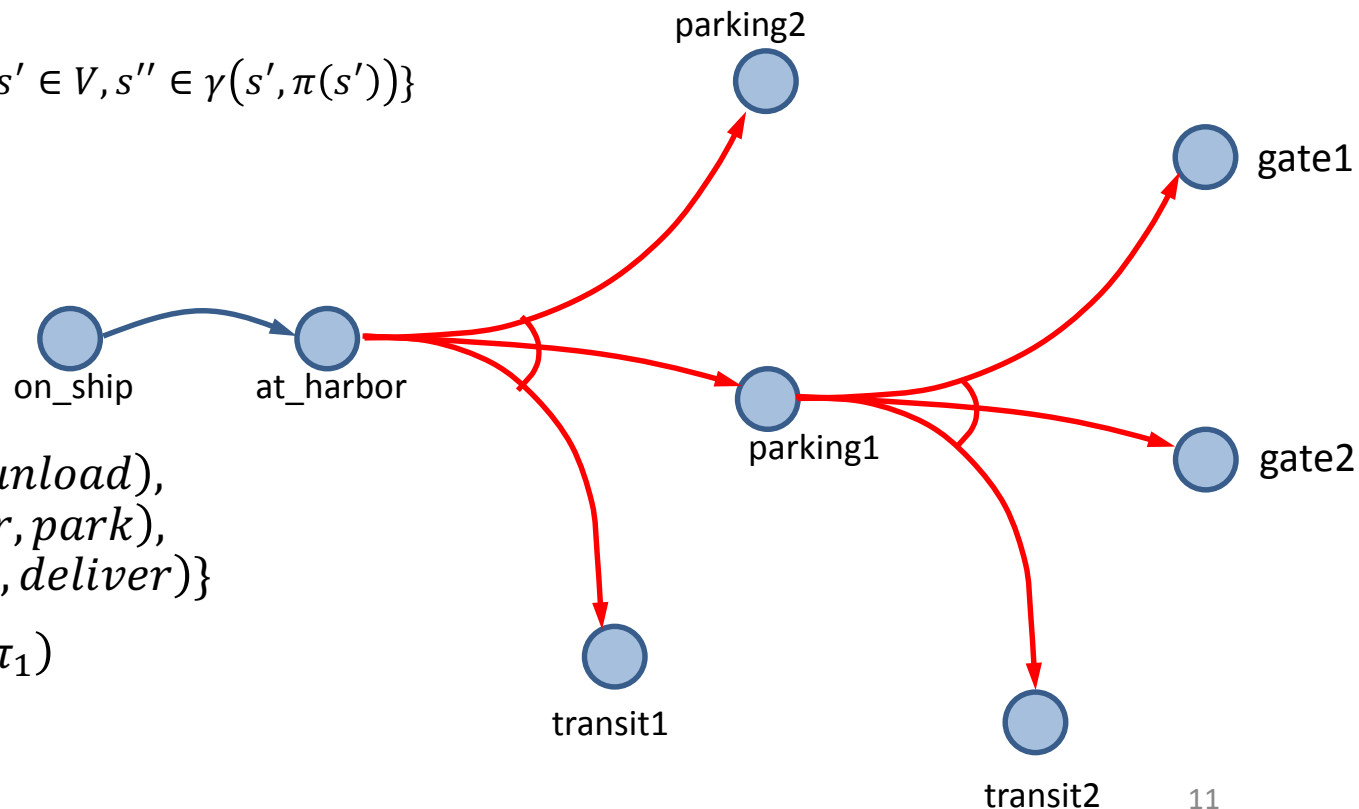
- **Meaning:**
 - Perform $\pi(s)$ whenever we are in state s

- $\pi_1 = \{(on_ship, unload), (at_harbor, park), (parking1, deliver)\}$



Definitions Over Policies

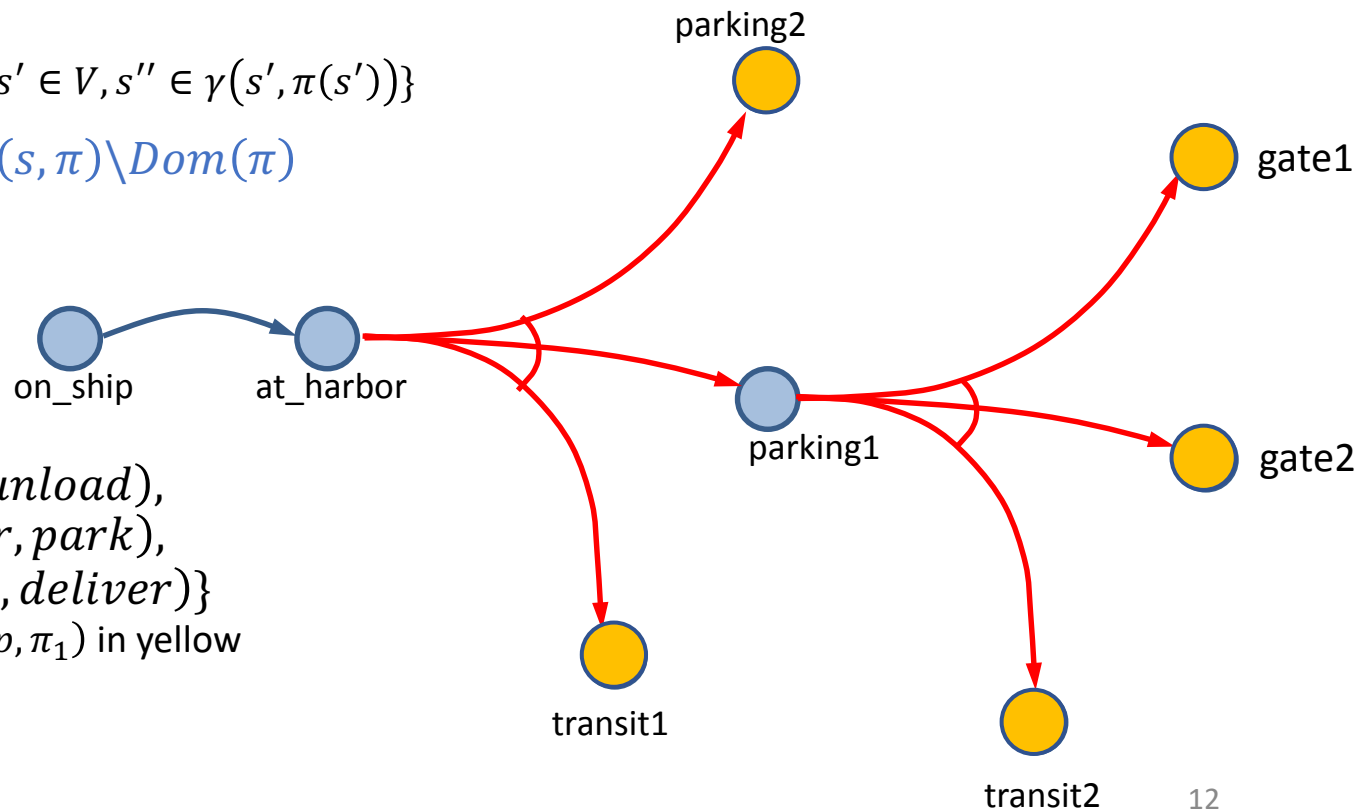
- **Transitive closure:**
{all states reachable from s using π }
 - $\hat{\gamma}(s, \pi) = S_0 \cup S_1 \cup S_2 \cup \dots$
 - $S_0 = \{s\}$
 - $S_{i+1} = \cup\{\gamma(s, \pi(s)) \mid s \in S_i\}, i \geq 0$
- **Reachability graph** $Graph(s, \pi) = (V, E)$
 - $V = \hat{\gamma}(s, \pi)$
 - $E = \{(s', s'') \mid s' \in V, s'' \in \gamma(s', \pi(s'))\}$



- $\pi_1 = \{(on_ship, unload), (at_harbor, park), (parking1, deliver)\}$
- $Graph(on_ship, \pi_1)$

Definitions Over Policies

- **Transitive closure:**
{all states reachable from s using π }
 - $\hat{\gamma}(s, \pi) = S_0 \cup S_1 \cup S_2 \cup \dots$
 - $S_0 = \{s\}$
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- **Reachability graph** $Graph(s, \pi) = (V, E)$
 - $V = \hat{\gamma}(s, \pi)$
 - $E = \{(s', s'') \mid s' \in V, s'' \in \gamma(s', \pi(s'))\}$
- $leaves(s, \pi) = \hat{\gamma}(s, \pi) \setminus Dom(\pi)$
 - May be empty



- $\pi_1 = \{(on_ship, unload), (at_harbor, park), (parking1, deliver)\}$
 - $leaves(on_ship, \pi_1)$ in yellow

Performing a Policy

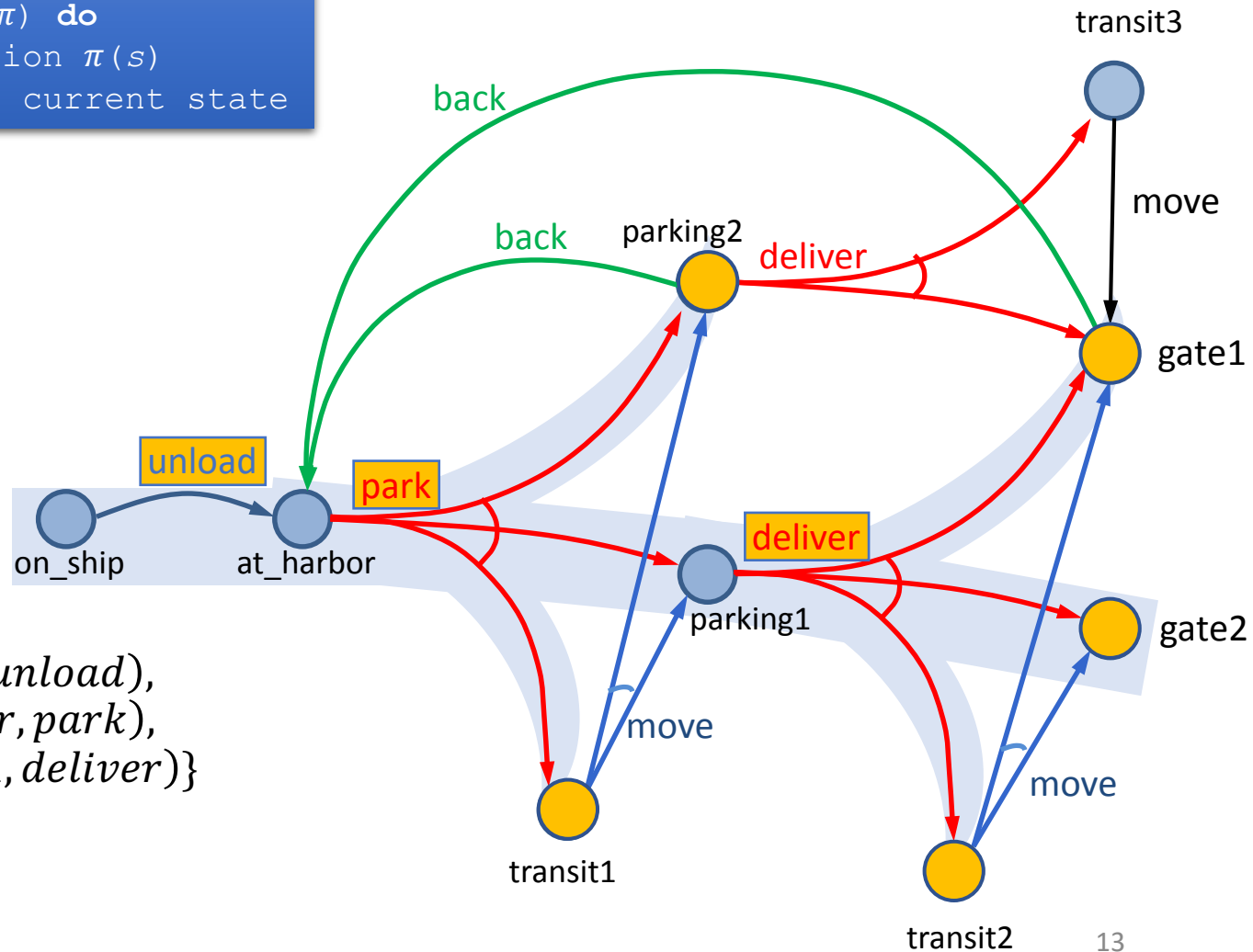
```
PerformPolicy( $\pi$ )
```

```
   $s \leftarrow$  observe current state
```

```
  while  $s \in \text{Dom}(\pi)$  do
```

```
    perform action  $\pi(s)$ 
```

```
     $s \leftarrow$  observe current state
```



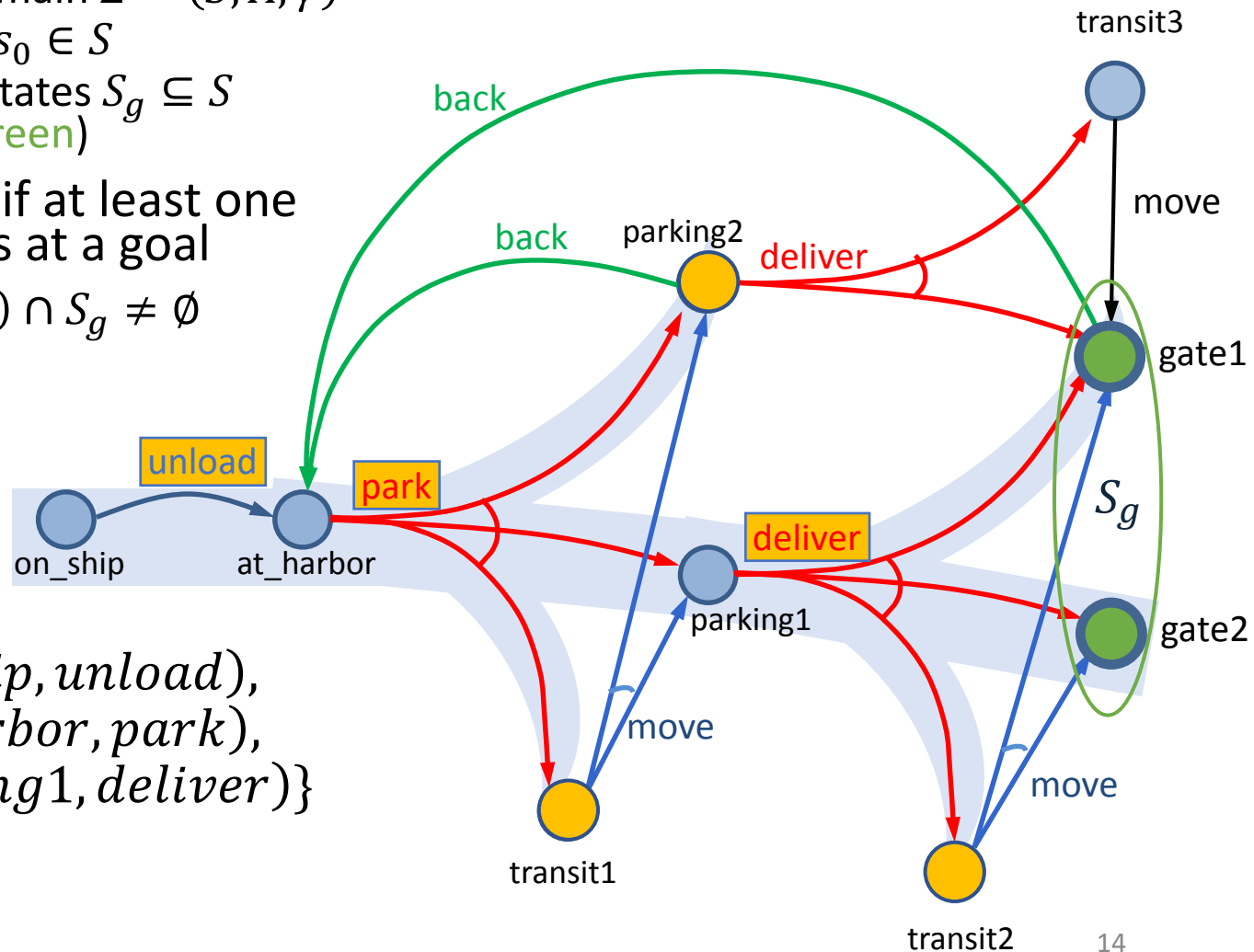
- $\pi_1 = \{(on_ship, unload), (at_harbor, park), (parking1, deliver)\}$

Planning Problems and Solutions

- Planning problem $P = (\Sigma, s_0, S_g)$
 - Planning domain $\Sigma = (S, A, \gamma)$
 - Initial state $s_0 \in S$
 - Set of goal states $S_g \subseteq S$ (shown in green)
- π is a **solution** if at least one execution ends at a goal
 - $leaves(s, \pi) \cap S_g \neq \emptyset$

Is π_1 a solution?

- $\pi_1 = \{(on_ship, unload), (at_harbor, park), (parking1, deliver)\}$

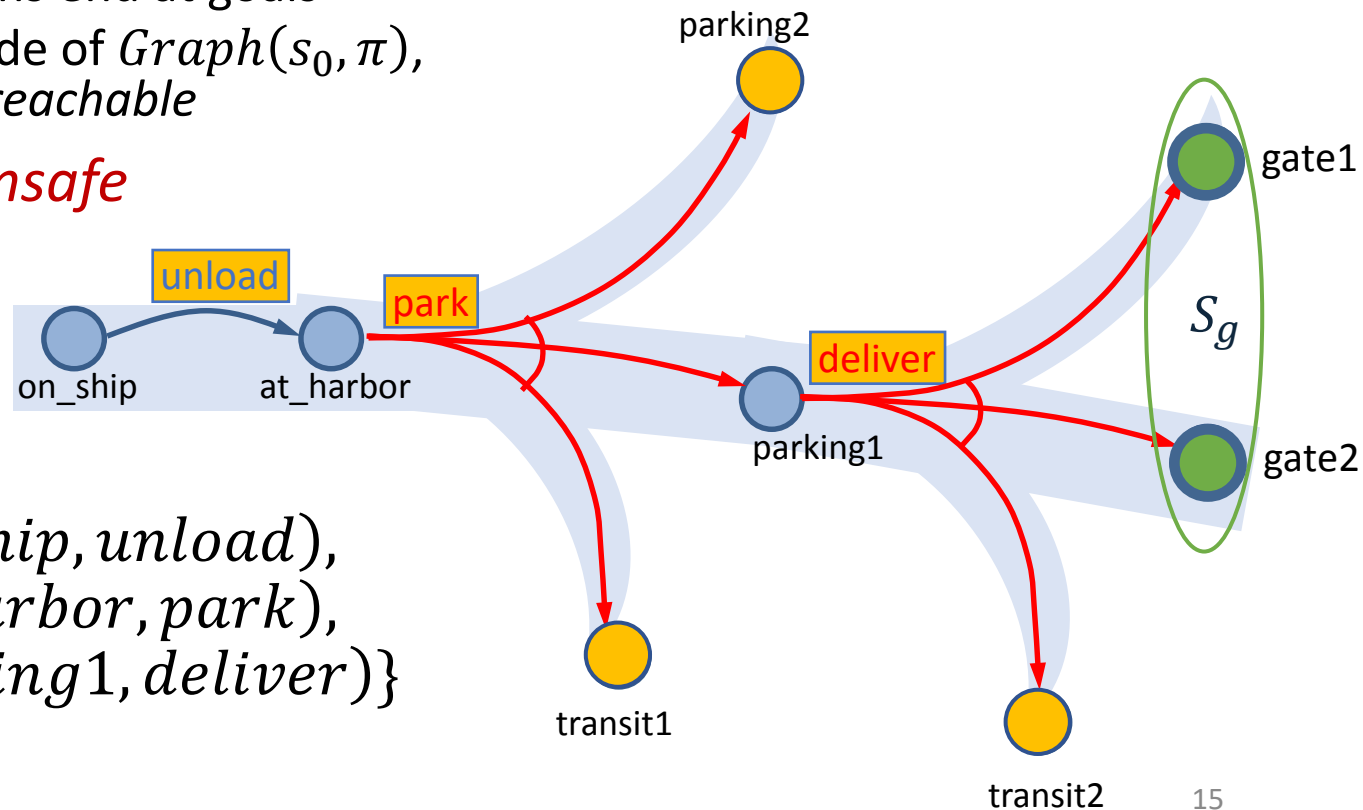


Safe Solutions

- A solution π is **safe** if

$$\forall s \in \hat{\gamma}(s_0, \pi), \\ \text{leaves}(s, \pi) \cap S_g \neq \emptyset$$

- ~~all executions end at goals~~
- at every node of $\text{Graph}(s_0, \pi)$, the goal is *reachable*
- Otherwise, **unsafe**

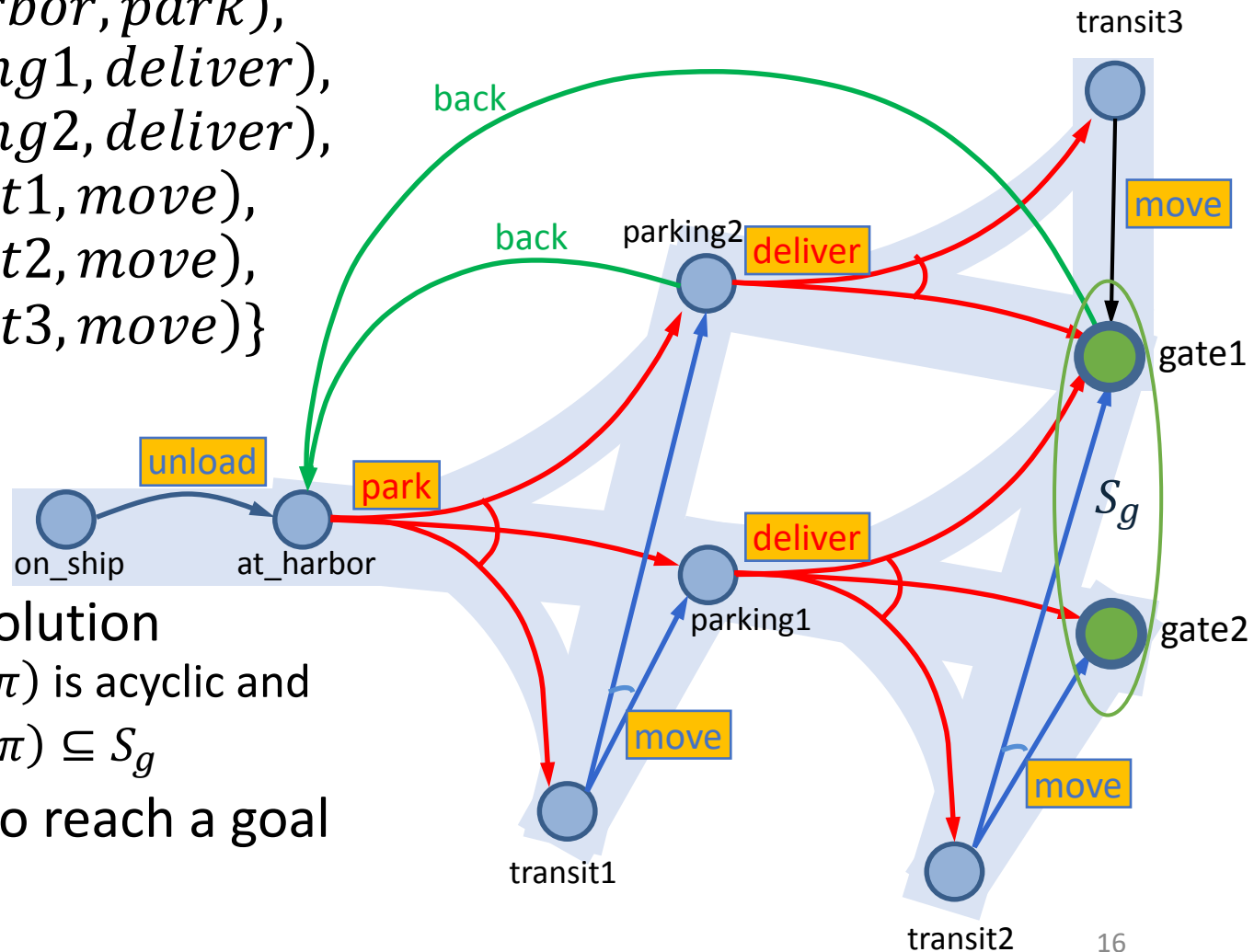


Is π_1 safe?

- $\pi_1 = \{(on_ship, unload), (at_harbor, park), (parking1, deliver)\}$

Safe Solutions

- $\pi_2 = \{(on_ship, unload), (at_harbor, park), (parking1, deliver), (parking2, deliver), (transit1, move), (transit2, move), (transit3, move)\}$



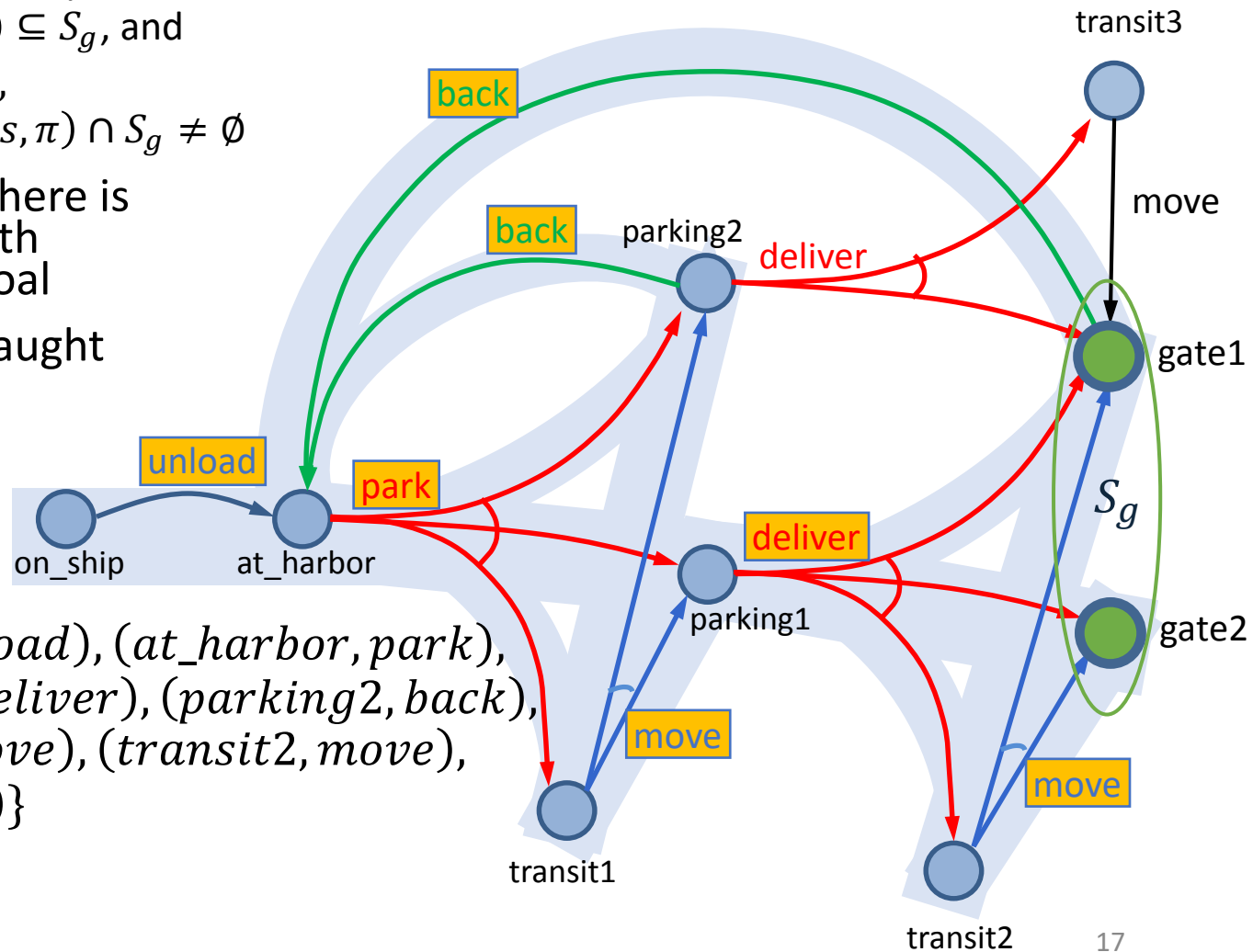
- **Acyclic safe solution**
 - $Graph(s_0, \pi)$ is acyclic and
 - $leaves(s_0, \pi) \subseteq S_g$
- Guaranteed to reach a goal

Safe Solutions

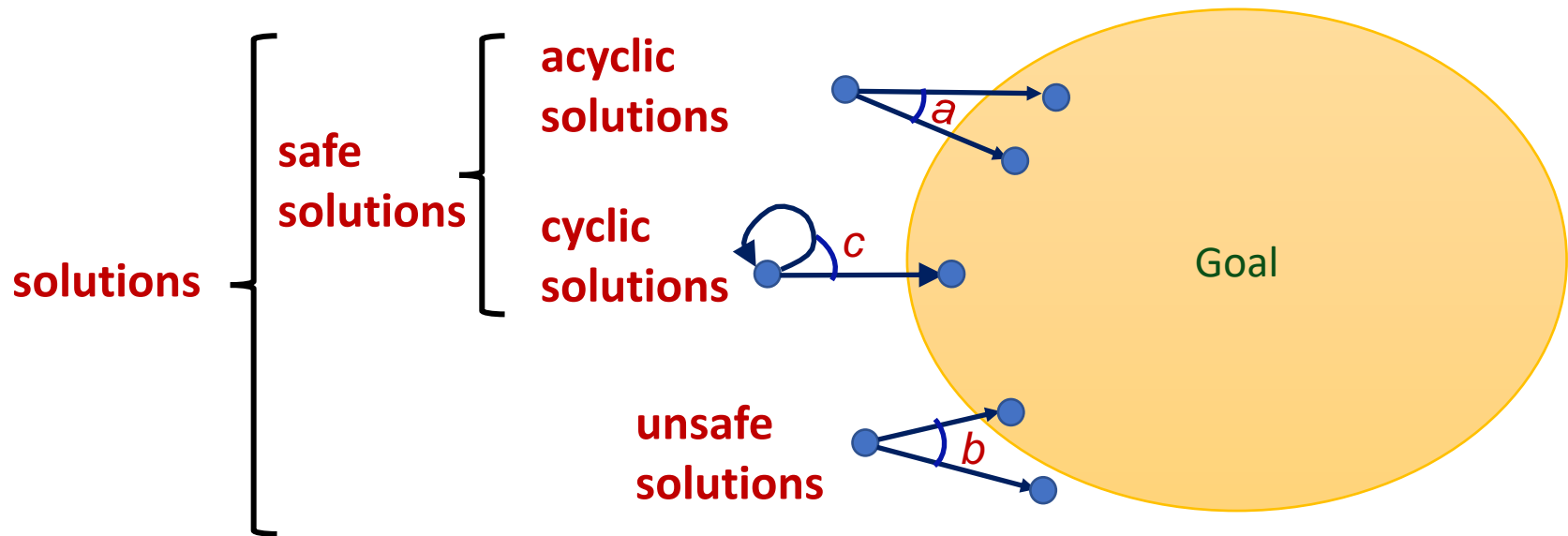
- **Cyclic** safe solution
 - $Graph(s_0, \pi)$ is cyclic,
 - $leaves(s_0, \pi) \subseteq S_g$, and
 - $\forall s \in \hat{\gamma}(s_0, \pi), leaves(s, \pi) \cap S_g \neq \emptyset$

- At every state, there is an execution path that ends at a goal
- Will never get caught in a dead end

- $\pi_3 =$
 $\{(on_ship, unload), (at_harbor, park), (parking1, deliver), (parking2, back), (transit1, move), (transit2, move), (gate1, back)\}$



Kinds of Solutions



Intermediate Summary

- Planning Problems
 - Planning domains
 - Plans as policies
 - Planning problems and solutions
 - Types of solutions: safe, unsafe, acyclic, cyclic

Outline per the Book

5.2 Planning Problem

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5.6 Online Approaches

- Lookahead
- Lookahead by Determinisation
- Lookahead with a bounded number of steps

Finding (Unsafe) Solutions

For comparison:
Forward-search with
deterministic models

Find-Solution (Σ, s_0, S_g)

```
 $s \leftarrow s_0$   
 $\pi \leftarrow \emptyset$   
 $Visited \leftarrow \{s_0\}$   
loop  
  if  $s \in S_g$  then  
    return  $\pi$   
   $A' \leftarrow \text{Applicable}(s)$   
  if  $A' = \emptyset$  then  
    return failure  
  nondeterministically choose  $a \in A'$   
  nondeterministically choose  $s' \in \gamma(s, a)$   
  if  $s' \in Visited$  then  
    return failure  
   $\pi(s) \leftarrow a$   
   $Visited \leftarrow Visited \cup \{s'\}$   
   $s \leftarrow s'$ 
```

Forward-search (Σ, s_0, g)

```
 $s \leftarrow s_0$   
 $\pi \leftarrow \langle \rangle$   
loop  
  if  $s$  satisfies  $g$  then  
    return  $\pi$   
   $A' \leftarrow \{a \in A \mid a \text{ is applicable in } s\}$   
  if  $A' = \emptyset$  then  
    return failure  
  nondeterministically choose  $a \in A'$   
   $s \leftarrow \gamma(s, a)$   
   $\pi \leftarrow \pi.a$ 
```

Decide which state to plan for

Cycle-checking

Find-Solution(Σ, s_0, S_g)

$s \leftarrow s_0$

$\pi \leftarrow \emptyset$

$Visited \leftarrow \{s_0\}$

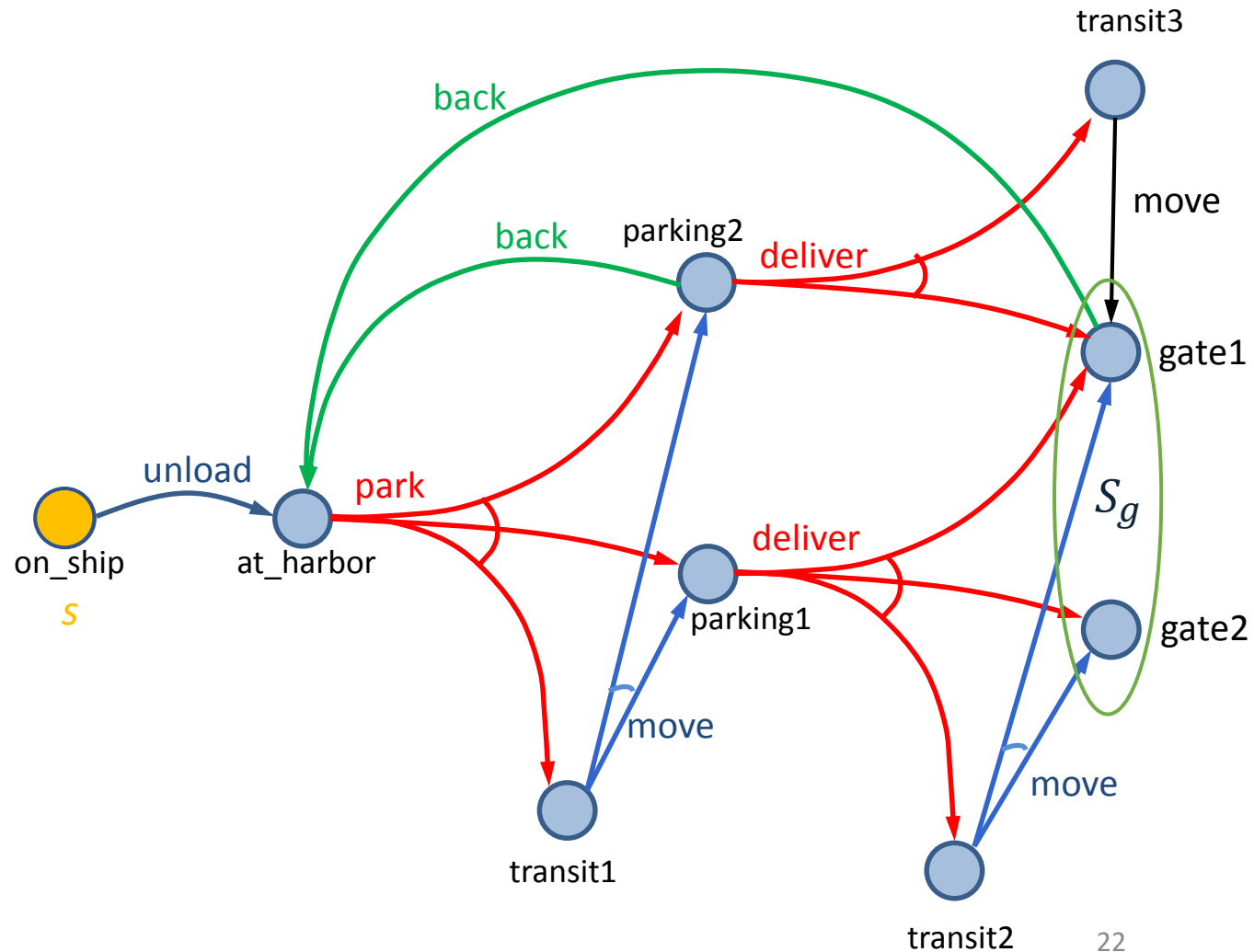
...

Example

$s = \text{on_ship}$

$\pi = \{\}$

$Visited = \{\text{on_ship}\}$



Find-Solution(Σ, s_0, S_g)

...

loop

if $s \in S_g$ then

return π

...

nondeterministically choose $a \in \text{Applicable}(s)$

nondeterministically choose $s' \in \gamma(s, a)$

...

$\pi(s) \leftarrow a$

$\text{Visited} \leftarrow \text{Visited} \cup \{s'\}$

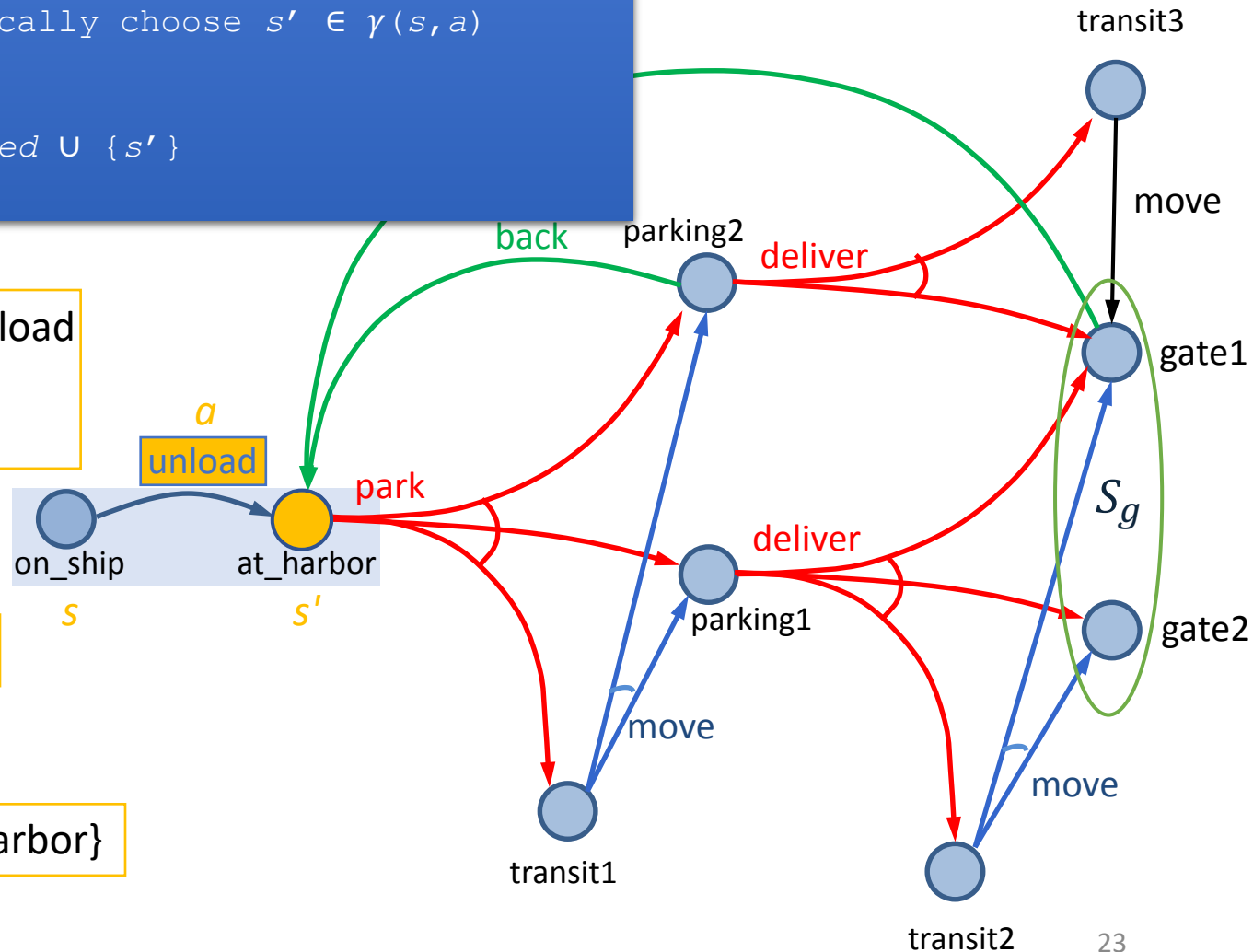
$s \leftarrow s'$

Example

$s = \text{on_ship}$, $a = \text{unload}$
 $\gamma(s, a) = \{\text{at_harbor}\}$
 $s' = \text{at_harbor}$

$\pi = \{(\text{on_ship}, \text{unload})\}$

$\text{Visited} = \{\text{on_ship}, \text{at_harbor}\}$



Find-Solution(Σ, s_0, S_g)

...

loop

if $s \in S_g$ then

return π

...

nondeterministically choose $a \in \text{Applicable}(s)$

nondeterministically choose $s' \in \gamma(s, a)$

...

$\pi(s) \leftarrow a$

$Visited \leftarrow Visited \cup \{s'\}$

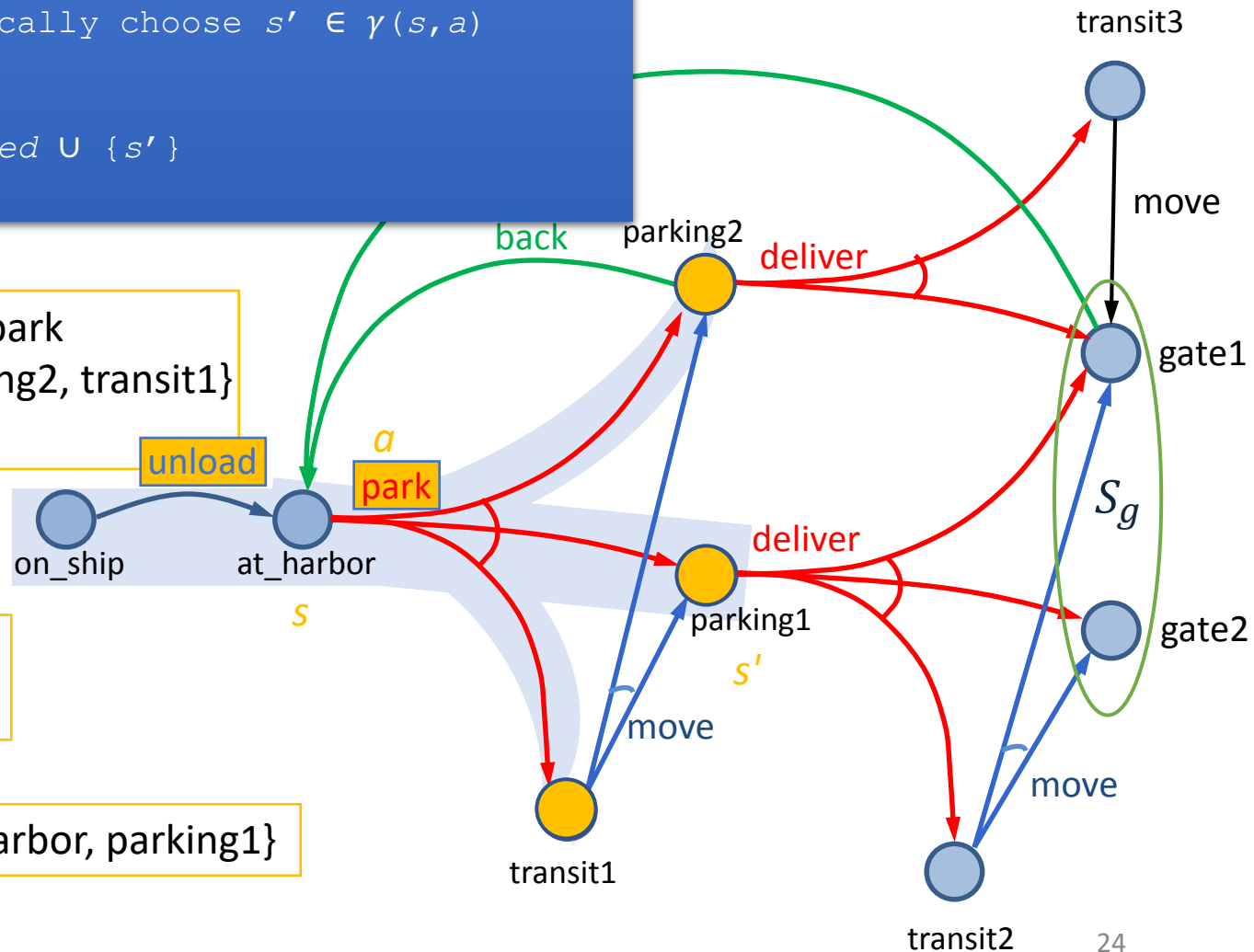
$s \leftarrow s'$

Example

$s = \text{at_harbor}$, $a = \text{park}$
 $\gamma(s, a) = \{\text{parking1}, \text{parking2}, \text{transit1}\}$
 $s' = \text{parking1}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park})\}$

$Visited = \{\text{on_ship}, \text{at_harbor}, \text{parking1}\}$



Find-Solution(Σ, s_0, S_g)

...

loop
 if $s \in S_g$ then
 return π

...

nondeterministically choose $a \in \text{Applicable}(s)$
 nondeterministically choose $s' \in \gamma(s, a)$

...

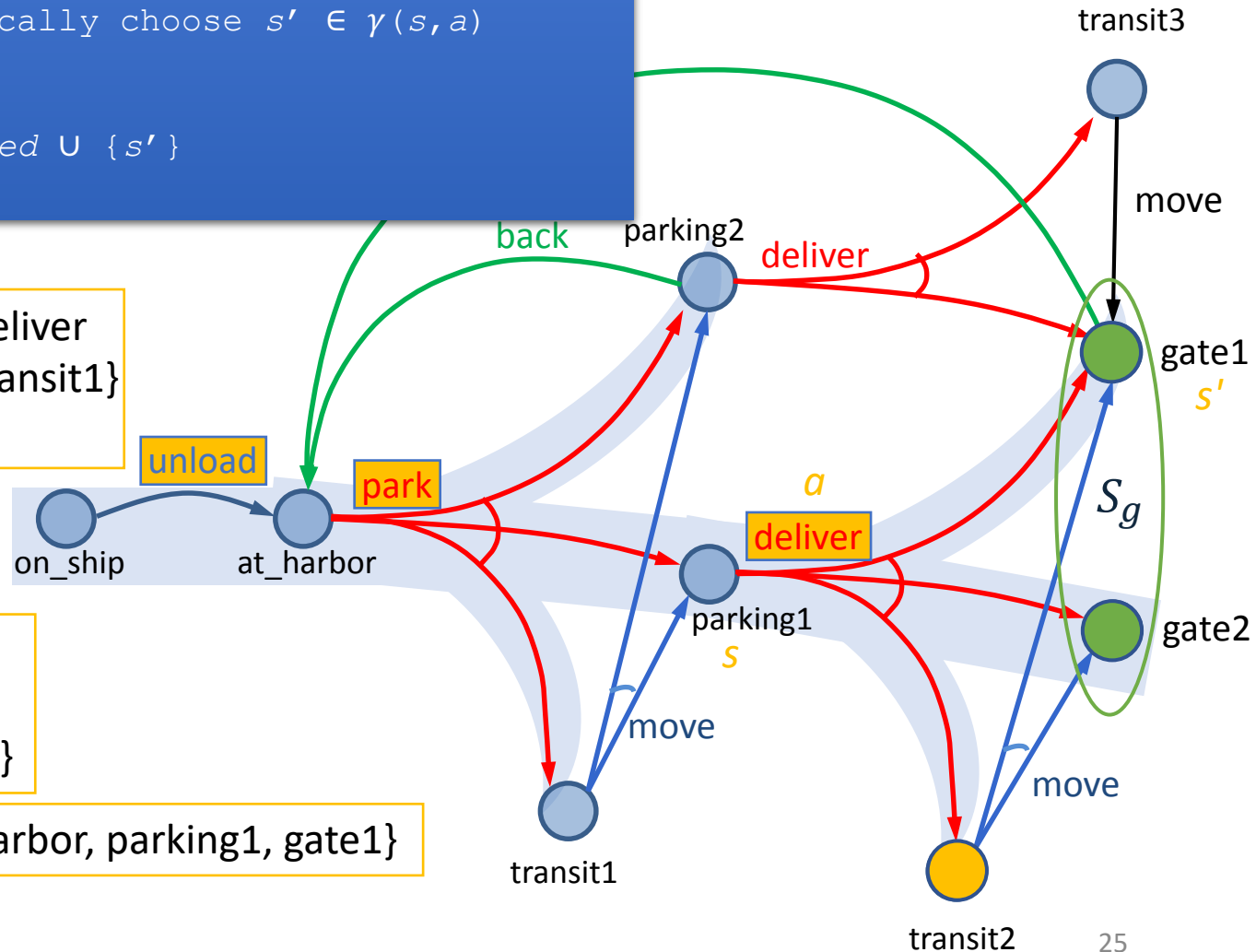
$\pi(s) \leftarrow a$
 $Visited \leftarrow Visited \cup \{s'\}$
 $s \leftarrow s'$

Example

$s = \text{parking1}, a = \text{deliver}$
 $\gamma(s, a) = \{\text{gate1}, \text{gate2}, \text{transit1}\}$
 $s' = \text{gate1}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver})\}$

$Visited = \{\text{on_ship}, \text{at_harbor}, \text{parking1}, \text{gate1}\}$



Find-Solution(Σ, s_0, S_g)

...

loop

if $s \in S_g$ then

return π

...

nondeterministically choose $a \in \text{Applicable}(s)$

nondeterministically choose $s' \in \gamma(s, a)$

...

$\pi(s) \leftarrow a$

$Visited \leftarrow Visited \cup \{s'\}$

$s \leftarrow s'$

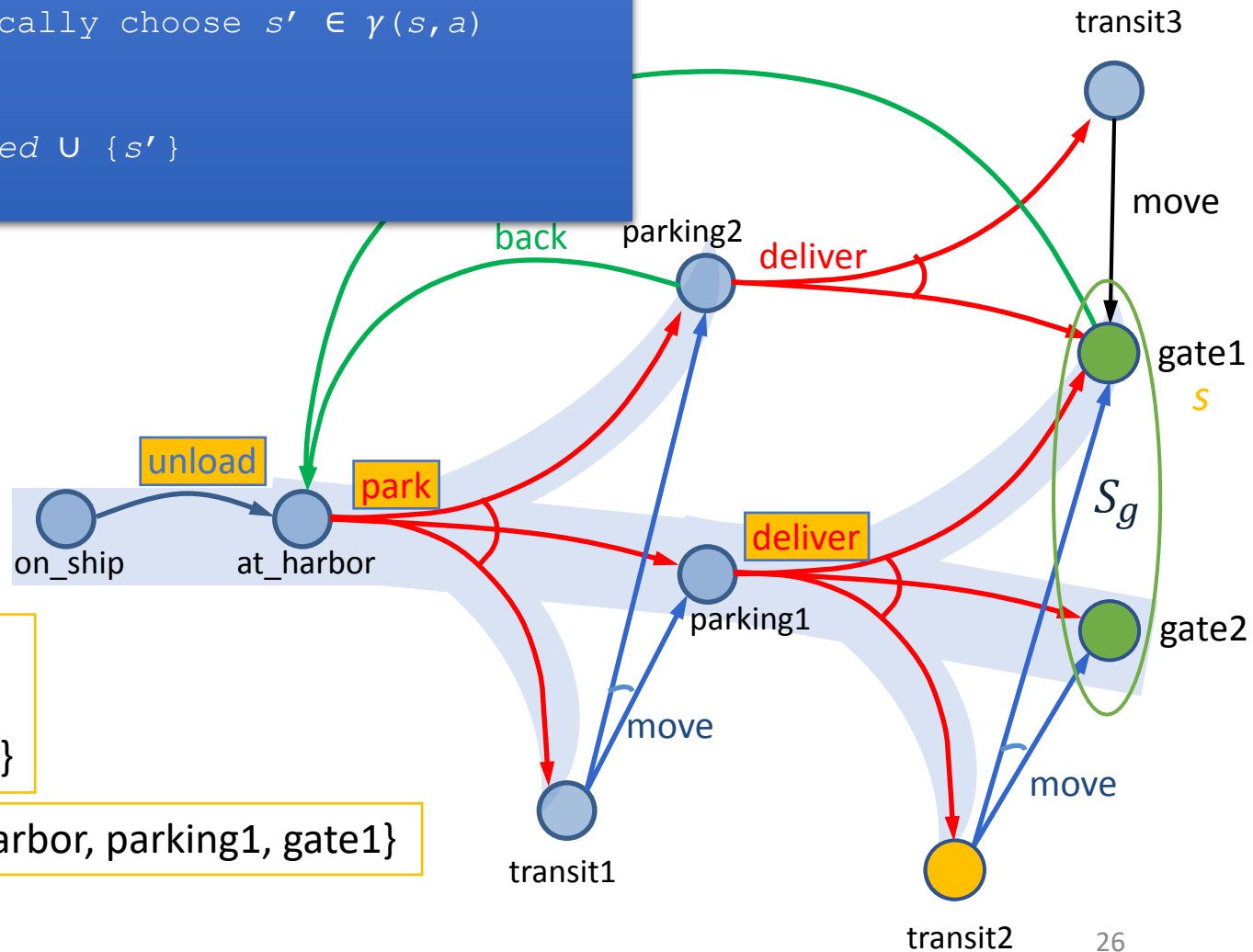
Example

$s = \text{gate1}$

Gate1 is a goal,
so return π

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver})\}$

$Visited = \{\text{on_ship}, \text{at_harbor}, \text{parking1}, \text{gate1}\}$



Finding Acyclic Safe Solutions

```
Find-Acyclic-Solution( $\Sigma, s_0, S_g$ )
```

```
 $\pi \leftarrow \emptyset$ 
```

```
Frontier  $\leftarrow \{s_0\}$ 
```

```
for every  $s \in \text{Frontier} \setminus S_g$  do
```

```
  Frontier  $\leftarrow \text{Frontier} \setminus \{s\}$ 
```

```
  if Applicable( $s$ ) =  $\emptyset$  then
```

```
    return failure
```

```
  nondeterministically choose  $a \in \text{Applicable}(s)$ 
```

```
   $\pi \leftarrow \pi \cup (s, a)$ 
```

```
  Frontier  $\leftarrow \text{Frontier} \cup (\gamma(s, a) \setminus \text{Dom}(\pi))$ 
```

```
  if has-loops( $\pi, s, \text{Frontier}$ ) then
```

```
    return failure
```

```
return  $\pi$ 
```

Keep track of unexpanded states, like A^*

Add all outcomes that π does not already handle

Cycle-checking

- Check for cycles

- For each $s' \in (\gamma(s, a) \cap \text{Dom}(\pi))$

- Is $s' \in \hat{\gamma}(s', \pi)$?

- Formally, *has-loops*($\pi, s, \text{Frontier}$) iff

- $\exists s' \in (\gamma(s, a) \cap \text{Dom}(\pi)) : s' \in \hat{\gamma}(s', \pi)$

- I.e., a state s' is reachable from itself

Find-Acyclic-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

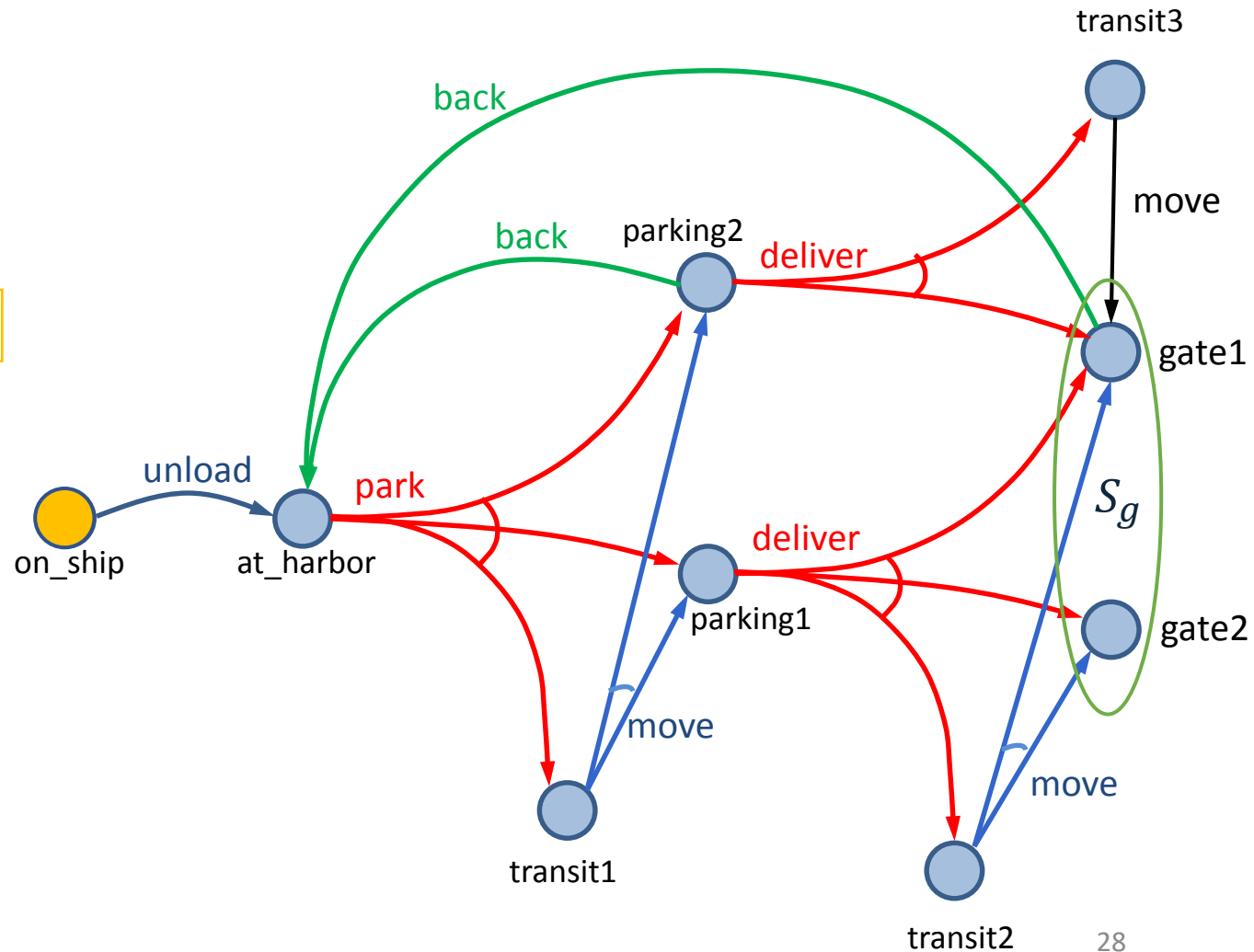
$Frontier \leftarrow \{s_0\}$

...

Example

$Frontier \setminus S_g = \{on_ship\}$

$\pi = \{\}$



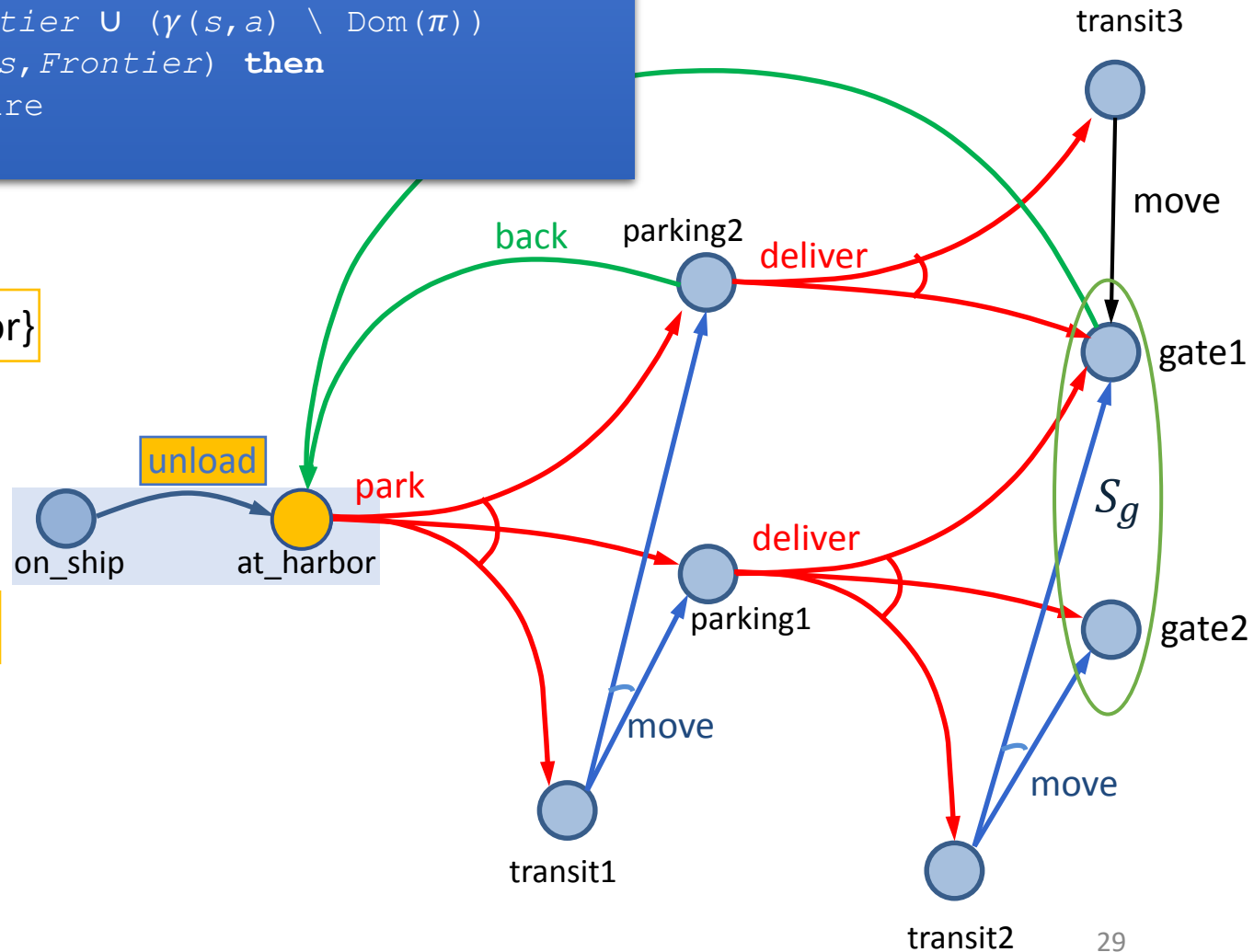
Find-Acyclic-Solution(Σ, s_0, S_g)

```
...  
for every  $s \in \text{Frontier} \setminus S_g$  do  
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }  
  ...  
  nondeterministically choose  $a \in \text{Applicable}(s)$   
   $\pi \leftarrow \pi \cup (s, a)$   
  Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )  
  if has-loops( $\pi, s, \text{Frontier}$ ) then  
    return failure  
return  $\pi$ 
```

$s = \text{on_ship}$

$\text{Frontier} \setminus S_g = \{\text{at_harbor}\}$

$\pi = \{(\text{on_ship}, \text{unload})\}$



Example

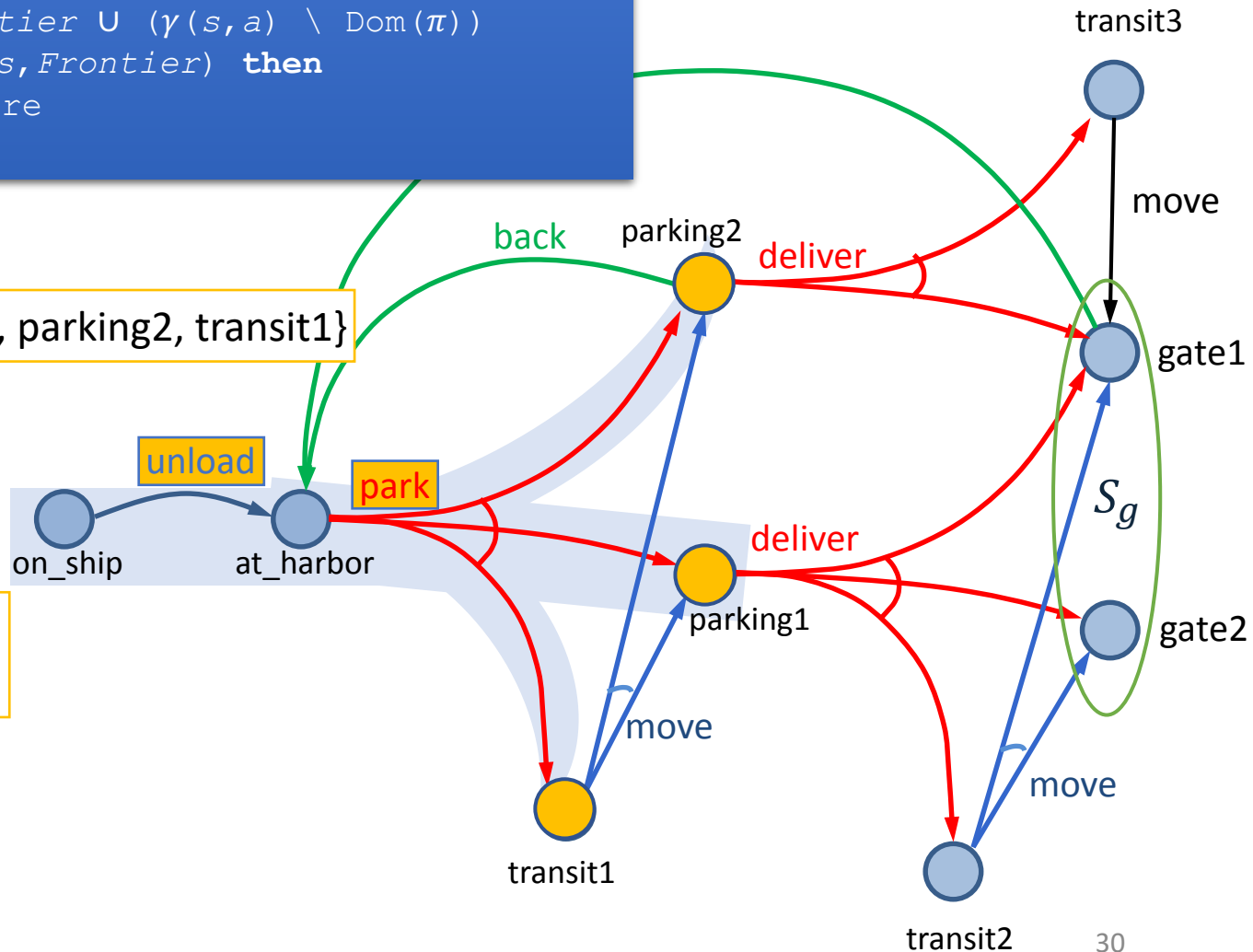
Find-Acyclic-Solution(Σ, s_0, S_g)

```
...
for every  $s \in \text{Frontier} \setminus S_g$  do
  Frontier  $\leftarrow$  Frontier  $\setminus$  {s}
  ...
  nondeterministically choose  $a \in \text{Applicable}(s)$ 
   $\pi \leftarrow \pi \cup (s, a)$ 
  Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )
  if has-loops( $\pi, s, \text{Frontier}$ ) then
    return failure
return  $\pi$ 
```

$s = \text{at_harbor}$

$\text{Frontier} \setminus S_g = \{\text{parking1}, \text{parking2}, \text{transit1}\}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park})\}$



Example

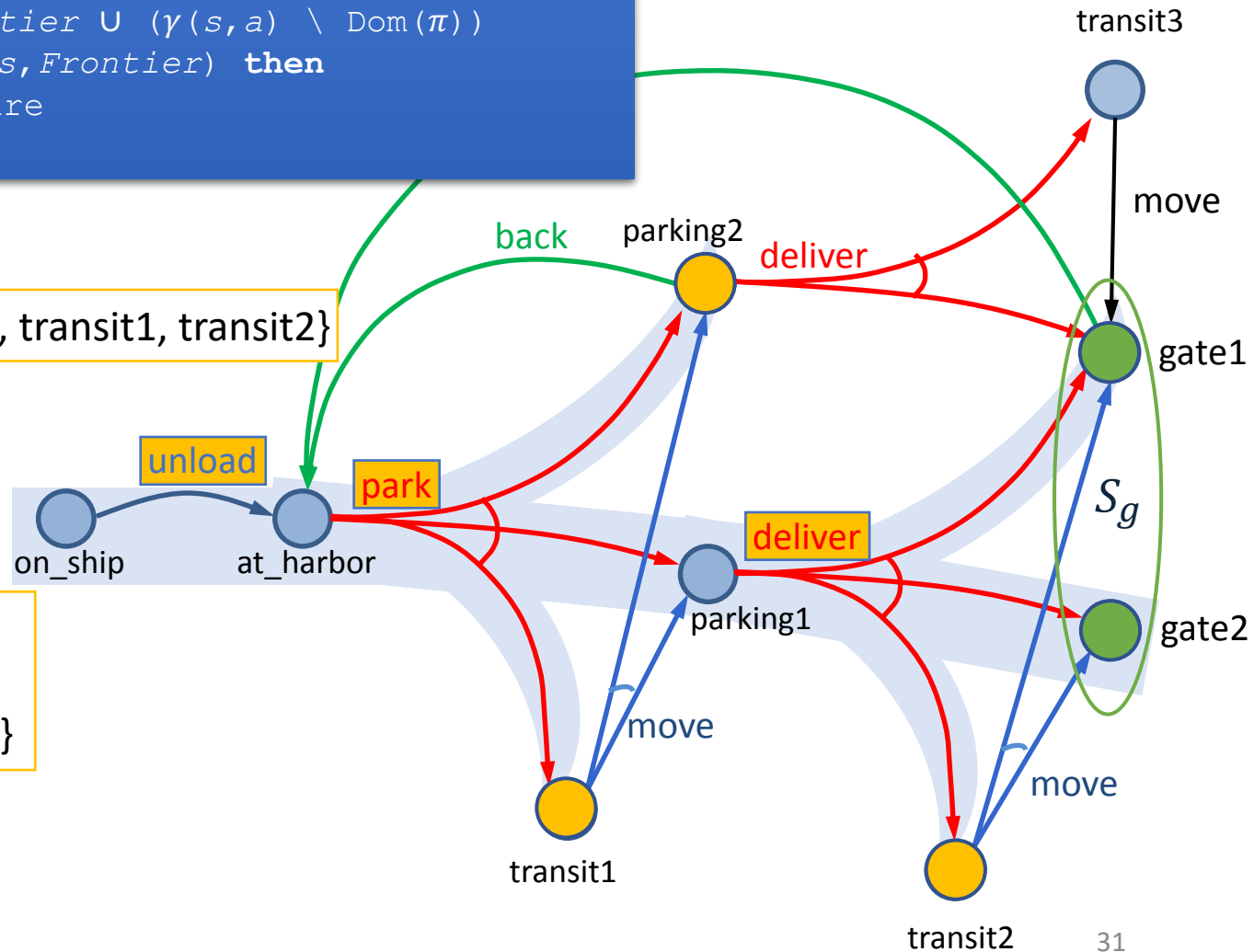
Find-Acyclic-Solution(Σ, s_0, S_g)

```
...  
for every  $s \in \text{Frontier} \setminus S_g$  do  
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }  
  ...  
  nondeterministically choose  $a \in \text{Applicable}(s)$   
   $\pi \leftarrow \pi \cup (s, a)$   
  Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )  
  if has-loops( $\pi, s, \text{Frontier}$ ) then  
    return failure  
return  $\pi$ 
```

$s = \text{parking1}$

$\text{Frontier} \setminus S_g = \{\text{parking2}, \text{transit1}, \text{transit2}\}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver})\}$



Example

Find-Acyclic-Solution(Σ, s_0, S_g)

```
...
for every  $s \in \text{Frontier} \setminus S_g$  do
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }
...
nondeterministically choose  $a \in \text{Appl}(s)$ 
 $\pi \leftarrow \pi \cup (s, a)$ 
Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )
if has-loops( $\pi, s, \text{Frontier}$ ) then
  return failure
return  $\pi$ 
```

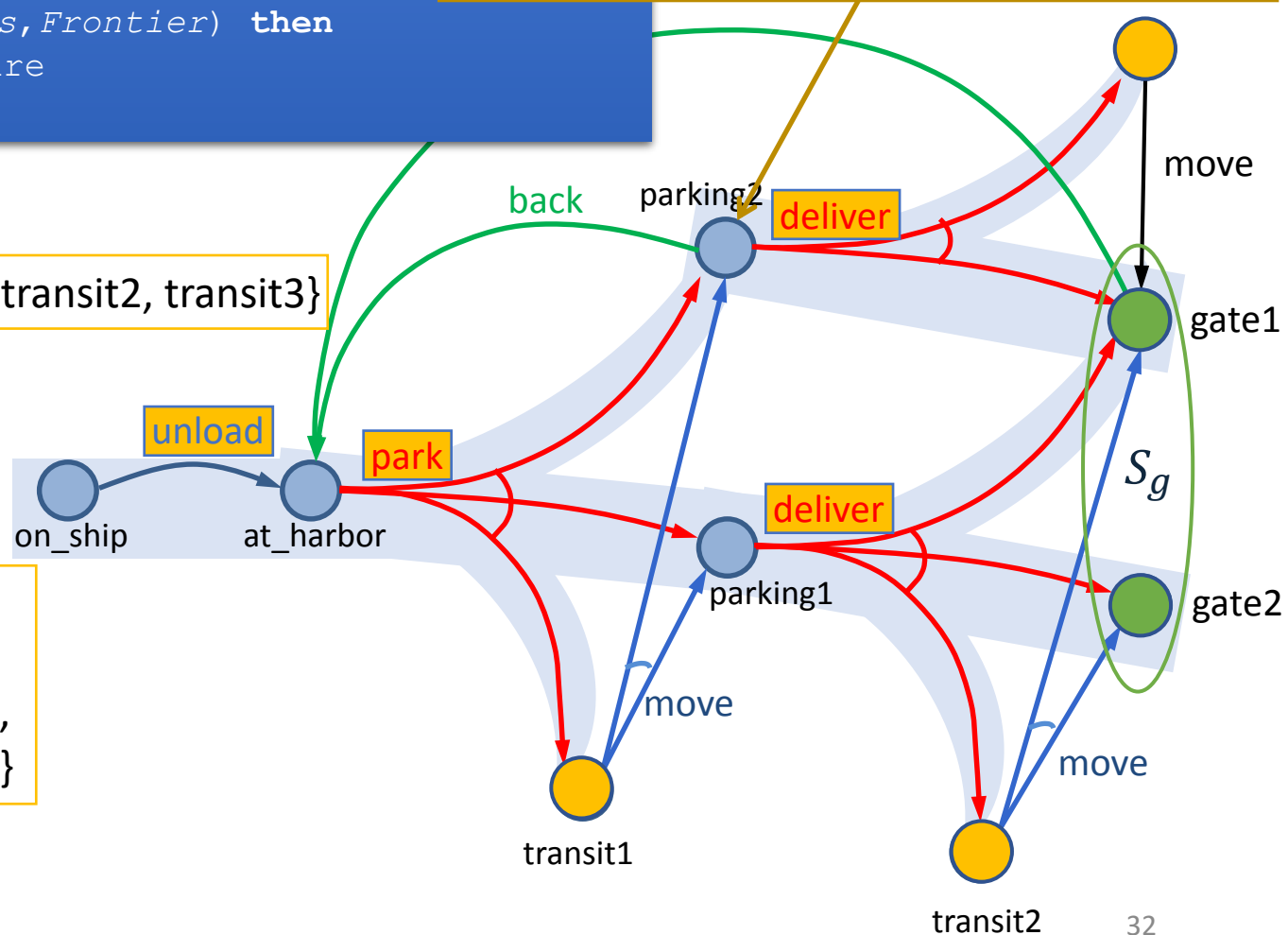
Example

- nondeterministically choose back or deliver
- back \Rightarrow cycle, so return failure
- deliver \Rightarrow no cycle, so continue

$s = \text{parking2}$

$\text{Frontier} \setminus S_g = \{\text{transit1}, \text{transit2}, \text{transit3}\}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver}),$
 $(\text{parking2}, \text{deliver})\}$



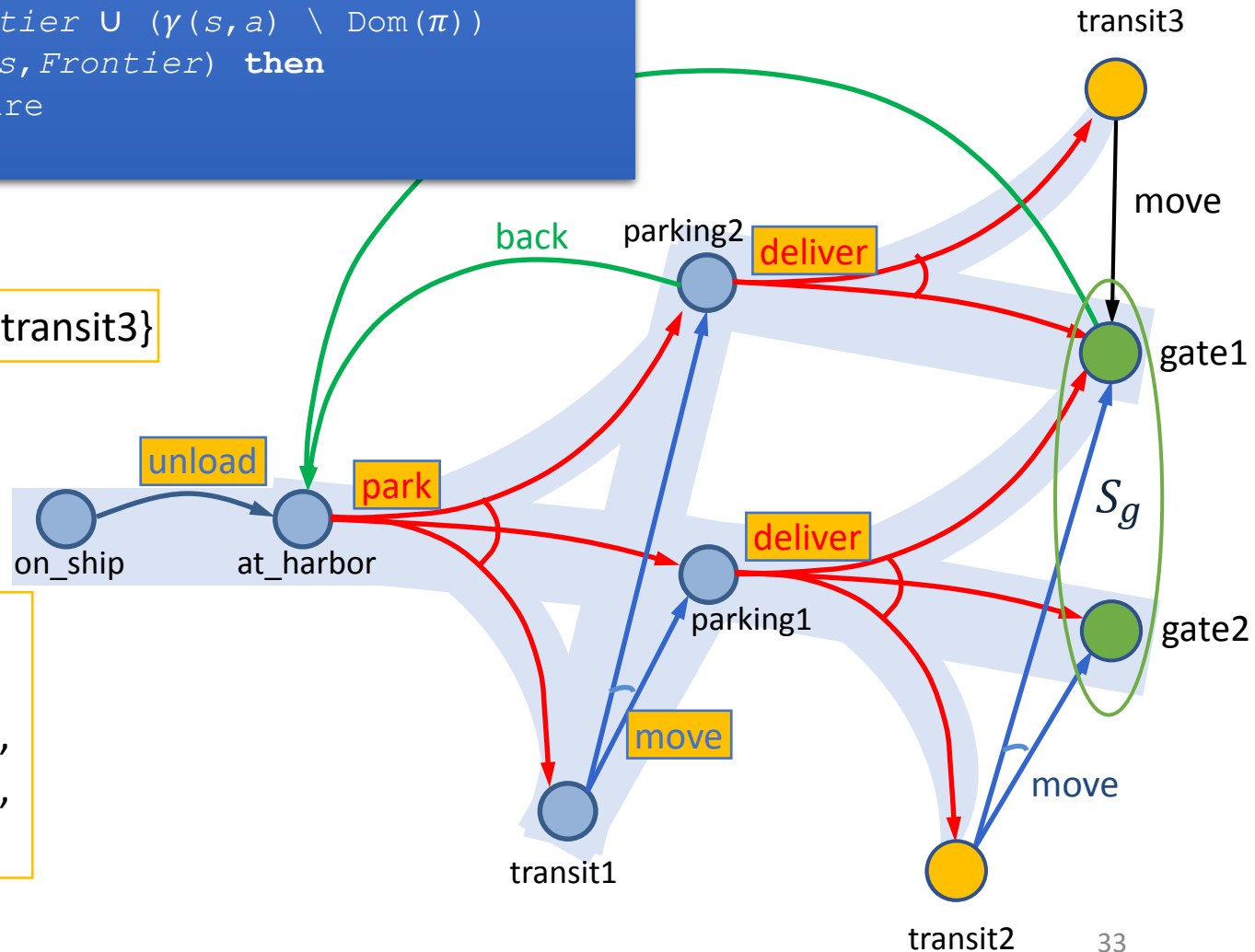
Find-Acyclic-Solution(Σ, s_0, S_g)

```
...
for every  $s \in \text{Frontier} \setminus S_g$  do
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }
...
nondeterministically choose  $a \in \text{Applicable}(s)$ 
 $\pi \leftarrow \pi \cup (s, a)$ 
Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )
if has-loops( $\pi, s, \text{Frontier}$ ) then
  return failure
return  $\pi$ 
```

$s = \text{transit1}$

$\text{Frontier} \setminus S_g = \{\text{transit2}, \text{transit3}\}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver}),$
 $(\text{parking2}, \text{deliver}),$
 $(\text{transit1}, \text{move})\}$



Example

Find-Acyclic-Solution(Σ, s_0, S_g)

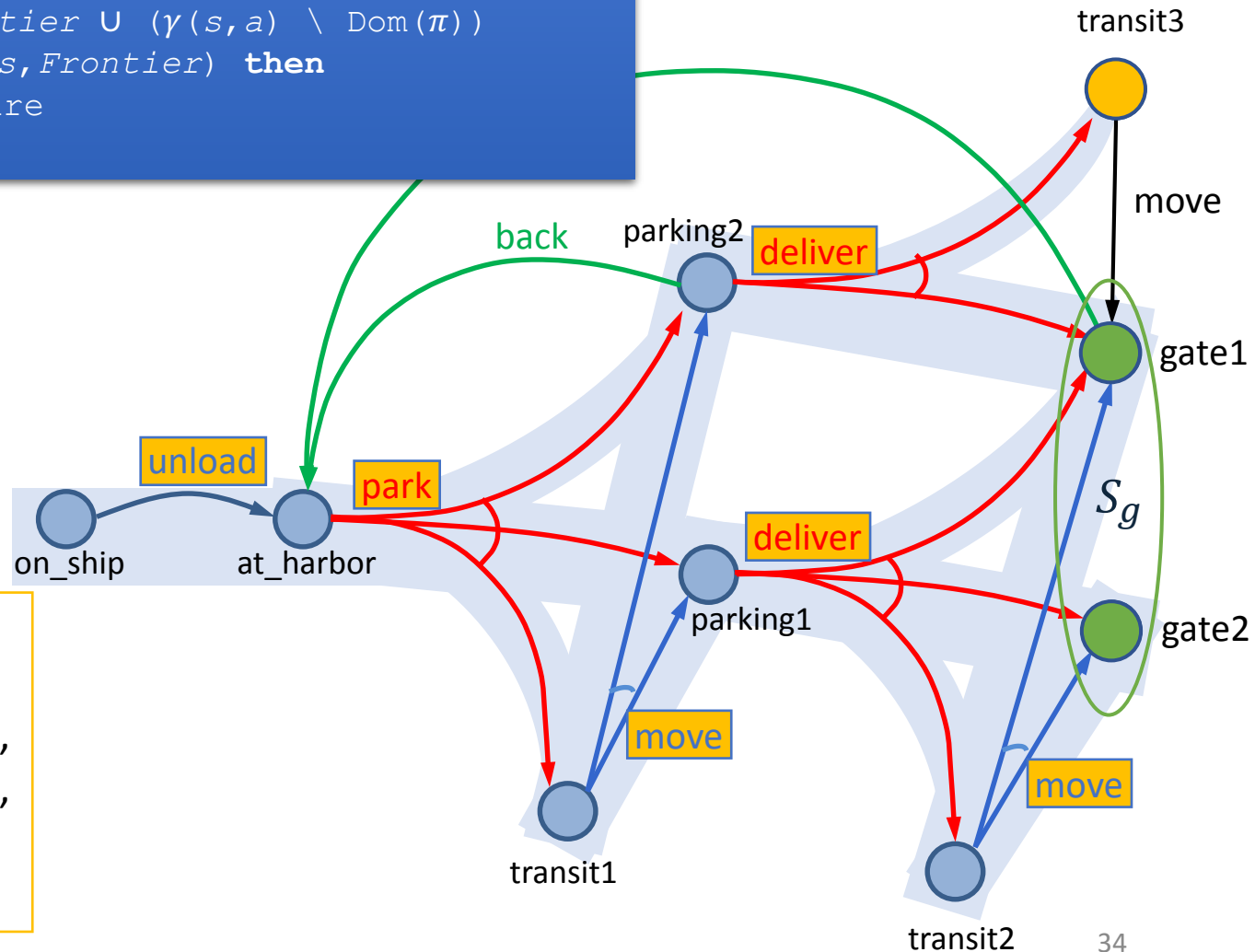
```
...  
for every  $s \in \text{Frontier} \setminus S_g$  do  
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }  
  ...  
  nondeterministically choose  $a \in \text{Applicable}(s)$   
   $\pi \leftarrow \pi \cup (s, a)$   
  Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )  
  if has-loops( $\pi, s, \text{Frontier}$ ) then  
    return failure  
return  $\pi$ 
```

$s = \text{transit2}$

$\text{Frontier} \setminus S_g = \{\text{transit3}\}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver}),$
 $(\text{parking2}, \text{deliver}),$
 $(\text{transit1}, \text{move}),$
 $(\text{transit2}, \text{move})\}$

Example



Find-Acyclic-Solution(Σ, s_0, S_g)

```
...
for every  $s \in \text{Frontier} \setminus S_g$  do
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }
...
nondeterministically choose  $a \in \text{Applicable}(s)$ 
 $\pi \leftarrow \pi \cup (s, a)$ 
Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )
if has-loops( $\pi, s, \text{Frontier}$ ) then
  return failure
return  $\pi$ 
```

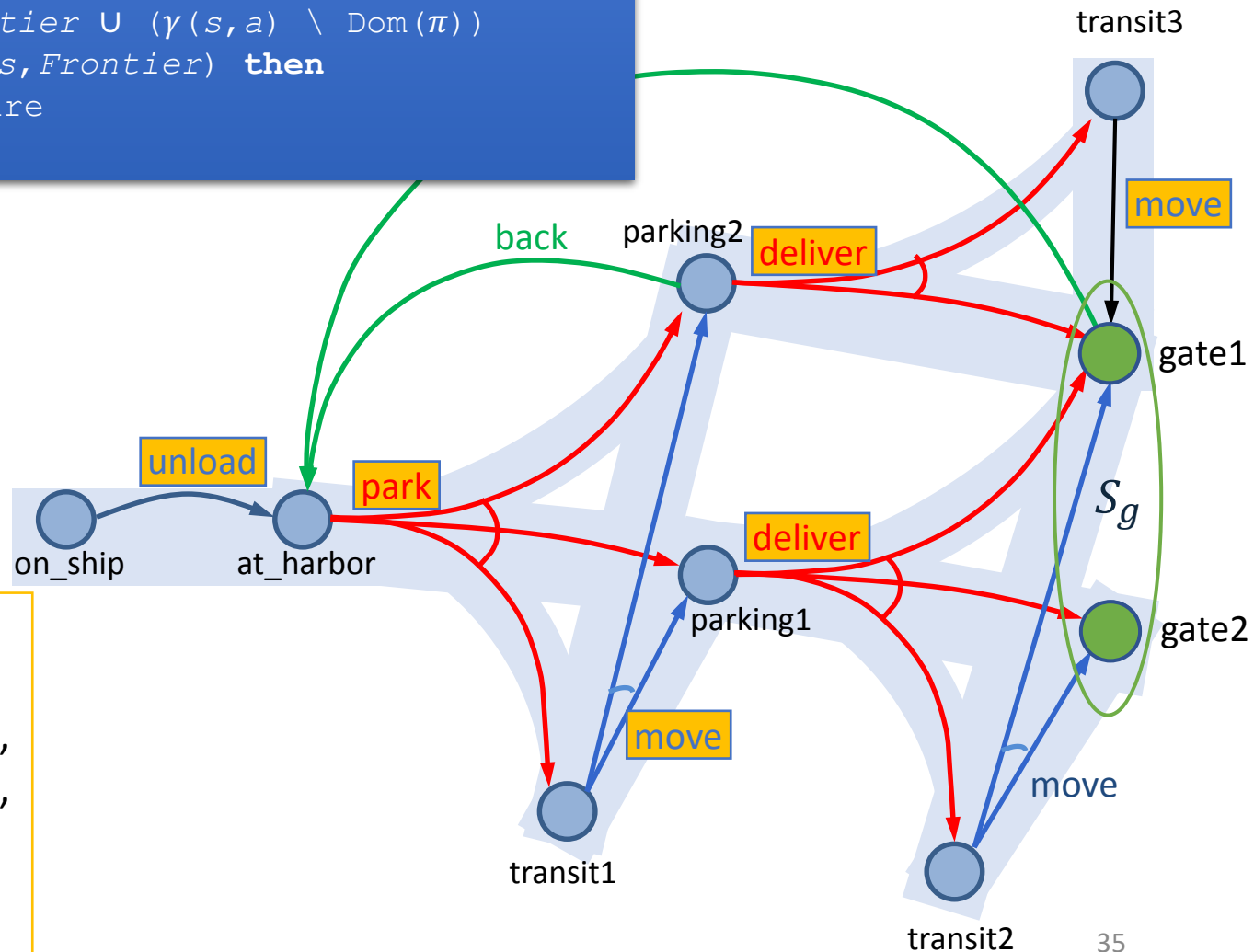
$s = \text{transit3}$

$\text{Frontier} \setminus S_g = \emptyset$

Found a solution,
so return π

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver}),$
 $(\text{parking2}, \text{deliver}),$
 $(\text{transit1}, \text{move}),$
 $(\text{transit2}, \text{move}),$
 $(\text{transit3}, \text{move})\}$

Example



Finding Safe Solutions

```
Find-Safe-Solution( $\Sigma, s_0, S_g$ )
```

```
 $\pi \leftarrow \emptyset$ 
```

```
Frontier  $\leftarrow \{s_0\}$ 
```

```
for every  $s \in \text{Frontier} \setminus S_g$  do
```

```
  Frontier  $\leftarrow \text{Frontier} \setminus \{s\}$ 
```

```
  if  $\text{Applicable}(s) = \emptyset$  then
```

```
    return failure
```

```
  nondeterministically choose  $a \in \text{Applicable}(s)$ 
```

```
   $\pi \leftarrow \pi \cup (s, a)$ 
```

```
  Frontier  $\leftarrow \text{Frontier} \cup (\gamma(s, a) \setminus \text{Dom}(\pi))$ 
```

```
  if  $\text{has-unsafe-loops}(\pi, s, \text{Frontier})$  then
```

```
    return failure
```

```
return  $\pi$ 
```

Different cycle-checking

- Same as Find-Acyclic-Solution except for cycle-checking
- has-unsafe-loops instead of has-loops
- Check if π contains any cycles that cannot be escaped:
 - For each $s' \in (\gamma(s, a) \cap \text{Dom}(\pi))$
 - Is $\hat{\gamma}(s', \pi) \cap \text{Frontier} = \emptyset$?
 - Formally, $\text{has-unsafe-loops}(\pi, s, \text{Frontier})$ iff
$$\exists s' \in (\gamma(s, a) \cap \text{Dom}(\pi)) : \hat{\gamma}(s', \pi) \cap \text{Frontier} = \emptyset$$

Find-Safe-Solution (Σ, s_0, S_g)

$\pi \leftarrow \emptyset$

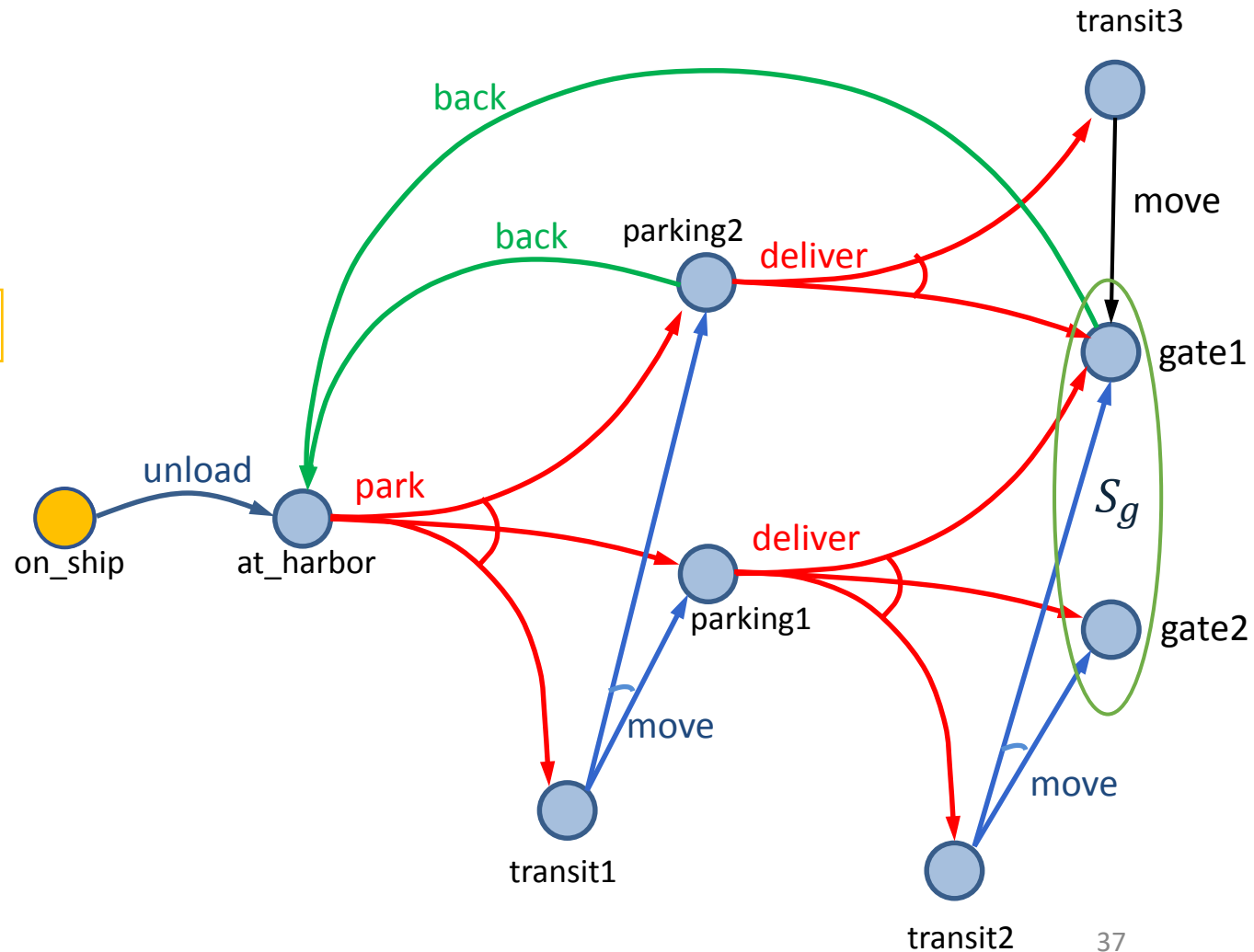
Frontier $\leftarrow \{s_0\}$

...

Example

Frontier $\setminus S_g = \{\text{on_ship}\}$

$\pi = \{\}$



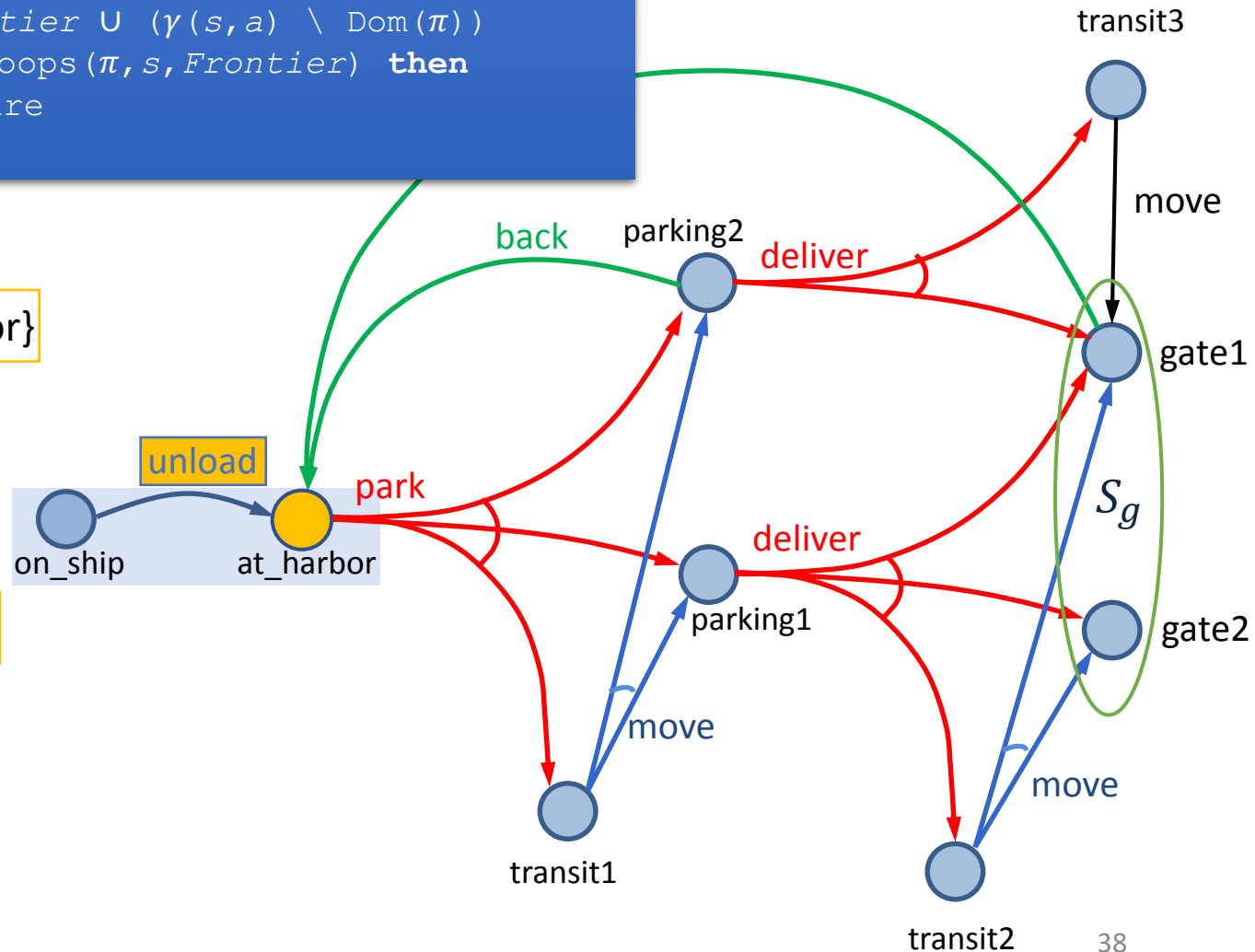
Find-Safe-Solution (Σ, s_0, S_g)

```
...  
for every  $s \in \text{Frontier} \setminus S_g$  do  
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }  
  ...  
  nondeterministically choose  $a \in \text{Applicable}(s)$   
   $\pi \leftarrow \pi \cup (s, a)$   
  Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )  
  if has-unsafe-loops( $\pi, s, \text{Frontier}$ ) then  
    return failure  
return  $\pi$ 
```

$s = \text{on_ship}$

$\text{Frontier} \setminus S_g = \{\text{at_harbor}\}$

$\pi = \{(\text{on_ship}, \text{unload})\}$



Example

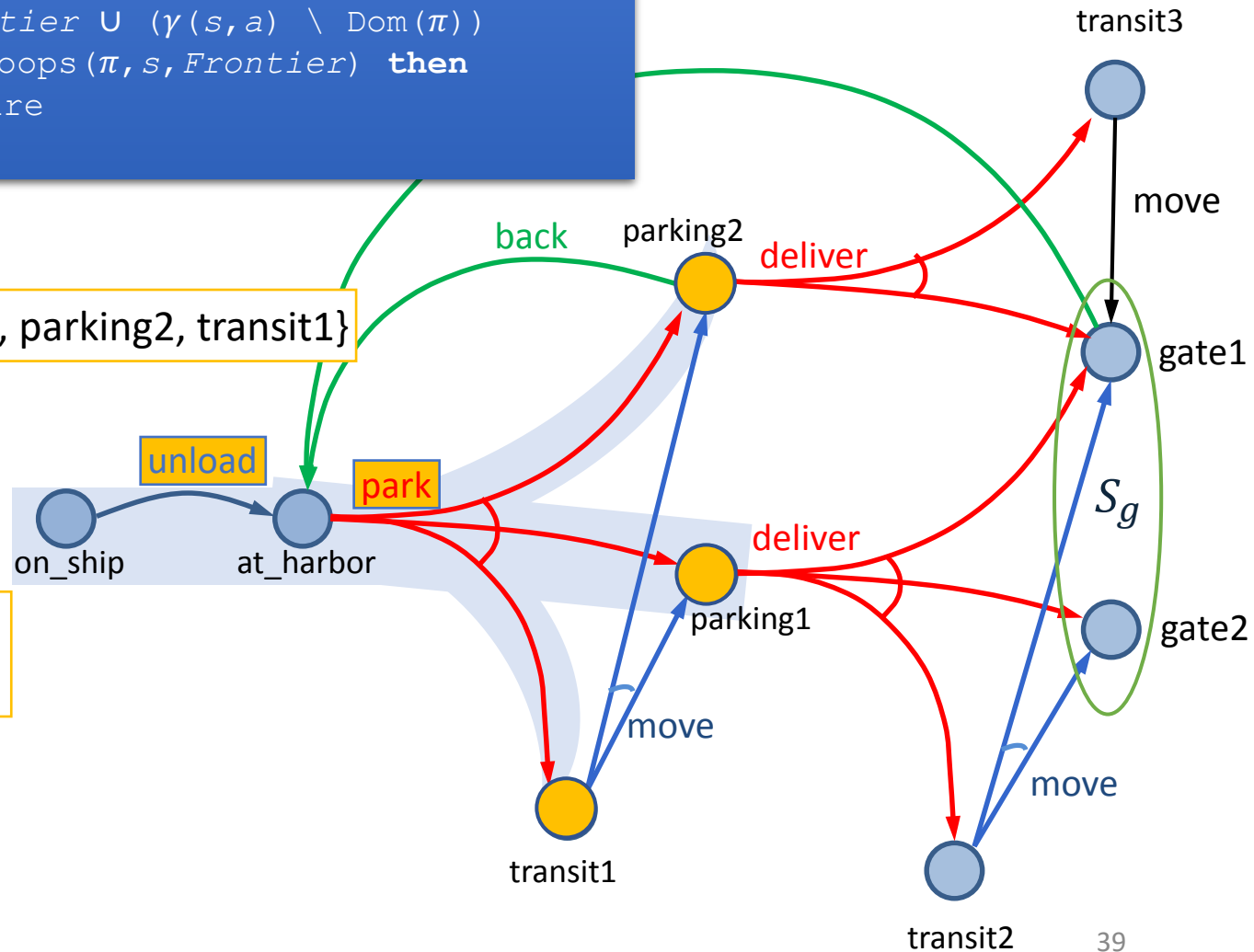
Find-Safe-Solution (Σ, s_0, S_g)

```
...  
for every  $s \in \text{Frontier} \setminus S_g$  do  
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }  
  ...  
  nondeterministically choose  $a \in \text{Applicable}(s)$   
   $\pi \leftarrow \pi \cup (s, a)$   
  Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )  
  if has-unsafe-loops( $\pi, s, \text{Frontier}$ ) then  
    return failure  
return  $\pi$ 
```

$s = \text{at_harbor}$

$\text{Frontier} \setminus S_g = \{\text{parking1}, \text{parking2}, \text{transit1}\}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park})\}$



Example

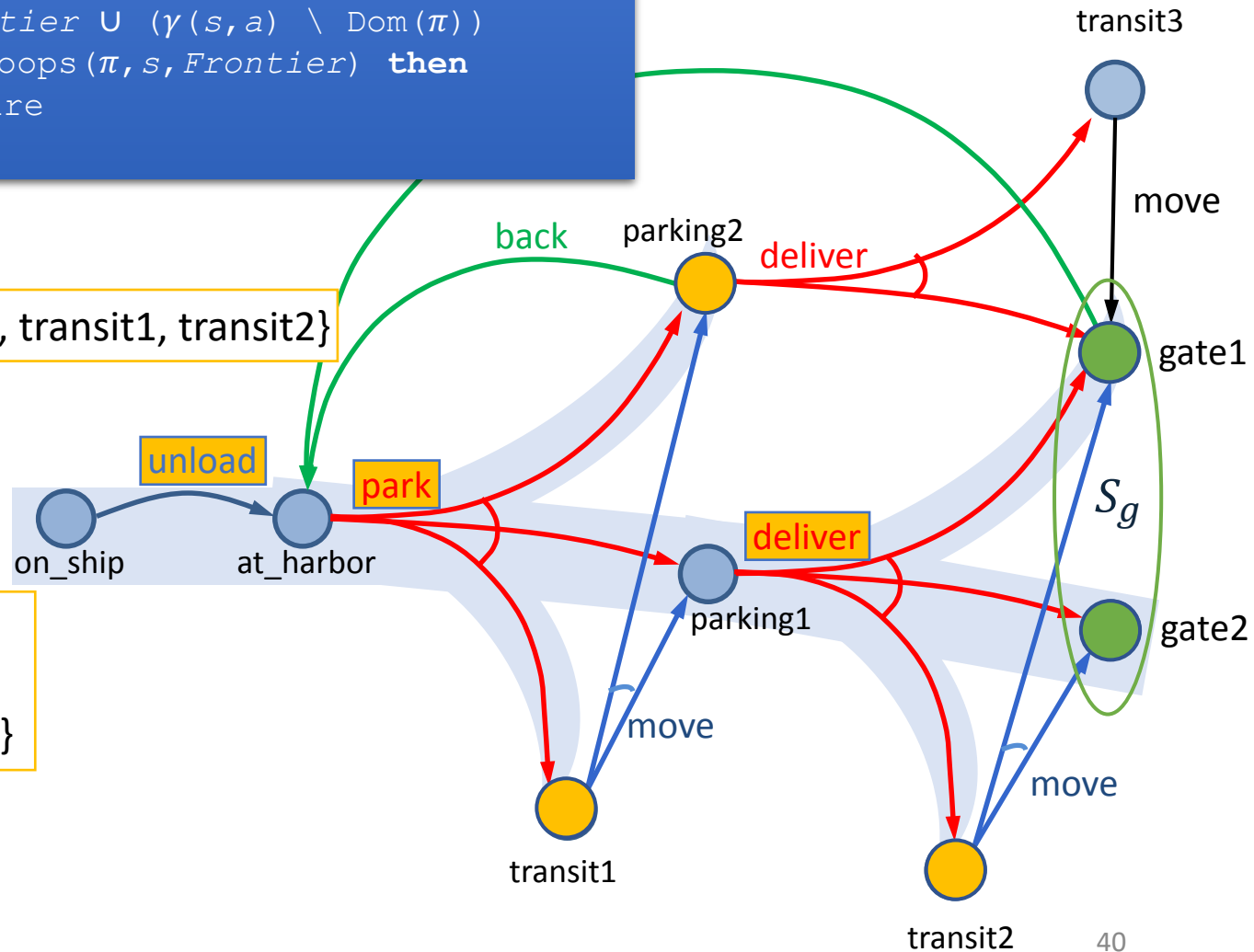
Find-Safe-Solution (Σ, s_0, S_g)

```
...  
for every  $s \in \text{Frontier} \setminus S_g$  do  
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }  
  ...  
  nondeterministically choose  $a \in \text{Applicable}(s)$   
   $\pi \leftarrow \pi \cup (s, a)$   
  Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )  
  if has-unsafe-loops( $\pi, s, \text{Frontier}$ ) then  
    return failure  
return  $\pi$ 
```

$s = \text{parking1}$

$\text{Frontier} \setminus S_g = \{\text{parking2}, \text{transit1}, \text{transit2}\}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver})\}$



Example

Find-Safe-Solution (Σ, s_0, S_g)

```
...  
for every  $s \in \text{Frontier} \setminus S_g$  do  
  Frontier  $\leftarrow$  Frontier  $\setminus \{s\}$   
  ...  
  nondeterministically choose  $a \in \text{Appl}$   
   $\pi \leftarrow \pi \cup (s, a)$   
  Frontier  $\leftarrow$  Frontier  $\cup (\gamma(s, a) \setminus \text{Dom}(\pi))$   
  if has-unsafe-loops( $\pi, s, \text{Frontier}$ ) then  
    return failure  
return  $\pi$ 
```

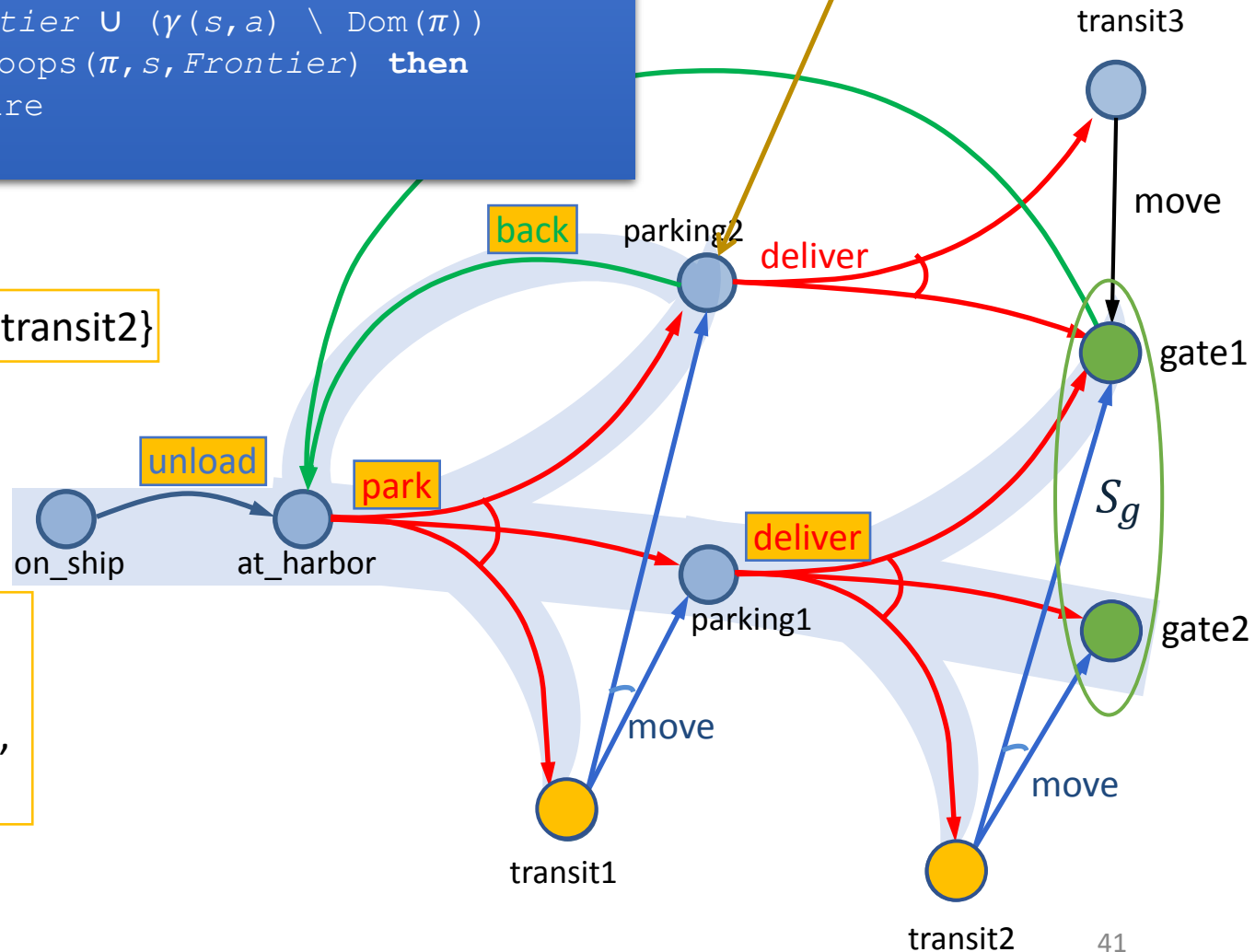
Example

nondeterministically choose back or deliver
• back is okay: escapable cycle

$s = \text{parking2}$

$\text{Frontier} \setminus S_g = \{\text{transit1}, \text{transit2}\}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver}),$
 $(\text{parking2}, \text{back})\}$



Find-Safe-Solution (Σ, s_0, S_g)

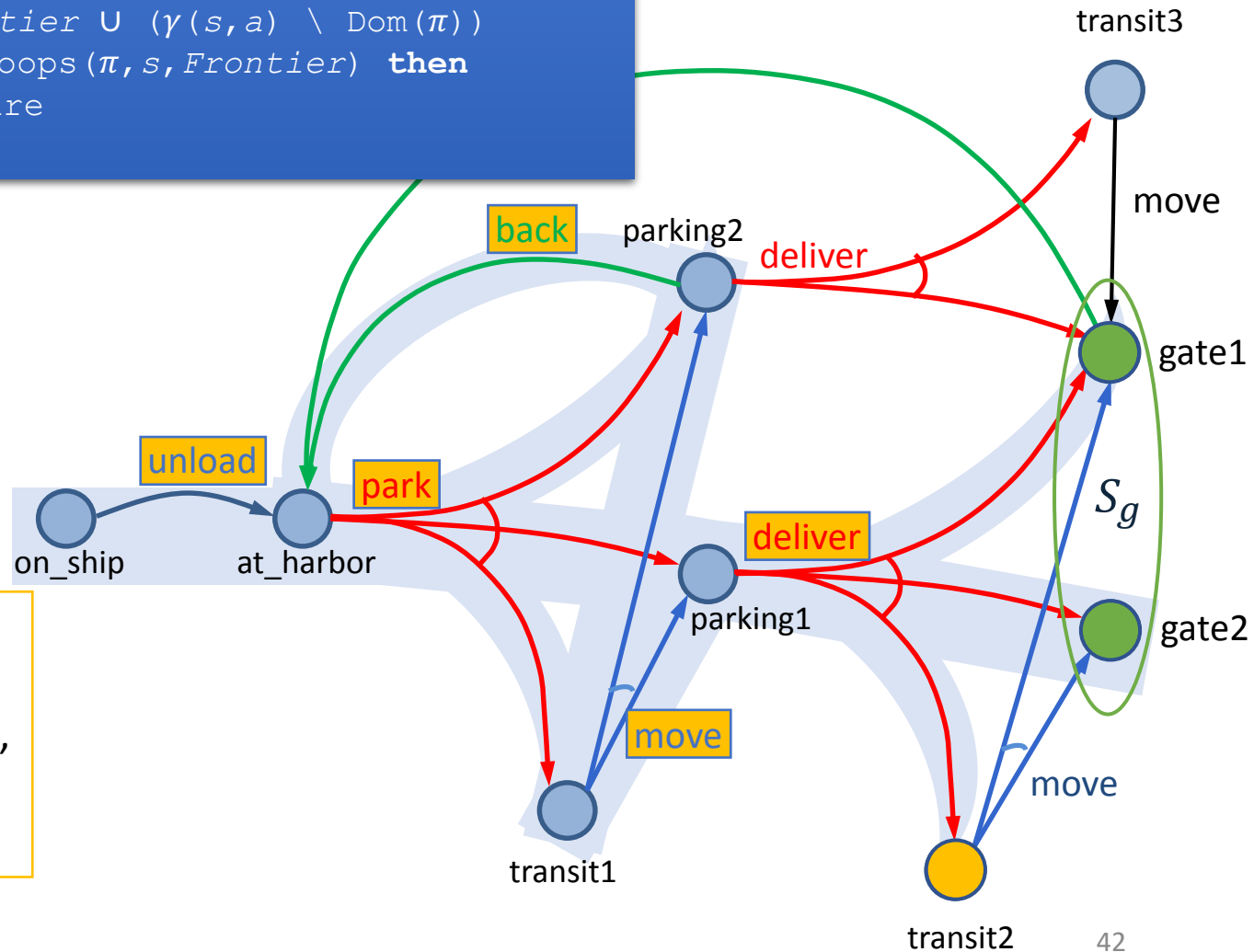
```
...  
for every  $s \in \text{Frontier} \setminus S_g$  do  
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }  
  ...  
  nondeterministically choose  $a \in \text{Applicable}(s)$   
   $\pi \leftarrow \pi \cup (s, a)$   
  Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )  
  if has-unsafe-loops( $\pi, s, \text{Frontier}$ ) then  
    return failure  
return  $\pi$ 
```

$s = \text{transit1}$

$\text{Frontier} \setminus S_g = \{\text{transit2}\}$

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver}),$
 $(\text{parking2}, \text{back}),$
 $(\text{transit1}, \text{move})\}$

Example



Find-Safe-Solution (Σ, s_0, S_g)

```
...  
for every  $s \in \text{Frontier} \setminus S_g$  do  
  Frontier  $\leftarrow$  Frontier  $\setminus$  { $s$ }  
  ...  
  nondeterministically choose  $a \in \text{Applicable}(s)$   
   $\pi \leftarrow \pi \cup (s, a)$   
  Frontier  $\leftarrow$  Frontier  $\cup$  ( $\gamma(s, a) \setminus \text{Dom}(\pi)$ )  
  if has-unsafe-loops( $\pi, s, \text{Frontier}$ ) then  
    return failure  
return  $\pi$ 
```

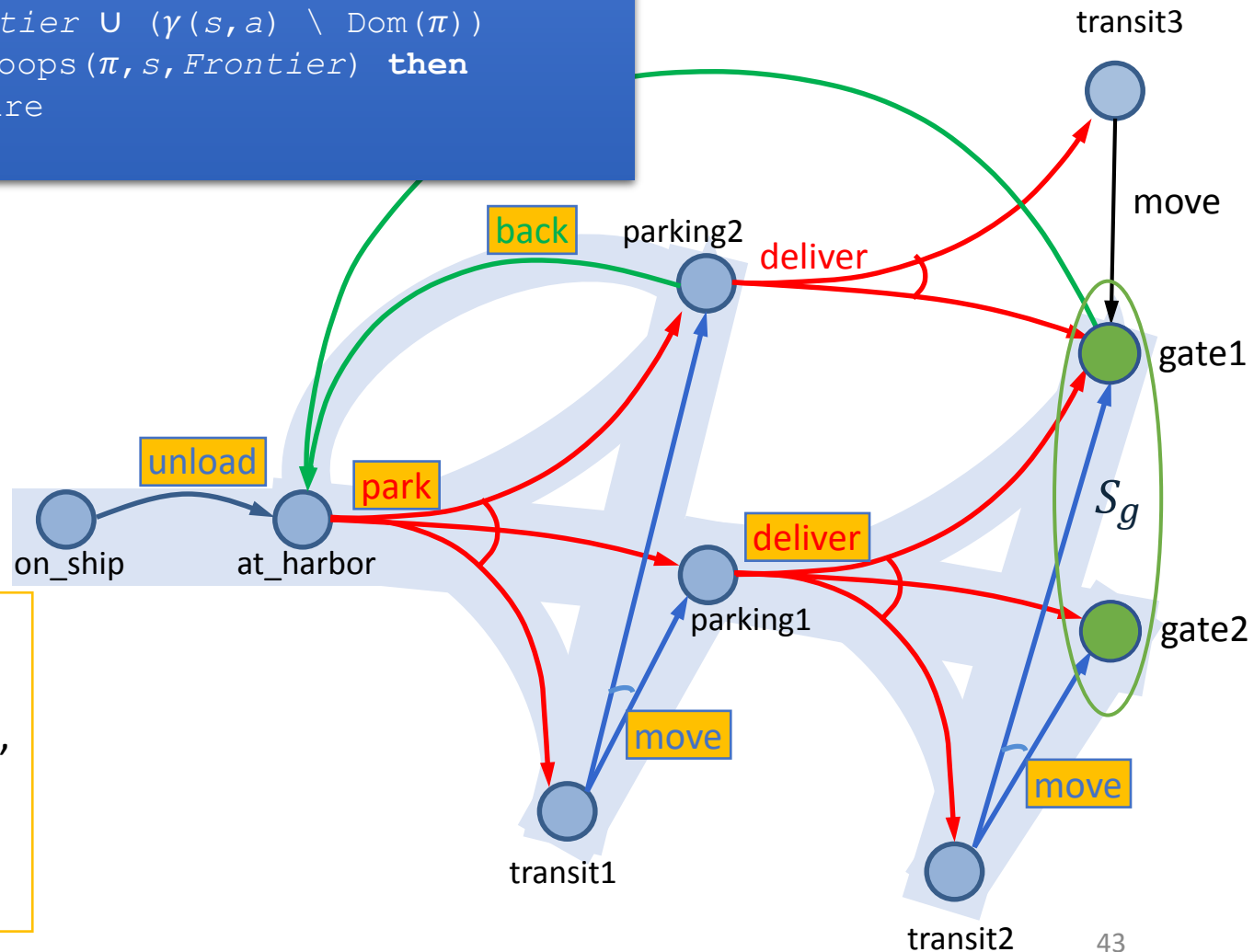
$s = \text{transit2}$

$\text{Frontier} \setminus S_g = \emptyset$

Found a solution,
so return π

$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver}),$
 $(\text{parking2}, \text{back}),$
 $(\text{transit1}, \text{move}),$
 $(\text{transit2}, \text{move})\}$

Example



Intermediate Summary

- And/Or Graph Search
 - Algorithms for each type of solution
 - unsafe, cyclic safe, acyclic safe

Outline per the Book

5.2 Planning Problem

- Planning domains
- Plans as policies
- Planning problems and solutions

5.3 And/Or Graph Search

- Planning by forward search

5.5 Determinisation Techniques

- Guided planning for safe solutions
- Planning for safe solutions by determinisation

5.6 Online Approaches

- Lookahead
- Lookahead by Determinisation
- Lookahead with a bounded number of steps

Guided-Find-Safe-Solution

- Motivation:
 - Much easier to find solutions if they don't have to be safe
 - Find-Safe-Solution needs plans for all possible outcomes of actions
 - Find-Solution only needs a plan for one of them
- Idea:
 - loop
 - Find a solution π
 - Look at each leaf node of π
 - If the leaf node is not a goal, find a solution and incorporate it into π

Guided-Find-Safe-Solution

Guided-Find-Safe-Solution (Σ, s_0, S_g)

if $s_0 \in S_g$ then

return \emptyset

if $\text{Applicable}(s_0) = \emptyset$ then

return failure

$\pi \leftarrow \emptyset$

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$

return π

arbitrarily select $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ then

return failure ⇐ not in the book

else

for every s' and a s.t. $\gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

π is a solution. Return the part that is reachable from s_0 .

Choose any leaf s that is not a goal. Find a solution π' for s .

For each (s, a) in π' , add to π unless π already has an action at s .

s is unsolvable. For each (s', a) that can produce s , modify π and Σ so we will never use a at s'

Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ **then**

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ **then**

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ **then**

return failure

else

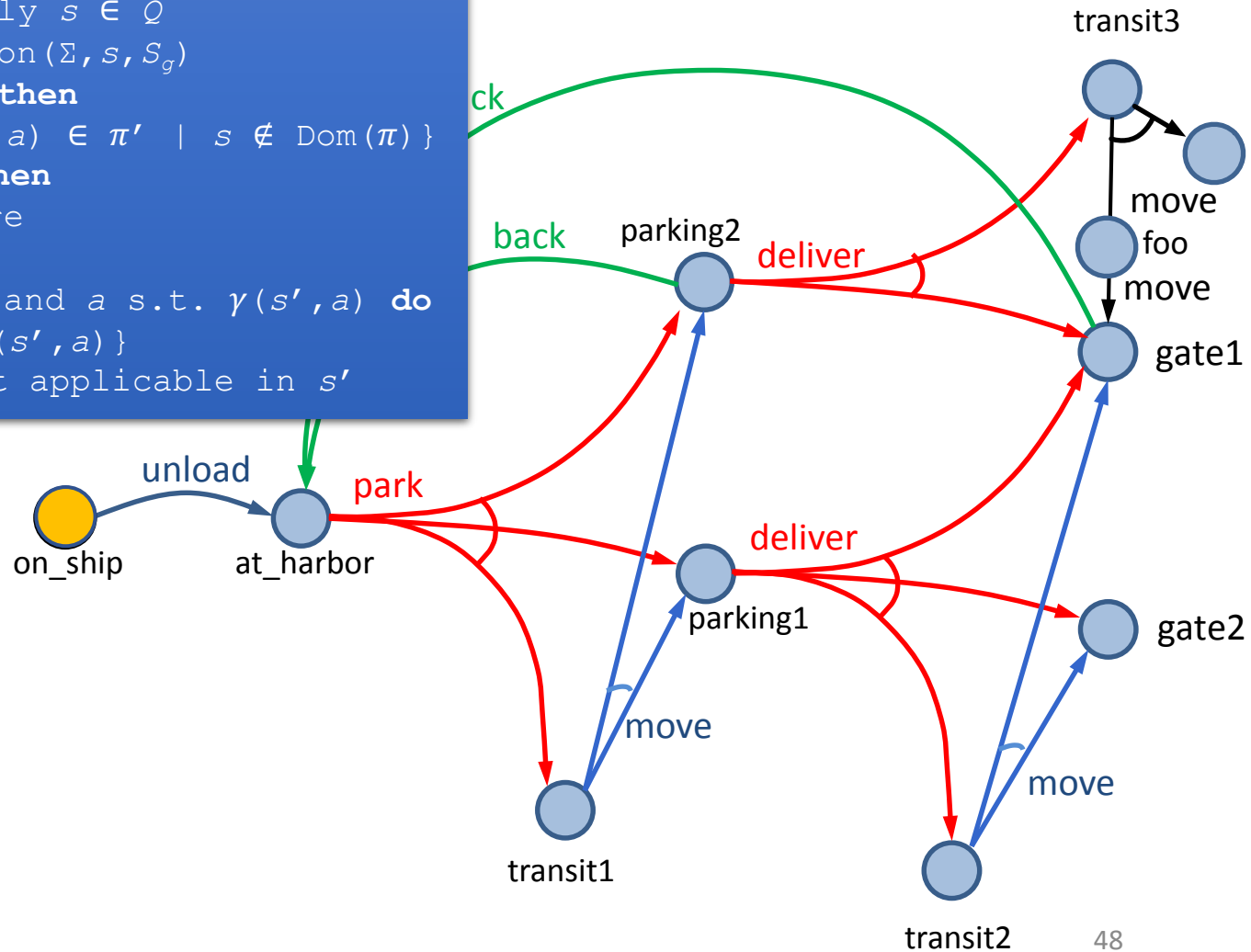
for every s' and a s.t. $\gamma(s', a)$ **do**

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

$s_0 = \text{on_ship}$

$\pi = \{\}$



Example

Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ **then**

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ **then**

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ **then**

return failure

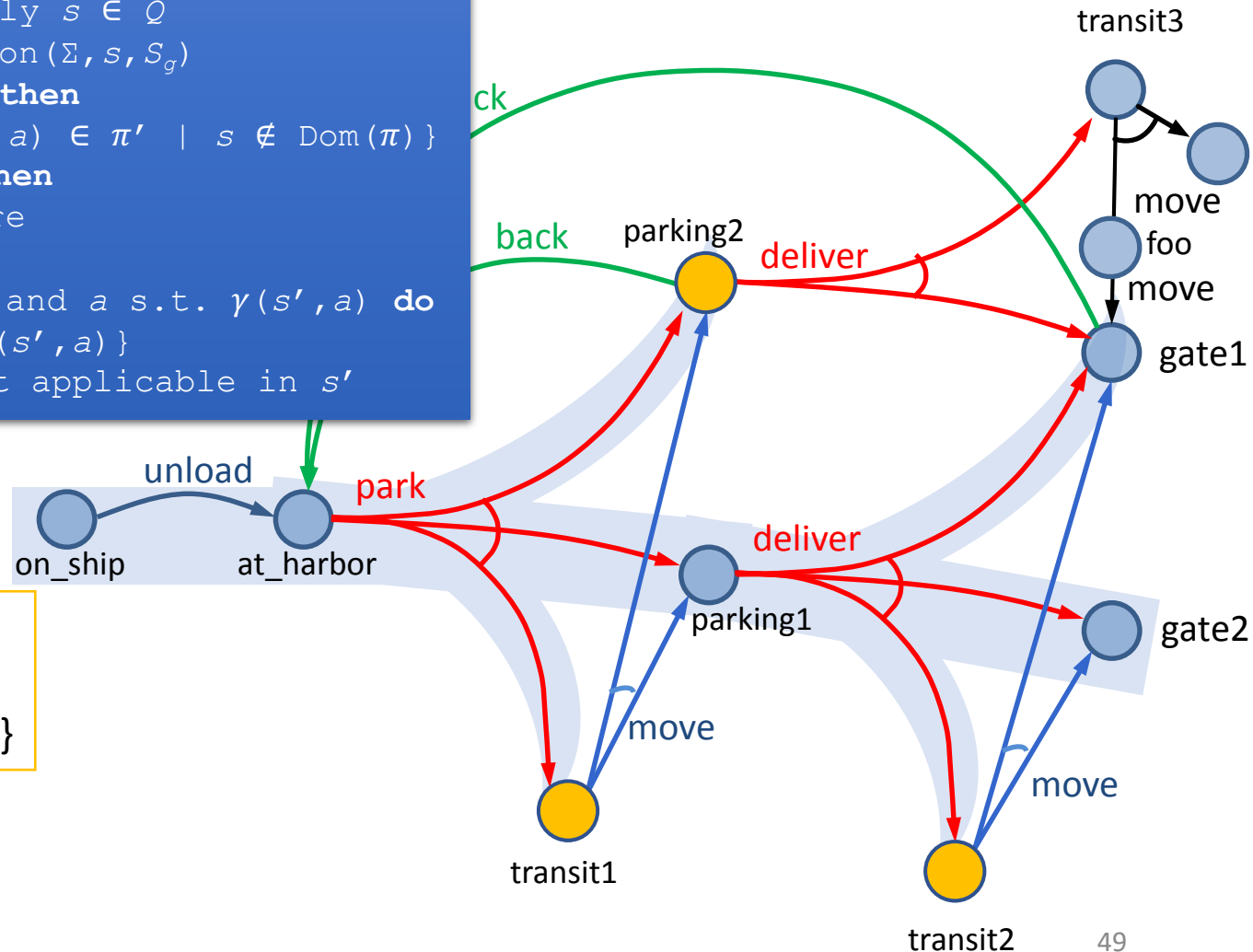
else

for every s' and a s.t. $\gamma(s', a)$ **do**

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ **then**

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ **then**

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ **then**

return failure

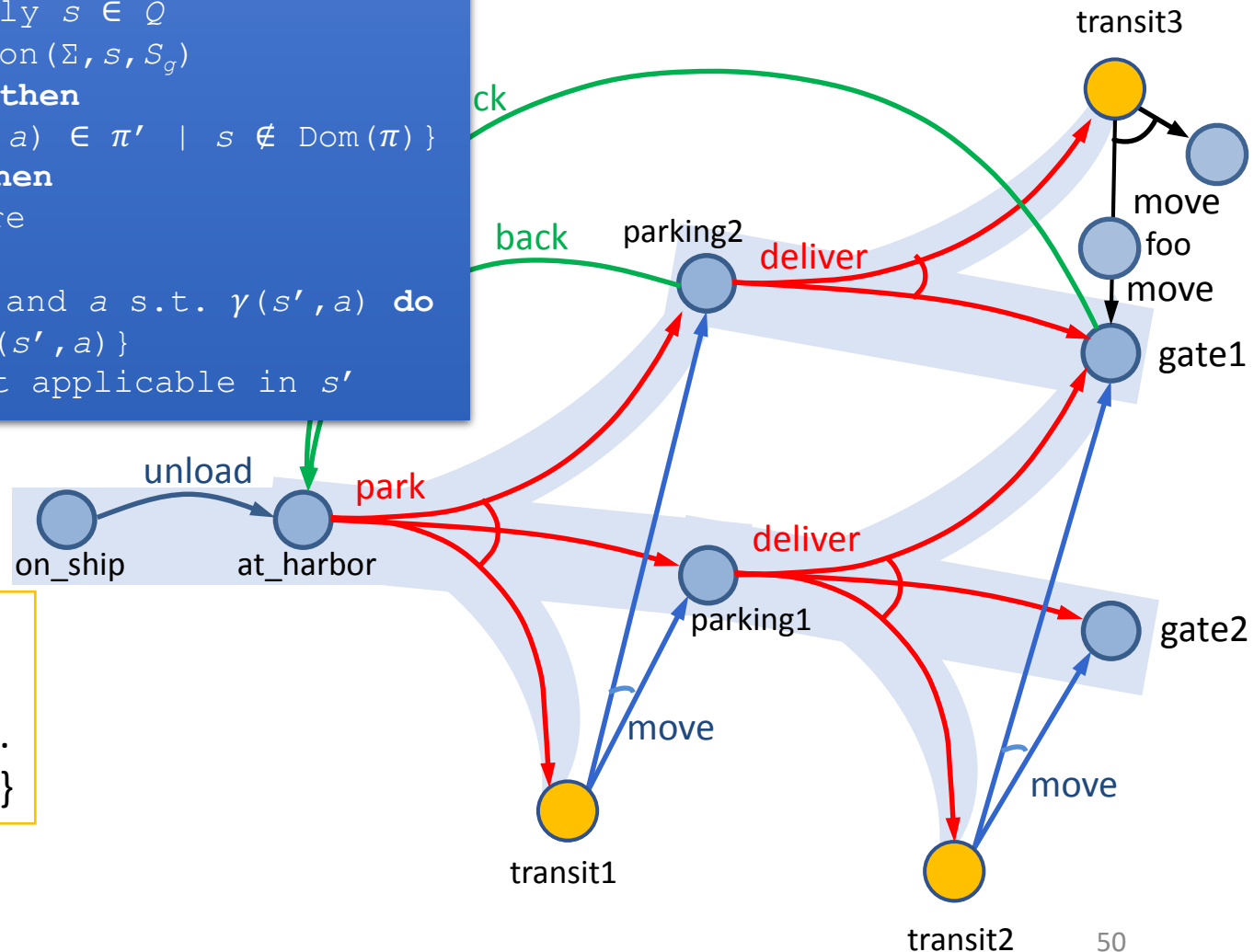
else

for every s' and a s.t. $\gamma(s', a)$ **do**

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ then

return failure

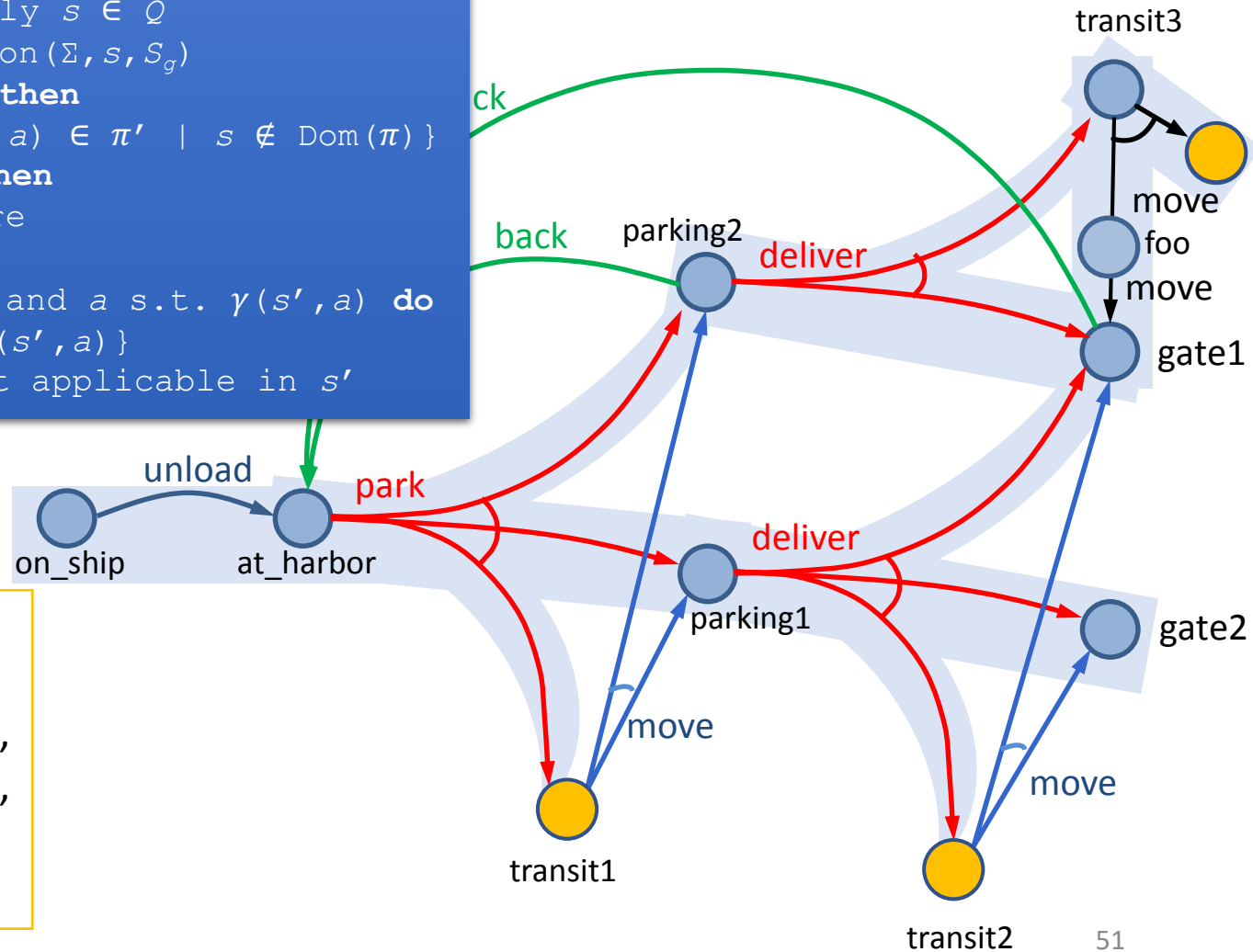
else

for every s' and a s.t. $\gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ then

return failure

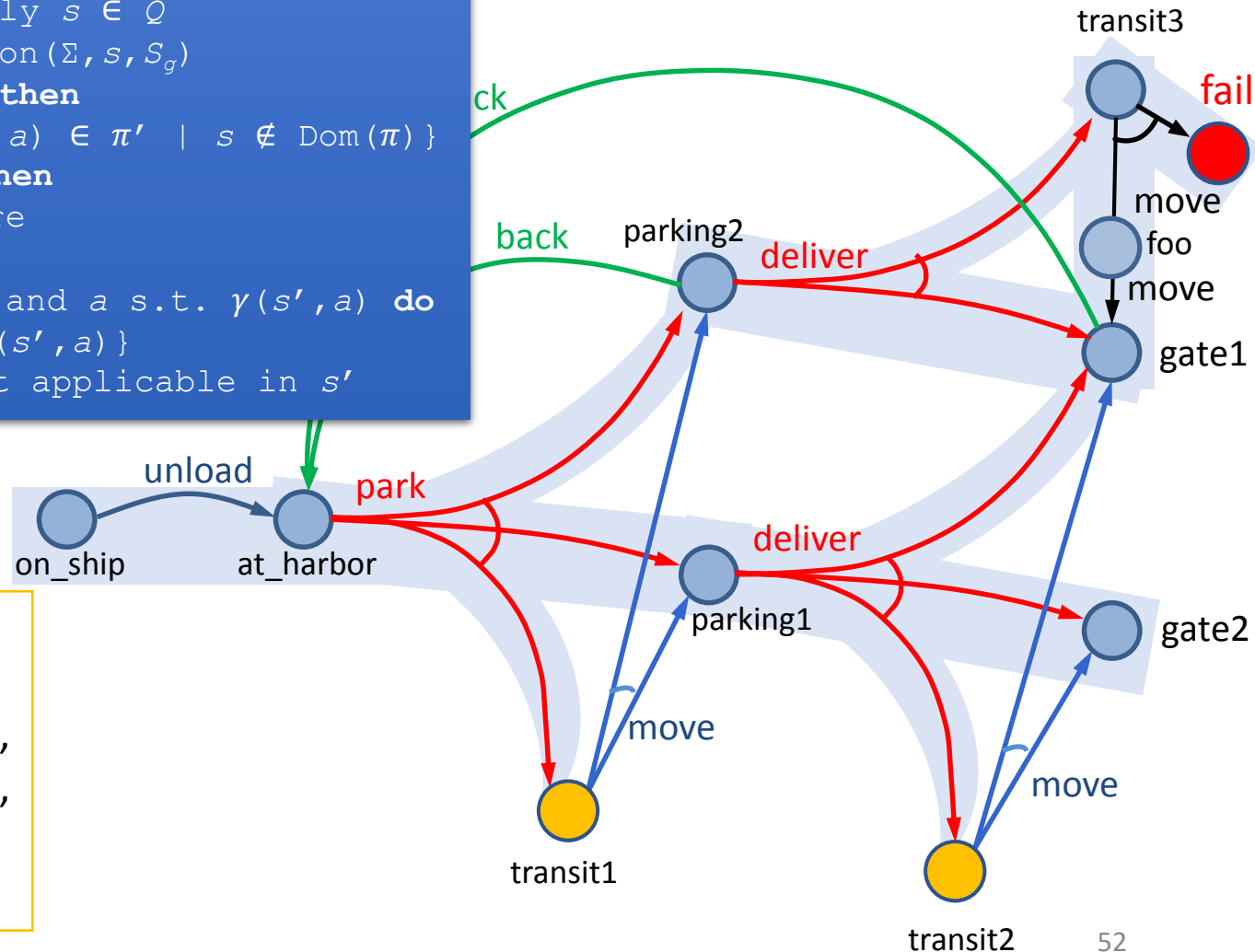
else

for every s' and a s.t. $\gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver}),$
 $(\text{parking2}, \text{deliver}),$
 $(\text{transit1}, \text{move}),$
 $(\text{foo}, \text{move})\}$

Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ then

return failure

else

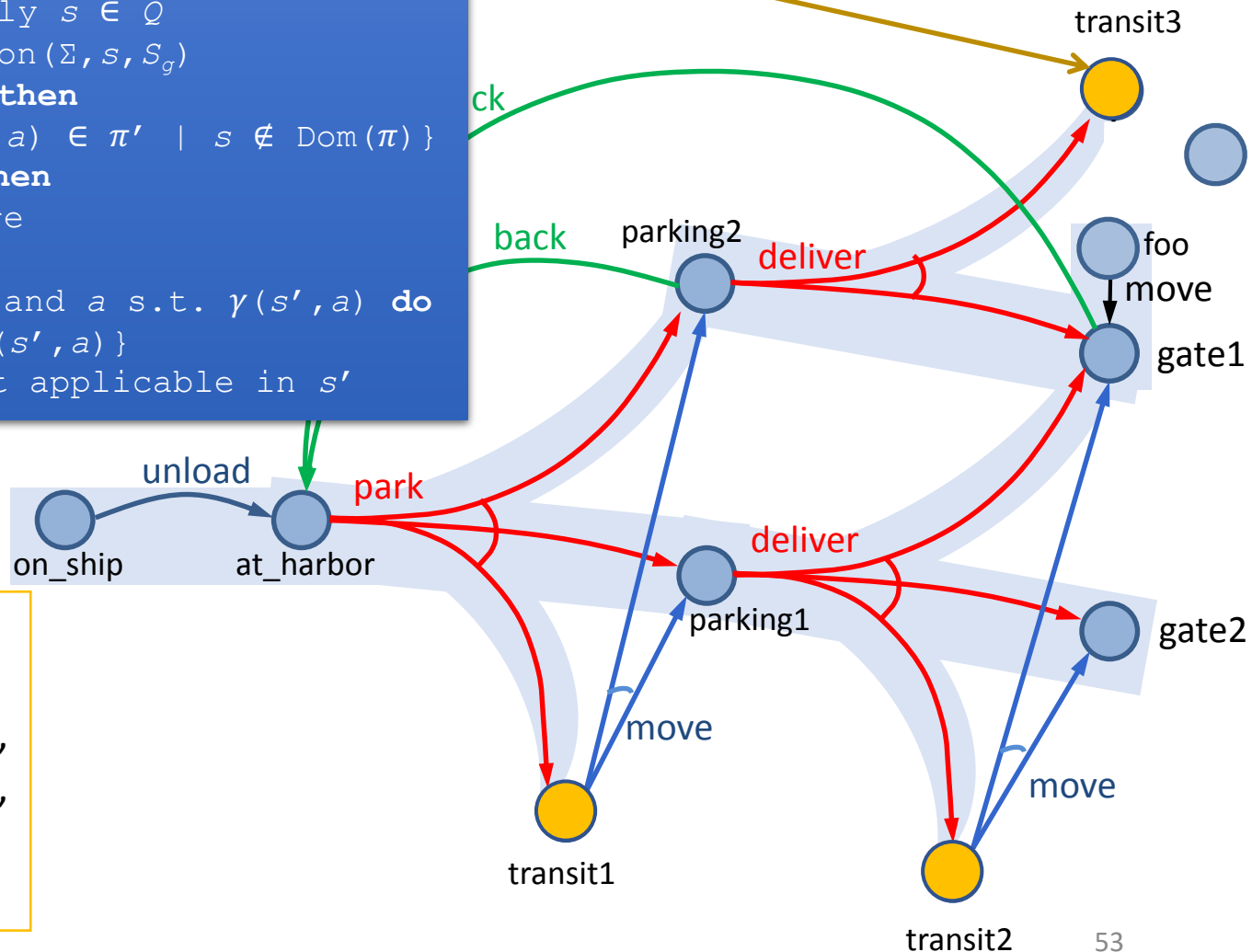
for every s' and a s.t. $\gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example

Modify Σ_d to make
move inapplicable



Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ then

return failure

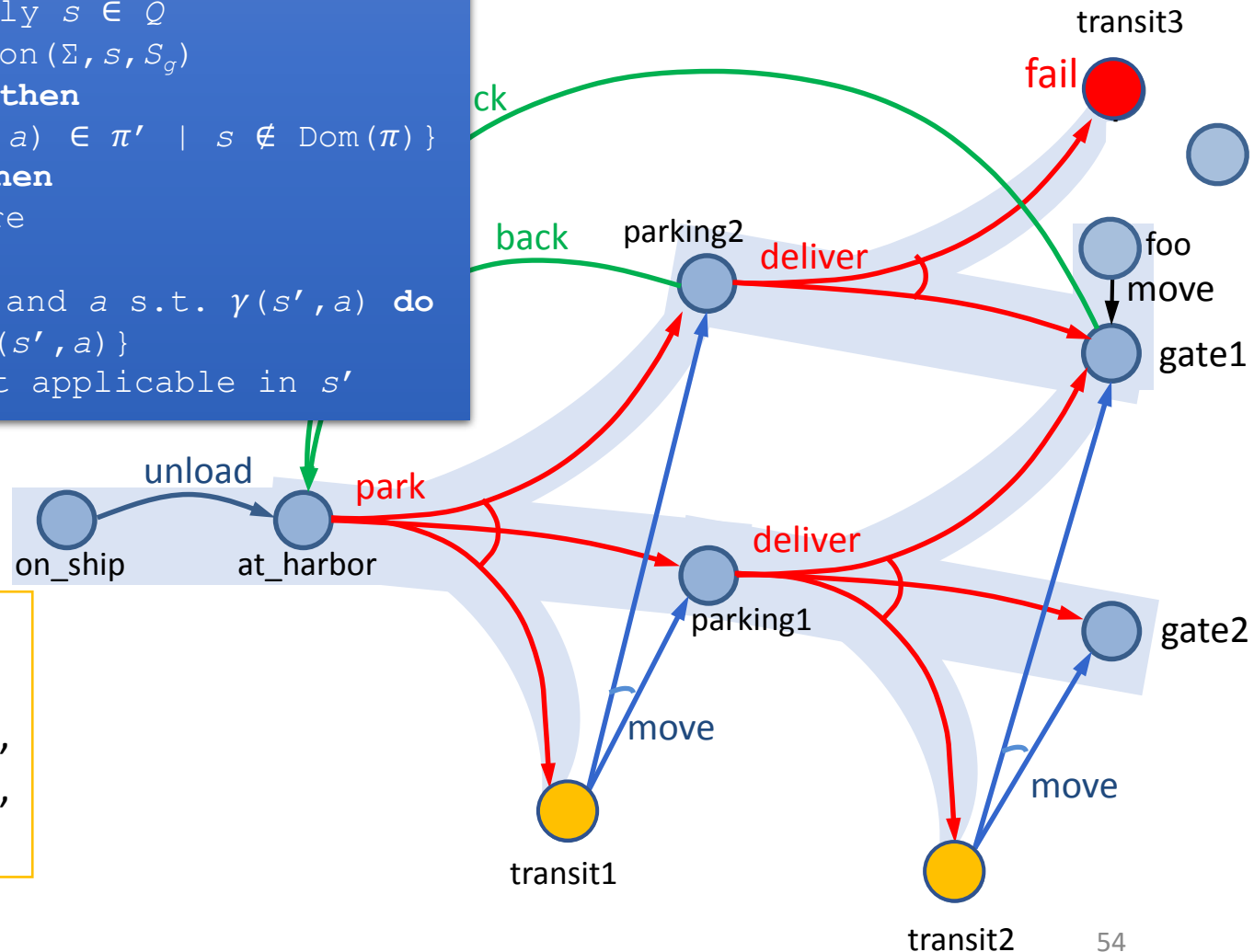
else

for every s' and a s.t. $\gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver}),$
 $(\text{parking2}, \text{deliver}),$
 $(\text{foo}, \text{move})\}$

Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ then

return failure

else

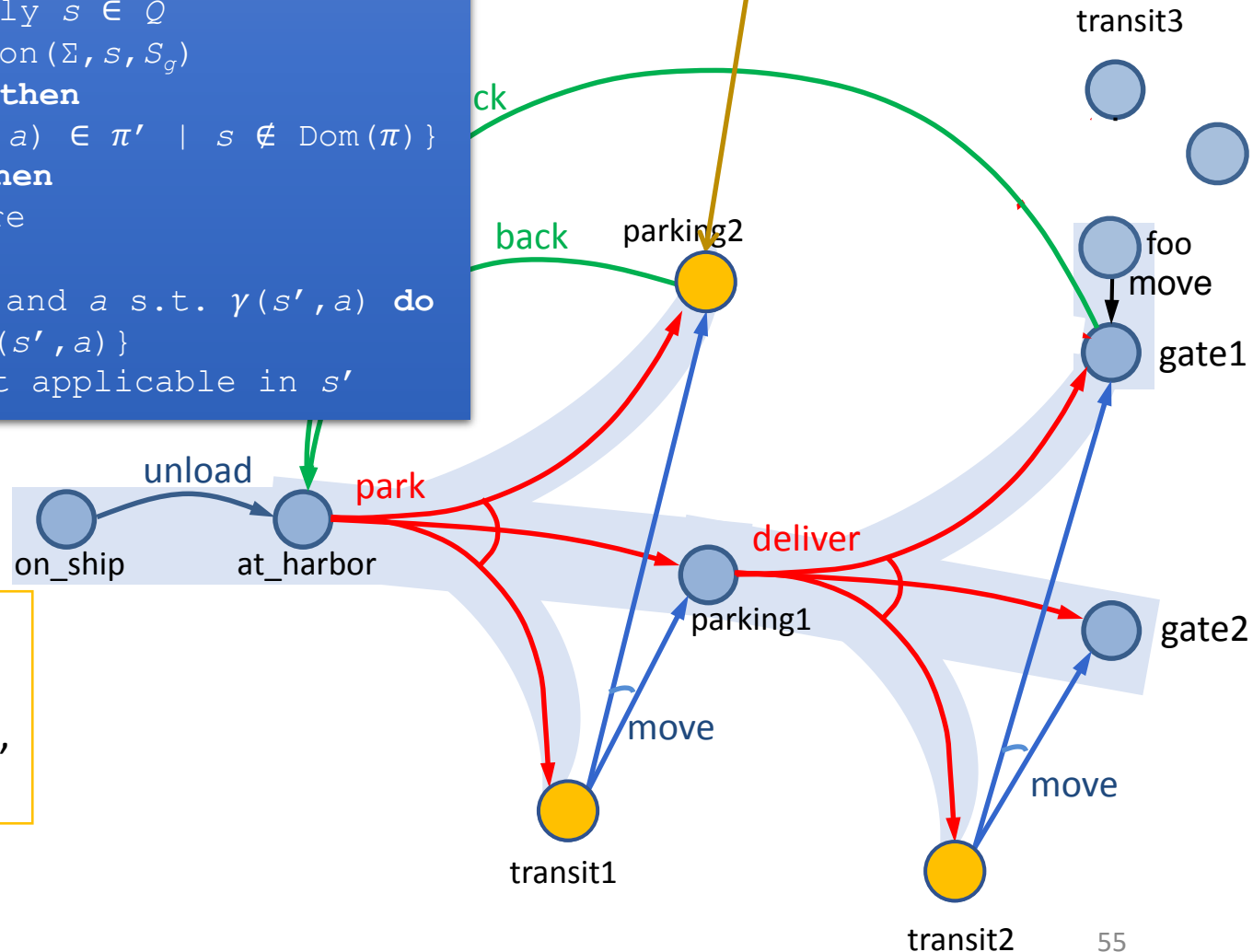
for every s' and a s.t. $\gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example

Modify Σ_d to make
move inapplicable



$\pi = \{(\text{on_ship}, \text{unload}),$
 $(\text{at_harbor}, \text{park}),$
 $(\text{parking1}, \text{deliver}),$
 $(\text{foo}, \text{move})\}$

Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ **then**

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ **then**

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ **then**

return failure

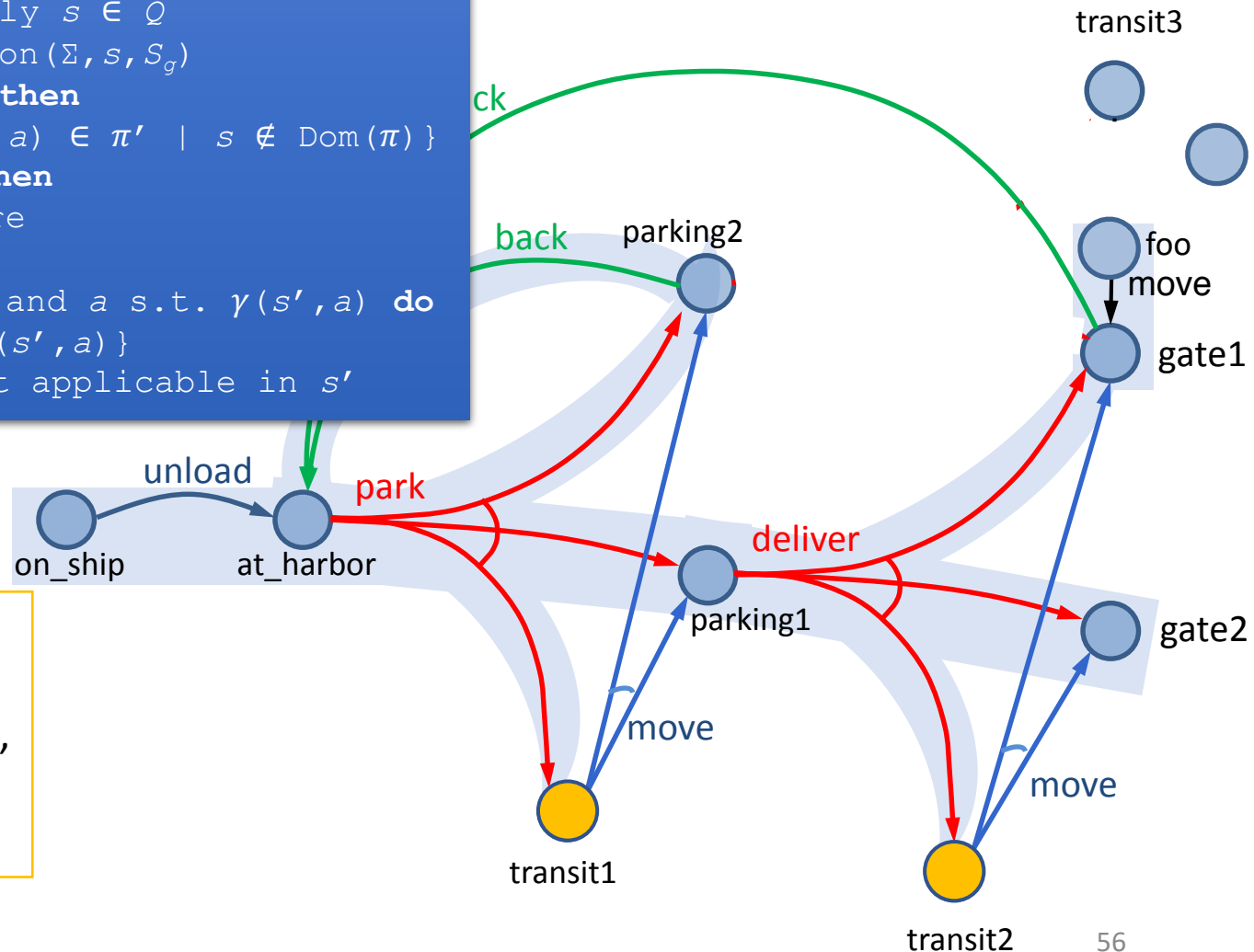
else

for every s' and a s.t. $\gamma(s', a)$ **do**

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ **then**

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\nu}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ **then**

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ **then**

return failure

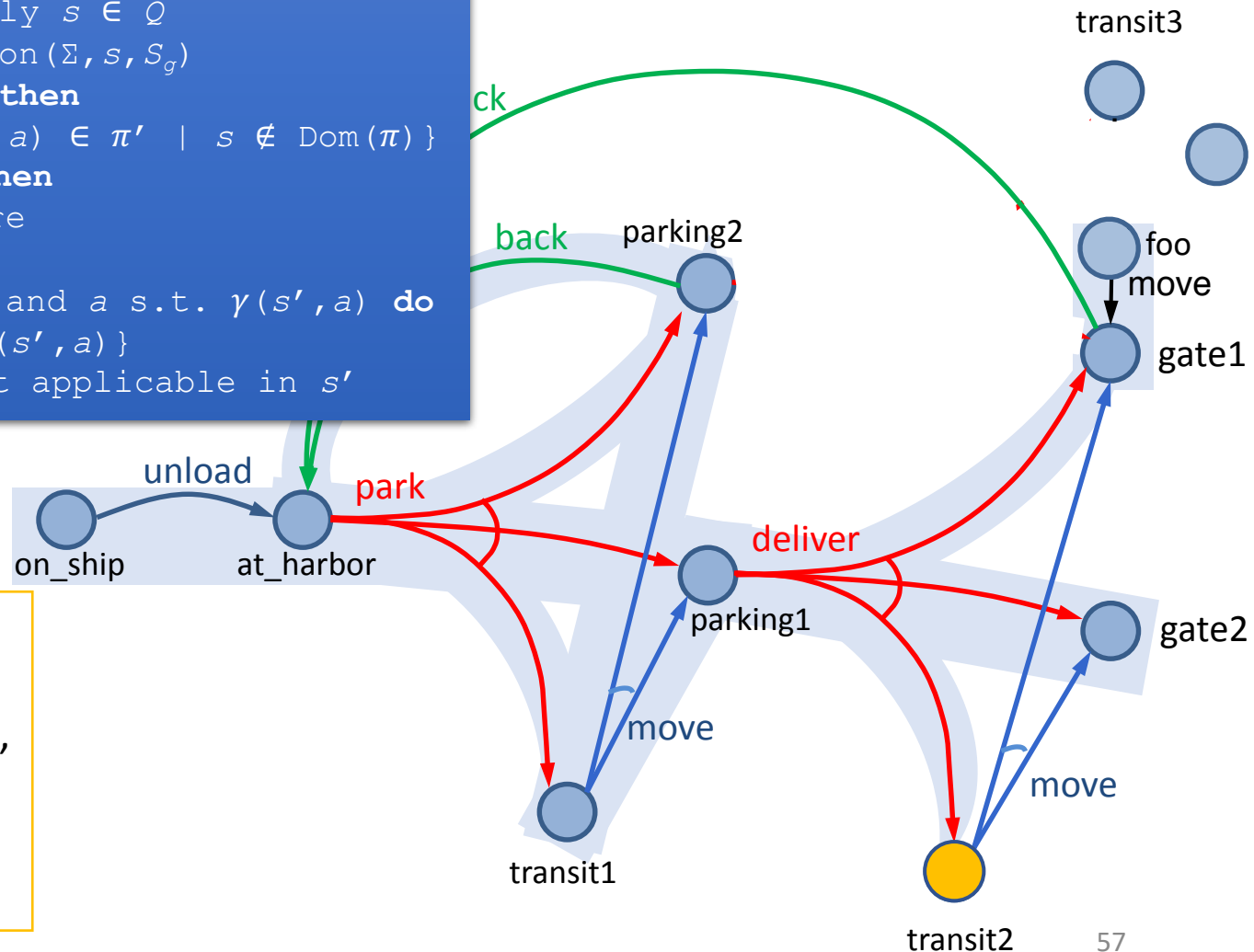
else

for every s' and a s.t. $\gamma(s', a)$ **do**

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example



Guided-Find-Safe-Solution (Σ, s_0, S_g)

...

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$

if $\pi' \neq \text{failure}$ then

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ then

return failure

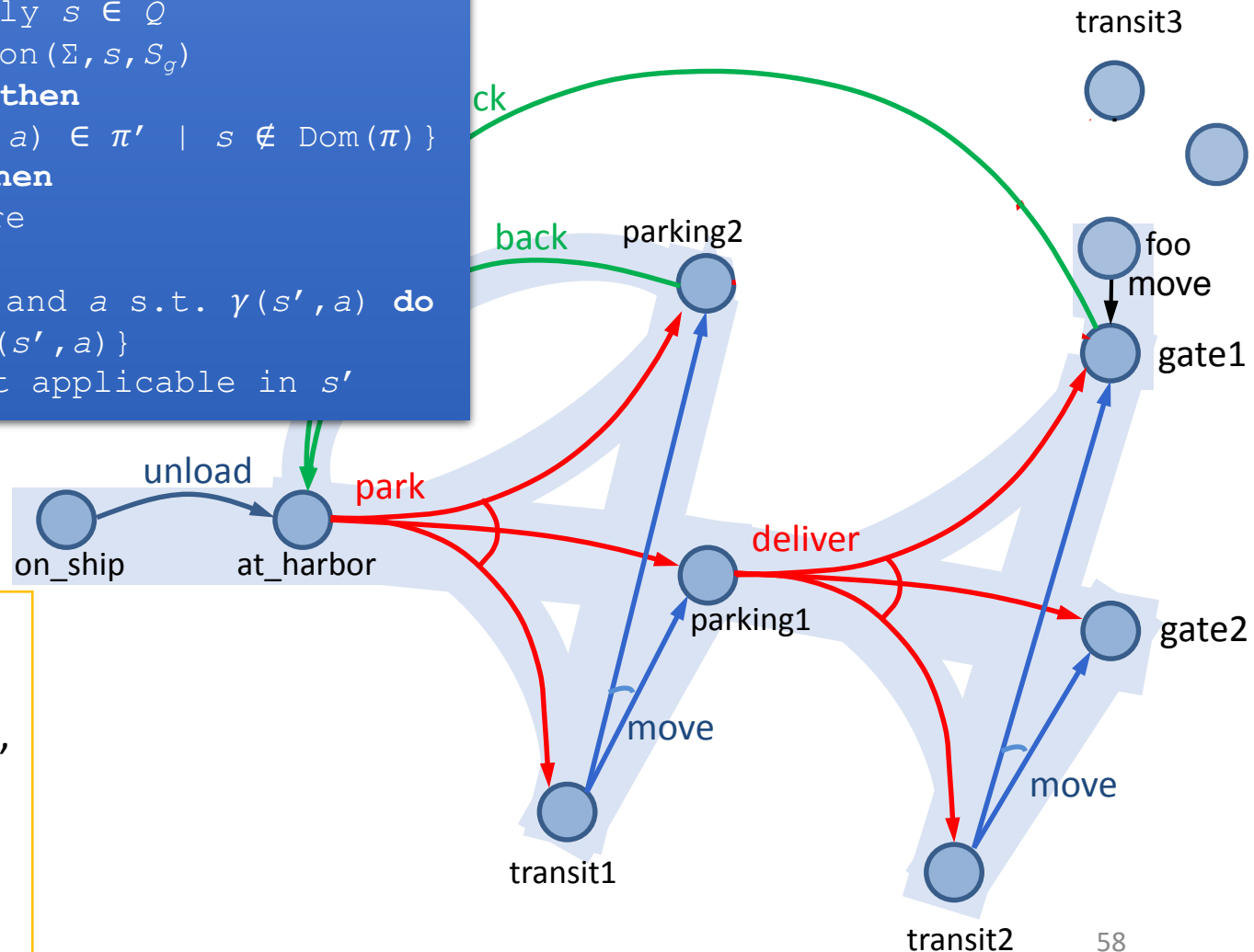
else

for every s' and a s.t. $\gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make a not applicable in s'

Example

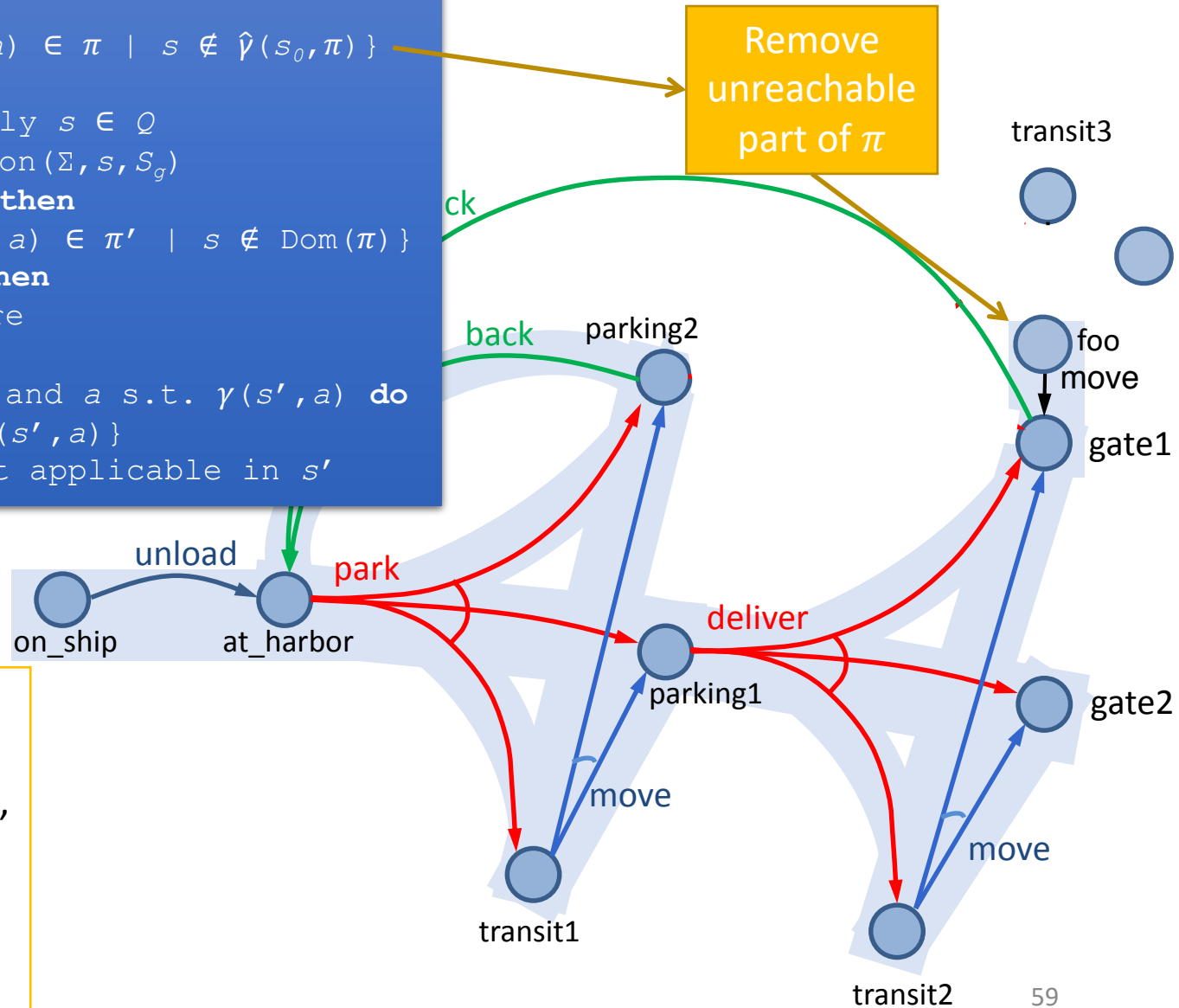


$\pi = \{(on_ship, unload),$
 $(at_harbor, park),$
 $(parking1, deliver),$
 $(foo, move),$
 $(parking2, back),$
 $(transit1, move),$
 $(transit2, move)\}$

Guided-Find-Safe-Solution (Σ, s_0, S_g)

```
...  
loop  
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$   
  if  $Q = \emptyset$  then  
     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{V}(s_0, \pi)\}$   
    return  $\pi$   
  select arbitrarily  $s \in Q$   
   $\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$   
  if  $\pi' \neq \text{failure}$  then  
     $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$   
  else if  $s = s_0$  then  
    return failure  
  else  
    for every  $s'$  and  $a$  s.t.  $\gamma(s', a)$  do  
       $\pi \leftarrow \pi \setminus \{(s', a)\}$   
      make  $a$  not applicable in  $s'$ 
```

Example



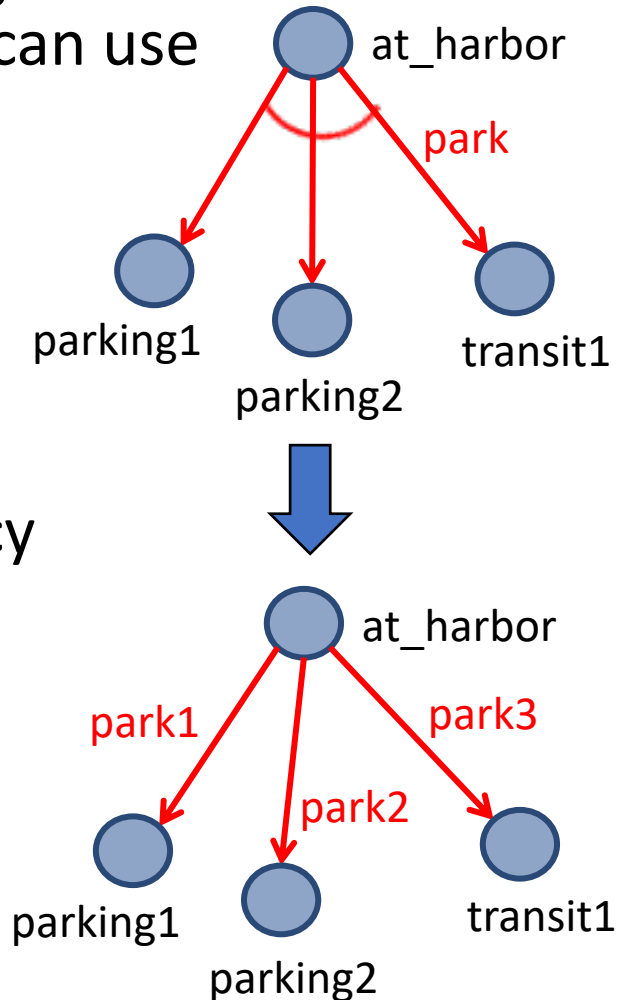
Determinisation

```
Guided-Find-Safe-Solution( $\Sigma, s_0, S_g$ )
  if  $s_0 \in S_g$  then
    return  $\emptyset$ 
  if  $\text{Applicable}(s_0) = \emptyset$  then
    return failure
   $\pi \leftarrow \emptyset$ 
  loop
     $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$ 
    if  $Q = \emptyset$  then
       $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\nu}(s_0, \pi)\}$ 
      return  $\pi$ 
    select arbitrarily  $s \in Q$ 
     $\pi' \leftarrow \text{Find-Solution}(\Sigma, s, S_g)$ 
    if  $\pi' \neq \text{failure}$  then
       $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$ 
    else if  $s = s_0$  then
      return failure
    else
      for every  $s'$  and  $a$  s.t.  $\gamma(s', a)$  do
         $\pi \leftarrow \pi \setminus \{(s', a)\}$ 
        make  $a$  not applicable in  $s'$ 
```

- How to implement it?
 - Need implementation of Find-Solution
 - Need it to be very efficient
 - Called many times
- Idea: instead, use a classical planner
 - Any algorithm from Chapter 2
 - Efficient algorithms, search heuristics
- For that, determinise actions

Determinisation

- Convert the nondeterministic actions into something the classical planner can use
- **Determinise**
 - Suppose a_i has n possible outcomes
 - n deterministic actions, one for each outcome
- Classical planner returns a plan $p = \langle a_1, a_2, \dots, a_n \rangle$
- If p is acyclic, can convert it to a policy
 - (unsafe) solution for P
 - $\{(s_0, \mathbf{a}_1), (s_1, \mathbf{a}_2), \dots, (s_{n-1}, \mathbf{a}_n)\}$ where
 - each \mathbf{a}_i is the nondeterministic action whose determinisation includes a_i
 - $s_i \in \gamma(s_{i-1}, \mathbf{a}_i)$



Determinisation

- Nondeterministic planning problem $P = (\Sigma, s_0, S_g)$
- Determinisation $P_d = (\Sigma_d, s_0, S_g)$
- Classical planner returns a solution for P_d
 - a plan $p = \langle a_1, a_2, \dots, a_n \rangle$
- If p is acyclic, can convert it to an (unsafe) solution for P
 - $\{(s_0, \mathbf{a}_1), (s_1, \mathbf{a}_2), \dots, (s_{n-1}, \mathbf{a}_n)\}$where
 - each \mathbf{a}_i is the nondeterministic action whose determinisation includes a_i
 - each $s_i \in \gamma(s_{i-1}, \mathbf{a}_i)$

```
Plan2policy(p= $\langle a_1, \dots, a_n \rangle, s$ )  
   $\pi \leftarrow \emptyset$   
  for  $i$  from 1 to  $n$  do  
     $\pi \leftarrow \pi \cup \{s, \text{det2nondet}(a_i)\}$   
     $s \leftarrow \gamma_d(s, a_i)$   
  return  $\pi$ 
```

Guided-Find-Safe-Solution

Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

if $s_0 \in S_g$ then

return \emptyset

if $\text{Applicable}(s_0) = \emptyset$ then

return failure

$\pi \leftarrow \emptyset$

$\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$

loop

$Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$

if $Q = \emptyset$ then

$\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\nu}(s_0, \pi)\}$

return π

select arbitrarily $s \in Q$

$p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$

if $p' \neq \text{fail}$ then

$\pi \leftarrow \text{Plan2policy}(p', s)$

$\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$

else if $s = s_0$ then

return failure

else

for every s' and a s.t. $\gamma(s', a)$ do

$\pi \leftarrow \pi \setminus \{(s', a)\}$

make the actions in the
determinisation not
applicable in s'

Same as Guided-Find-Safe-Solution.

Any classical planner that does not return cyclic plans.

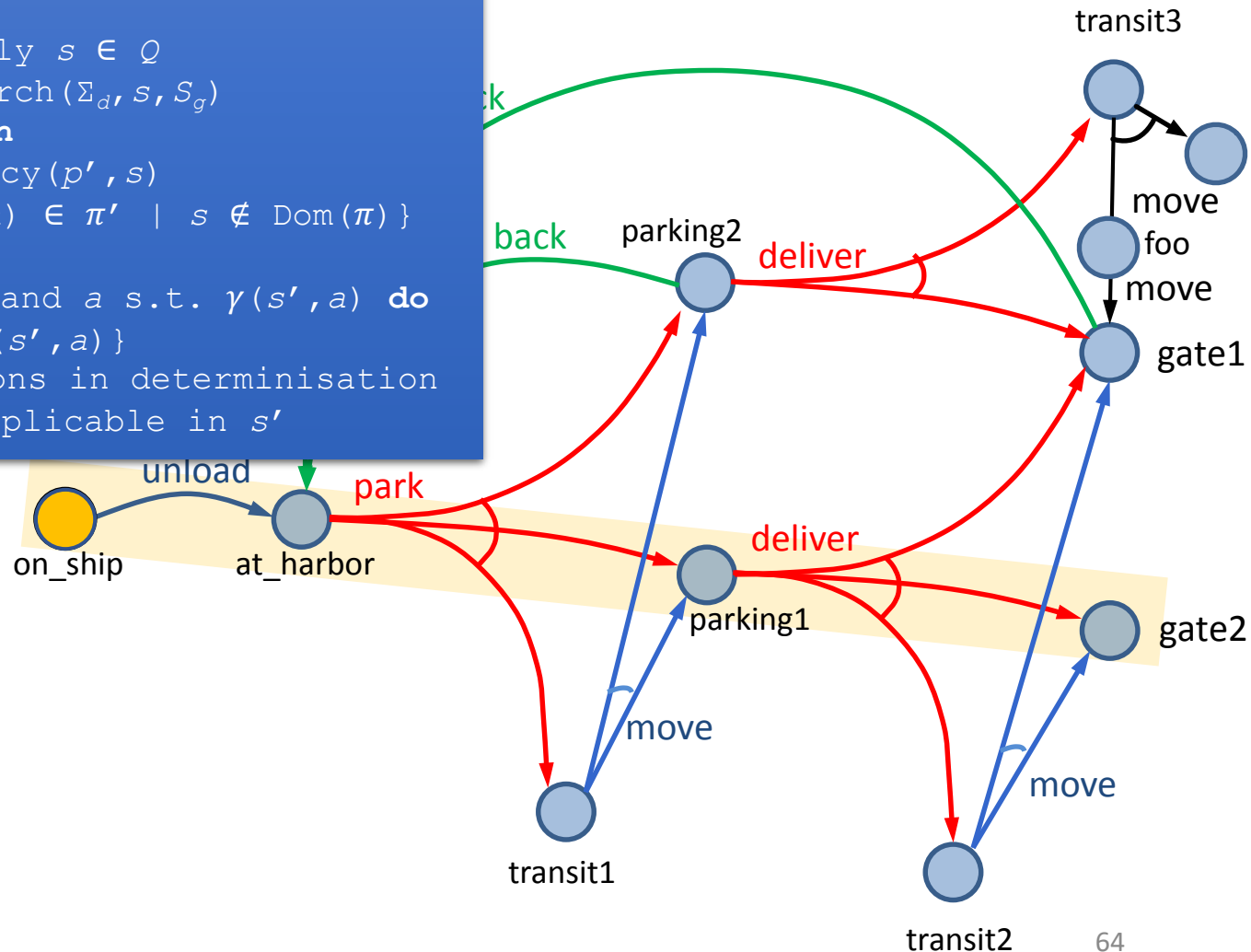
Convert p' to a policy. Add each (s, a) to π unless π already has an action at s .

s is unsolvable. For each (s', a) that can produce s , modify π and Σ_d so we will never use a at s' .

Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
loop  
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$   
  if  $Q = \emptyset$  then  
     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$   
    return  $\pi$   
  select arbitrarily  $s \in Q$   
   $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$   
  if  $p' \neq \text{fail}$  then  
     $\pi \leftarrow \text{Plan2policy}(p', s)$   
     $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$   
  else if ... else  
    for every  $s'$  and  $a$  s.t.  $\gamma(s', a)$  do  
       $\pi \leftarrow \pi \setminus \{(s', a)\}$   
      make actions in determinisation  
      not applicable in  $s'$ 
```

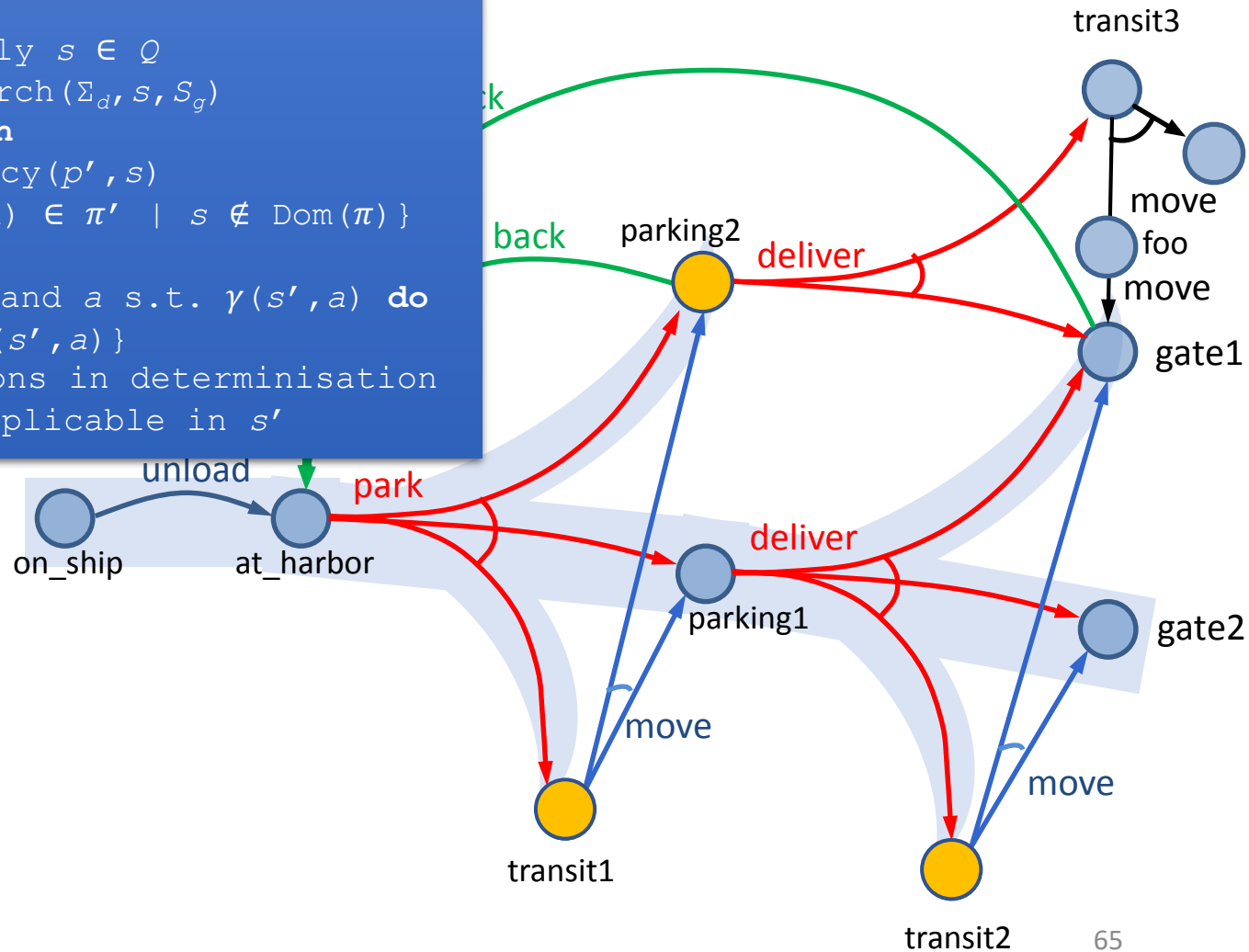
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
loop  
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$   
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    return  $\pi$   
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  else if ... else  
    for every  $s'$  and  $a$  s.t.  $\gamma(s', a)$  do  
       $\pi \leftarrow \pi \setminus \{(s', a)\}$   
      make actions in determinisation  
      not applicable in  $s'$ 
```

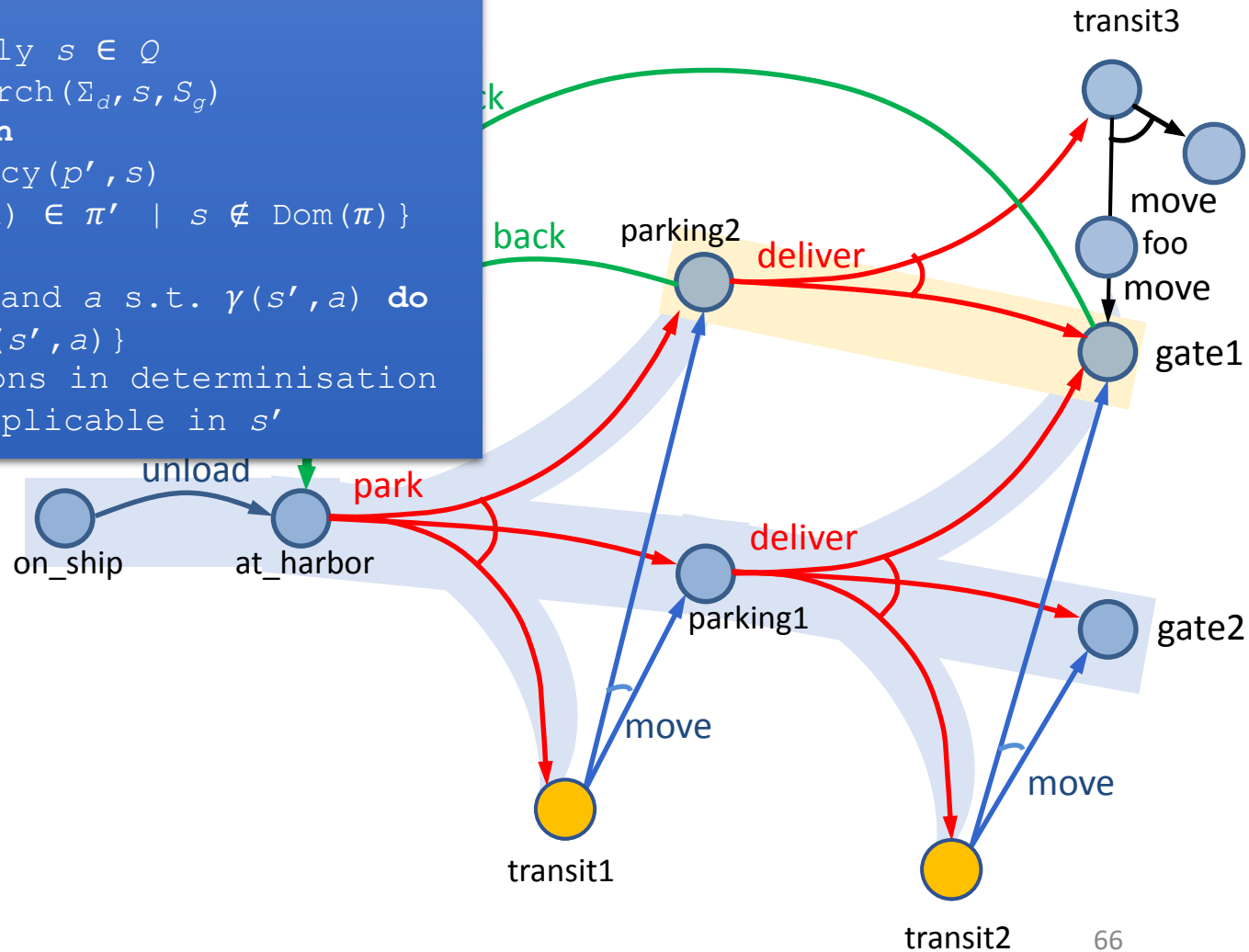
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
loop  
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$   
  if  $Q = \emptyset$  then  
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  select arbitrarily  $s \in Q$   
   $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$   
  if  $p' \neq \text{fail}$  then  
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     $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$   
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      make actions in determinisation  
      not applicable in  $s'$ 
```

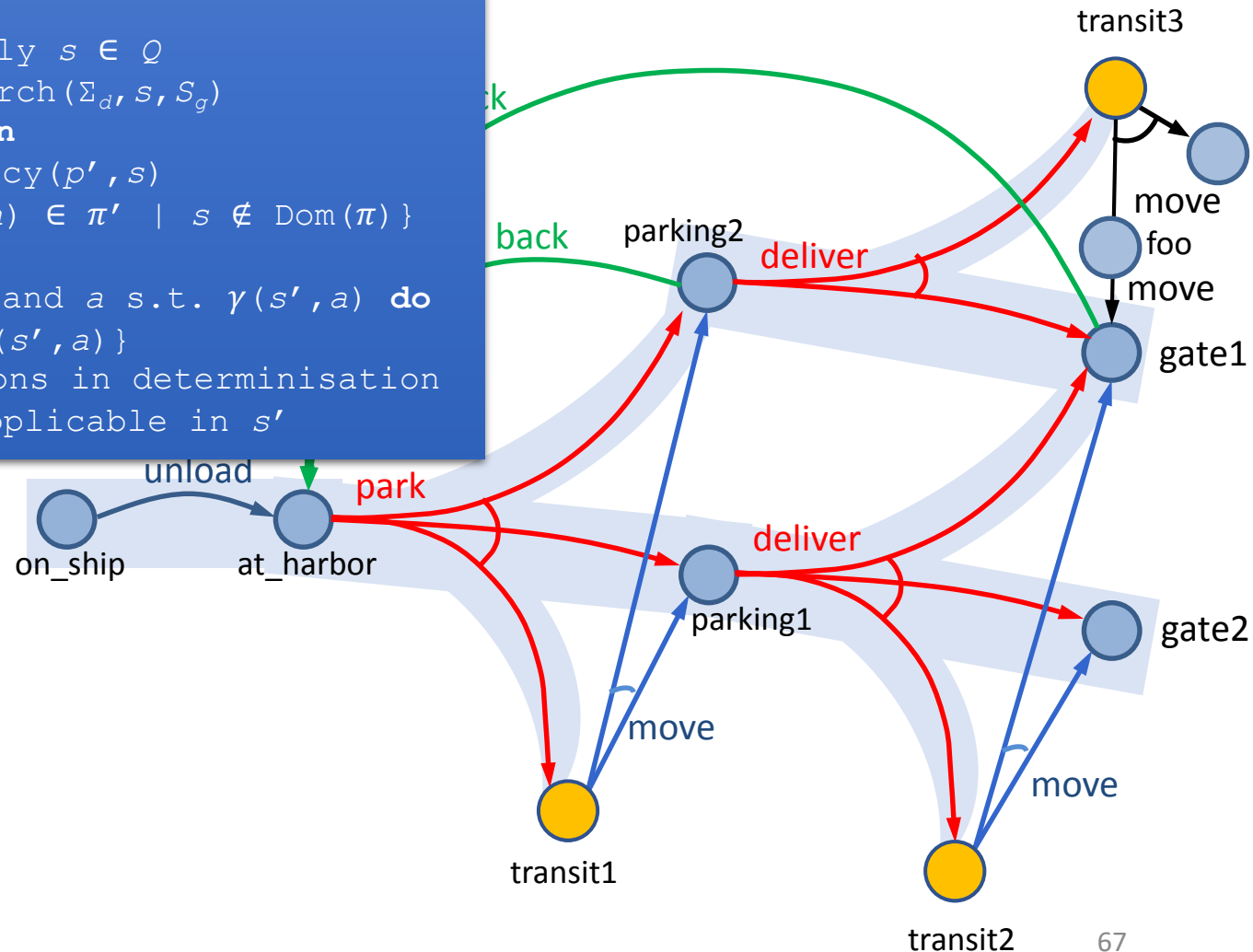
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
loop  
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$   
  if  $Q = \emptyset$  then  
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  select arbitrarily  $s \in Q$   
   $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$   
  if  $p' \neq \text{fail}$  then  
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    for every  $s'$  and  $a$  s.t.  $\gamma(s', a)$  do  
       $\pi \leftarrow \pi \setminus \{(s', a)\}$   
      make actions in determinisation  
      not applicable in  $s'$ 
```

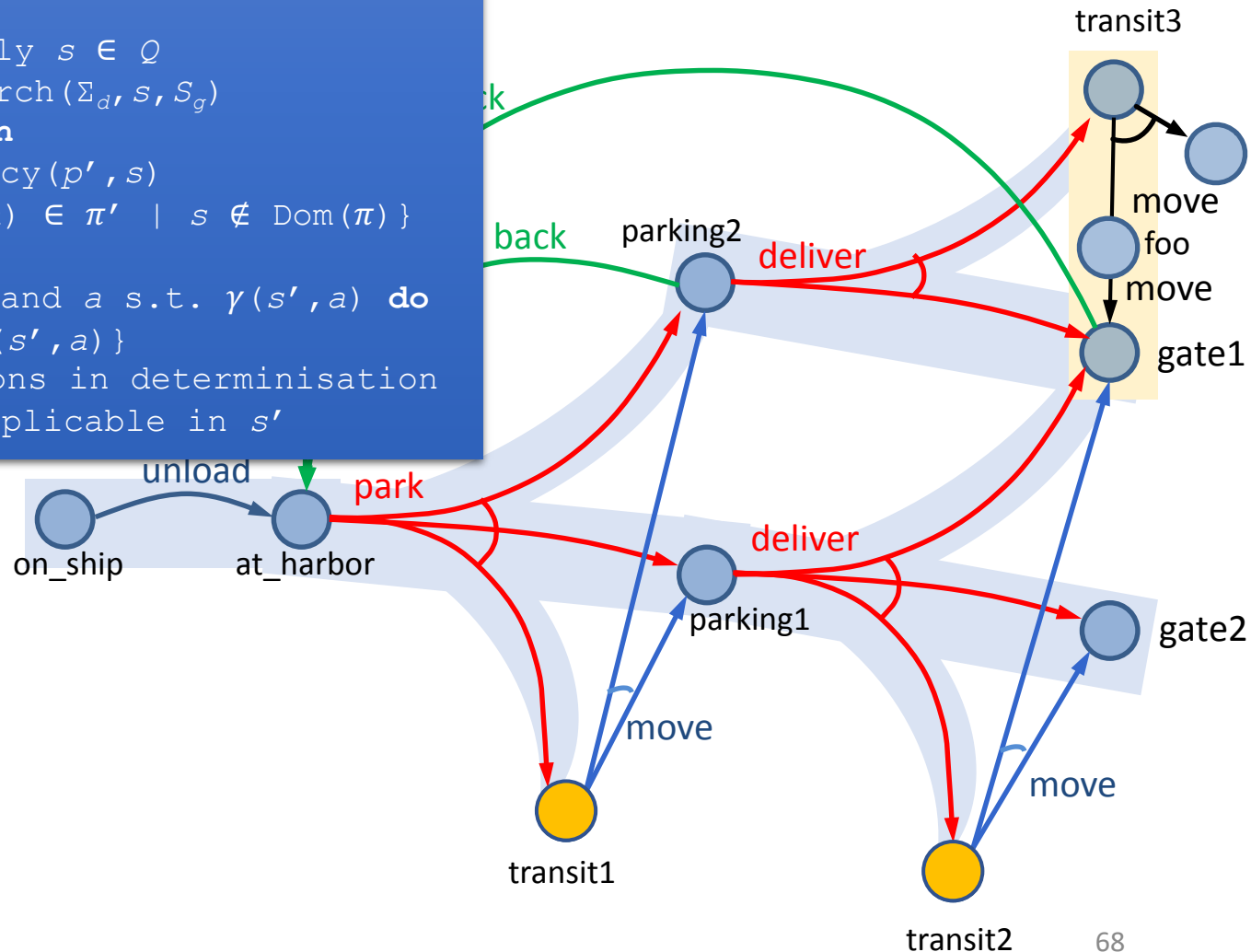
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
loop  
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$   
  if  $Q = \emptyset$  then  
     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$   
    return  $\pi$   
  select arbitrarily  $s \in Q$   
   $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$   
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      make actions in determinisation  
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```

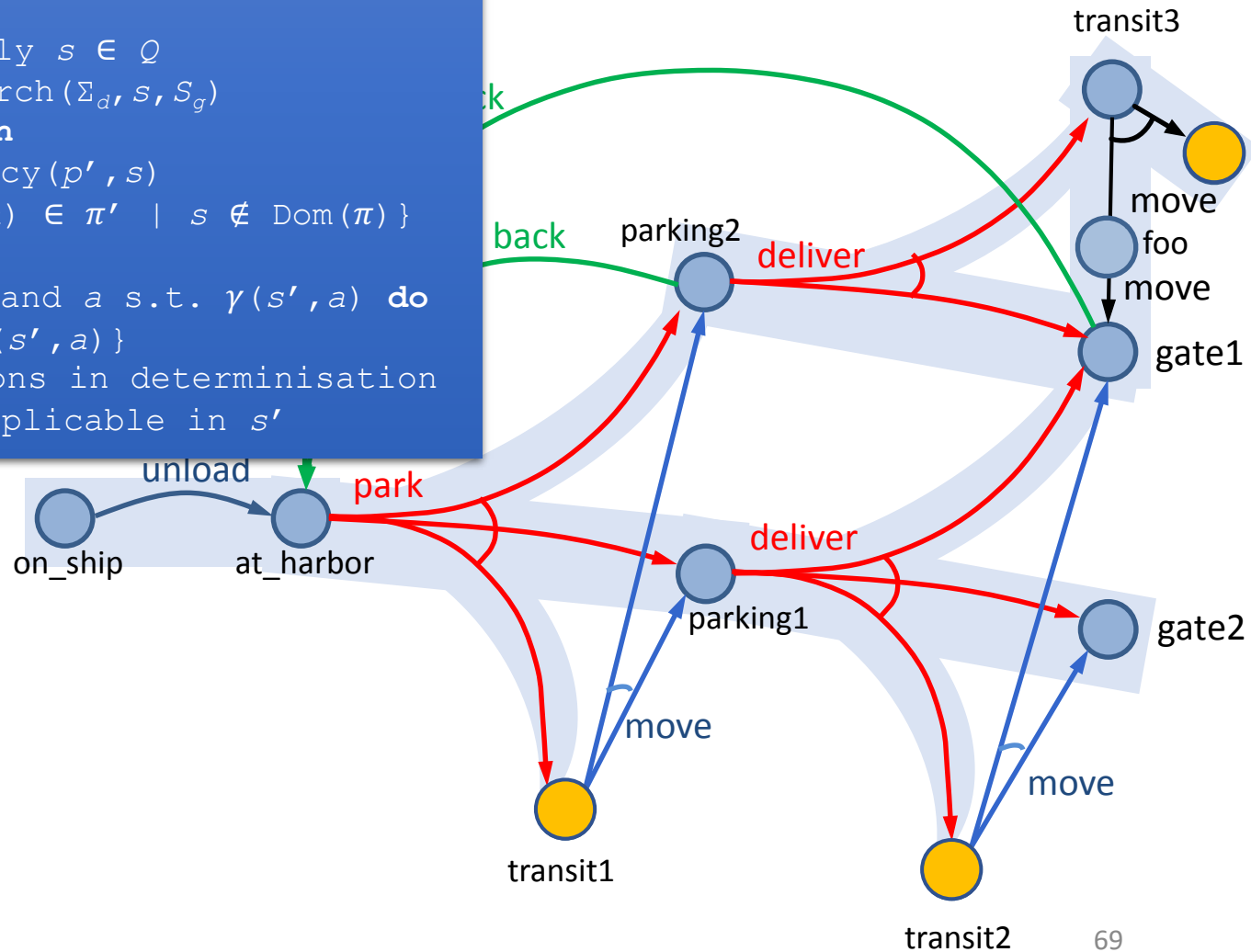
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$ 
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   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$ 
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      make actions in determinisation
      not applicable in  $s'$ 
```

Example

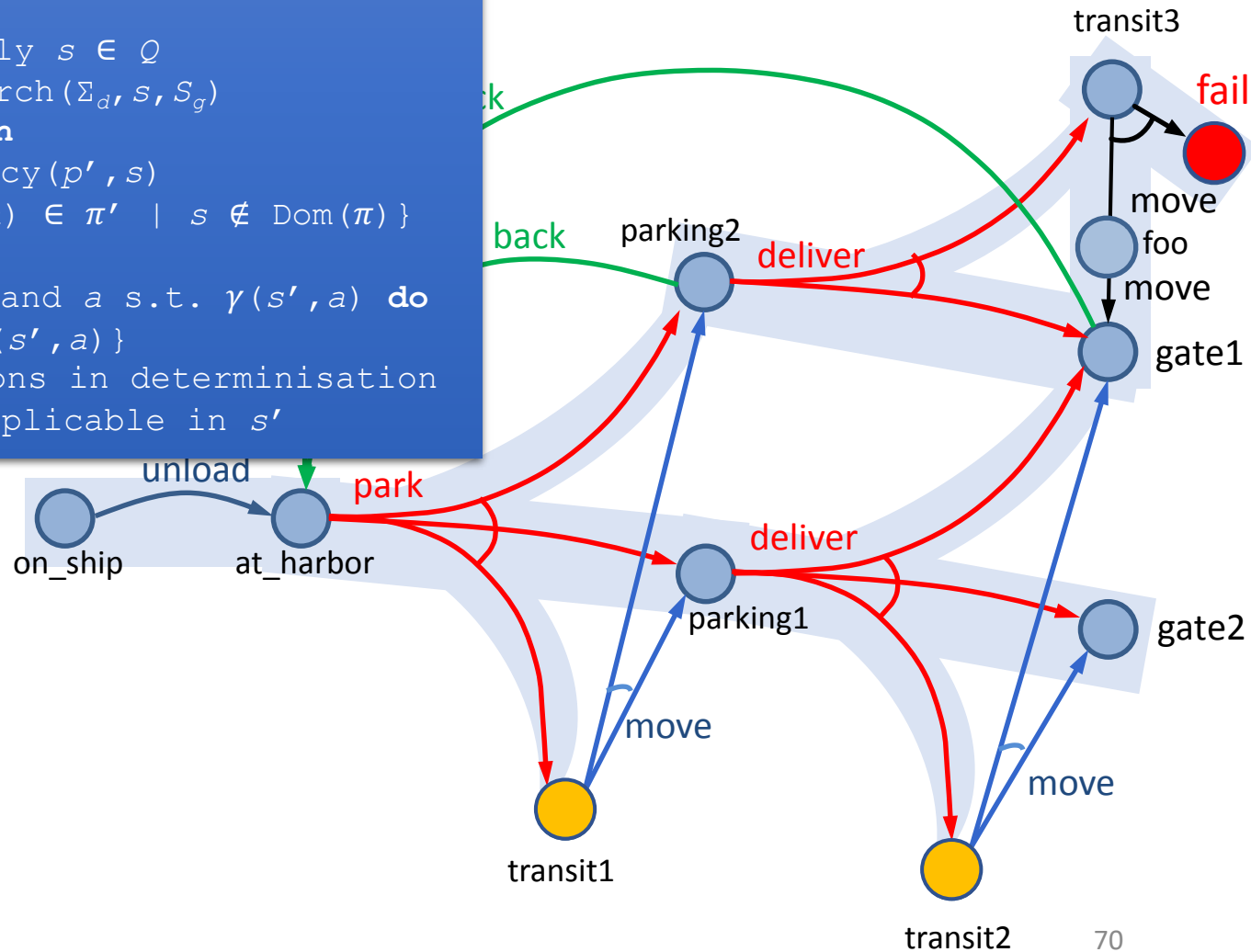


Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```

...
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    return  $\pi$ 
  select arbitrarily  $s \in Q$ 
   $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$ 
  if  $p' \neq \text{fail}$  then
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       $\pi \leftarrow \pi \setminus \{(s', a)\}$ 
      make actions in determinisation
      not applicable in  $s'$ 
  
```

Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

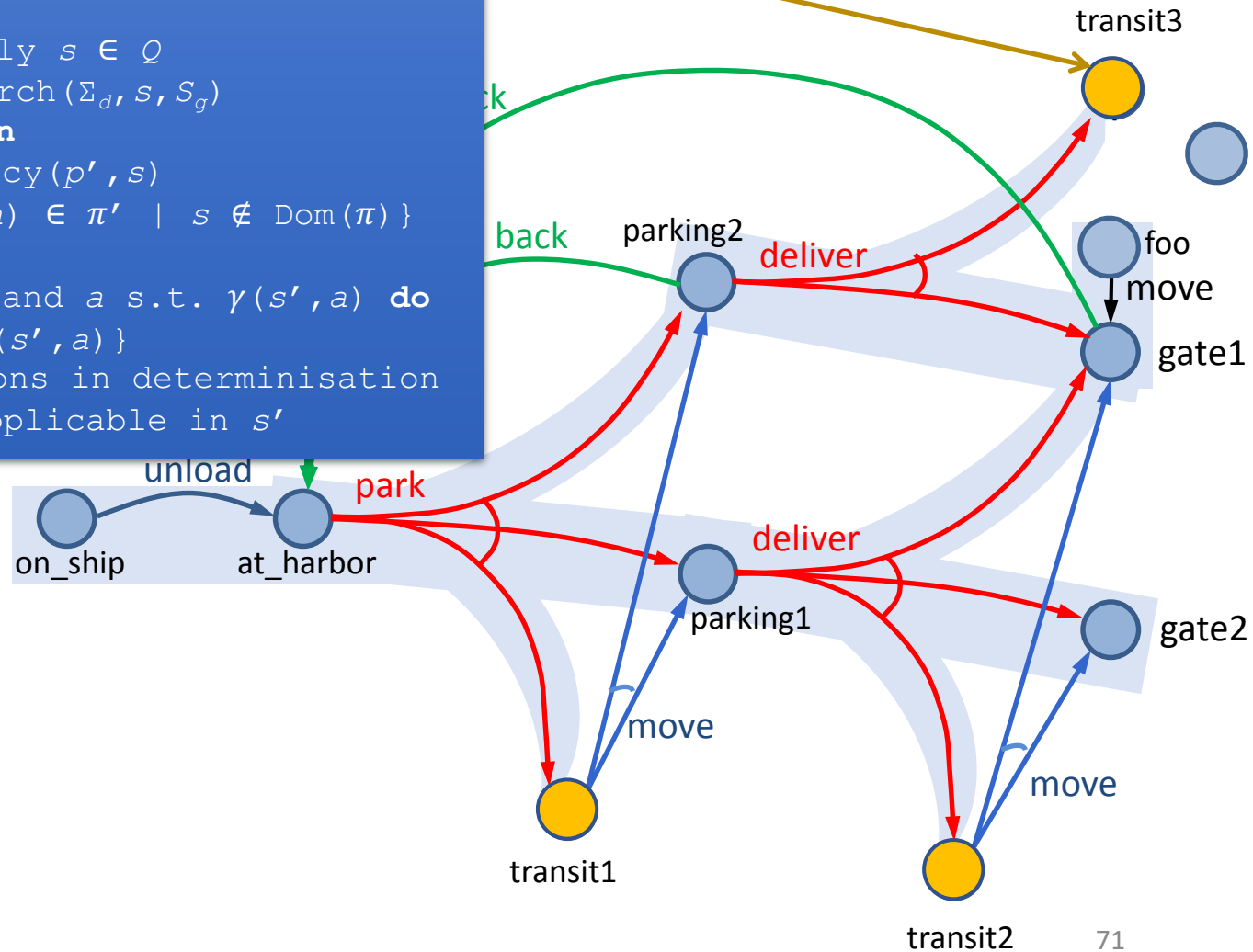
```

...
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$ 
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   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$ 
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       $\pi \leftarrow \pi \setminus \{(s', a)\}$ 
      make actions in determinisation
      not applicable in  $s'$ 

```

Example

Modify Σ_d to make move inapplicable

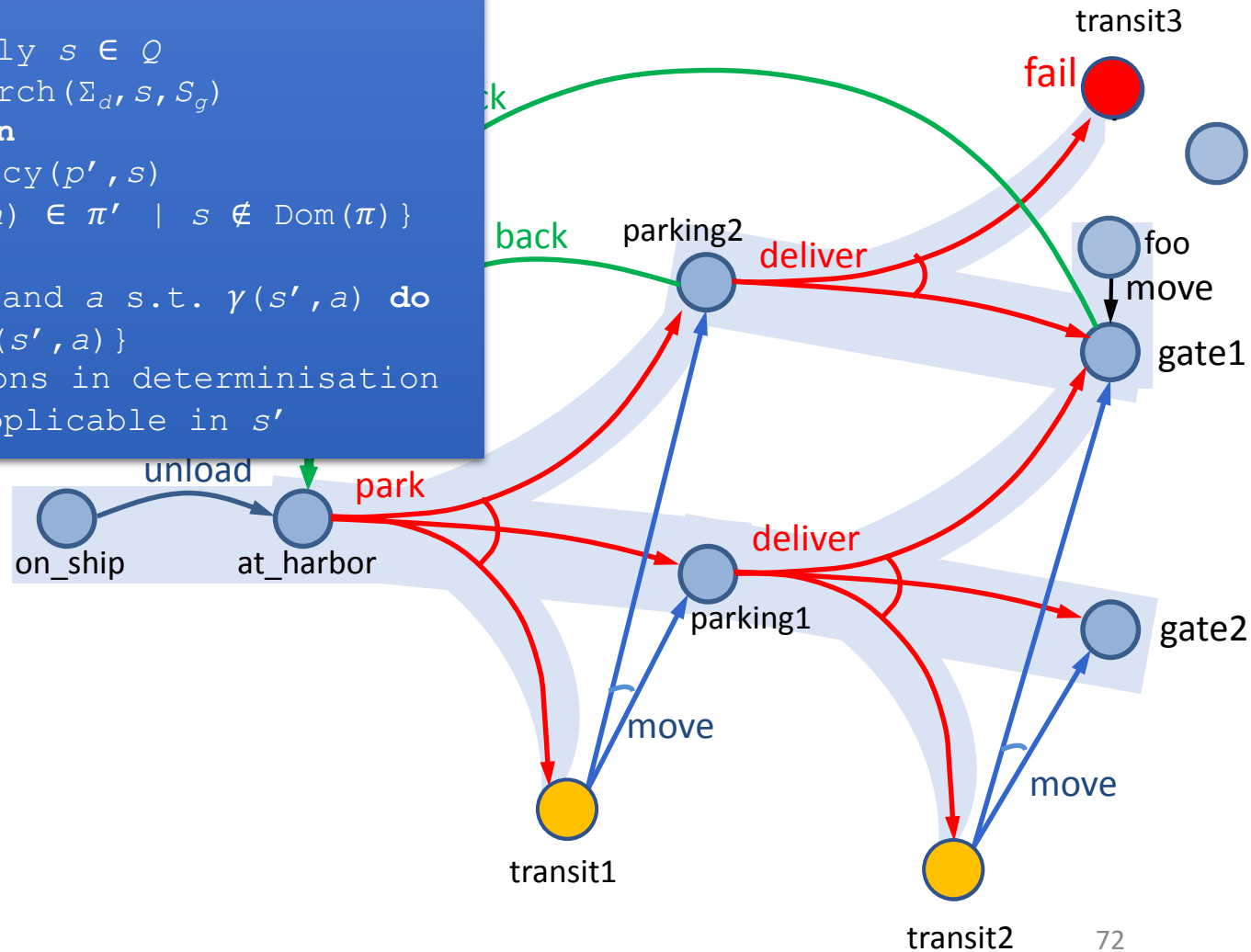


Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```

...
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$ 
loop
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$ 
  if  $Q = \emptyset$  then
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    return  $\pi$ 
  select arbitrarily  $s \in Q$ 
   $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$ 
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    for every  $s'$  and  $a$  s.t.  $\gamma(s', a)$  do
       $\pi \leftarrow \pi \setminus \{(s', a)\}$ 
      make actions in determinisation
      not applicable in  $s'$ 
  
```

Example



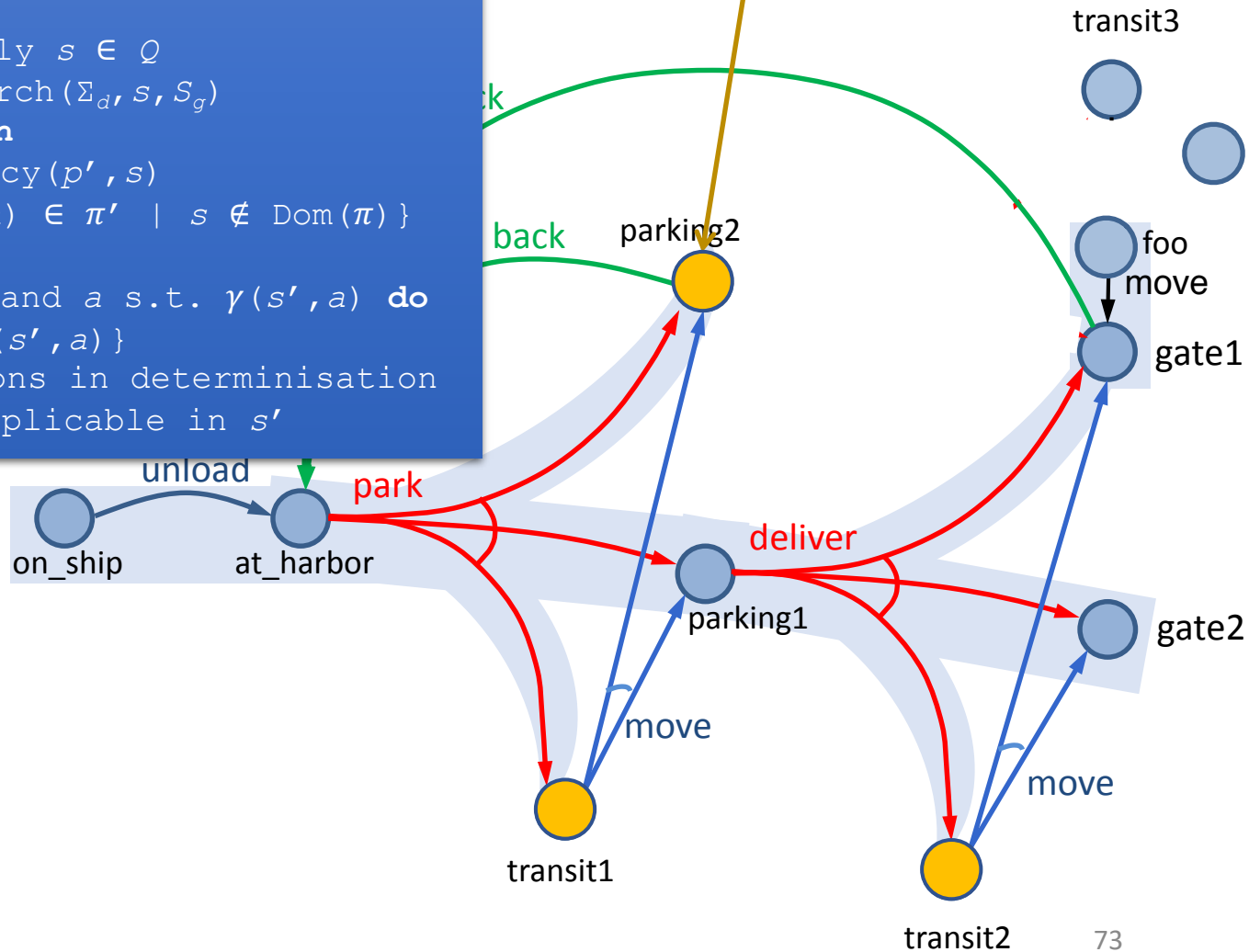
Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```

...
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$ 
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      not applicable in  $s'$ 
  
```

Example

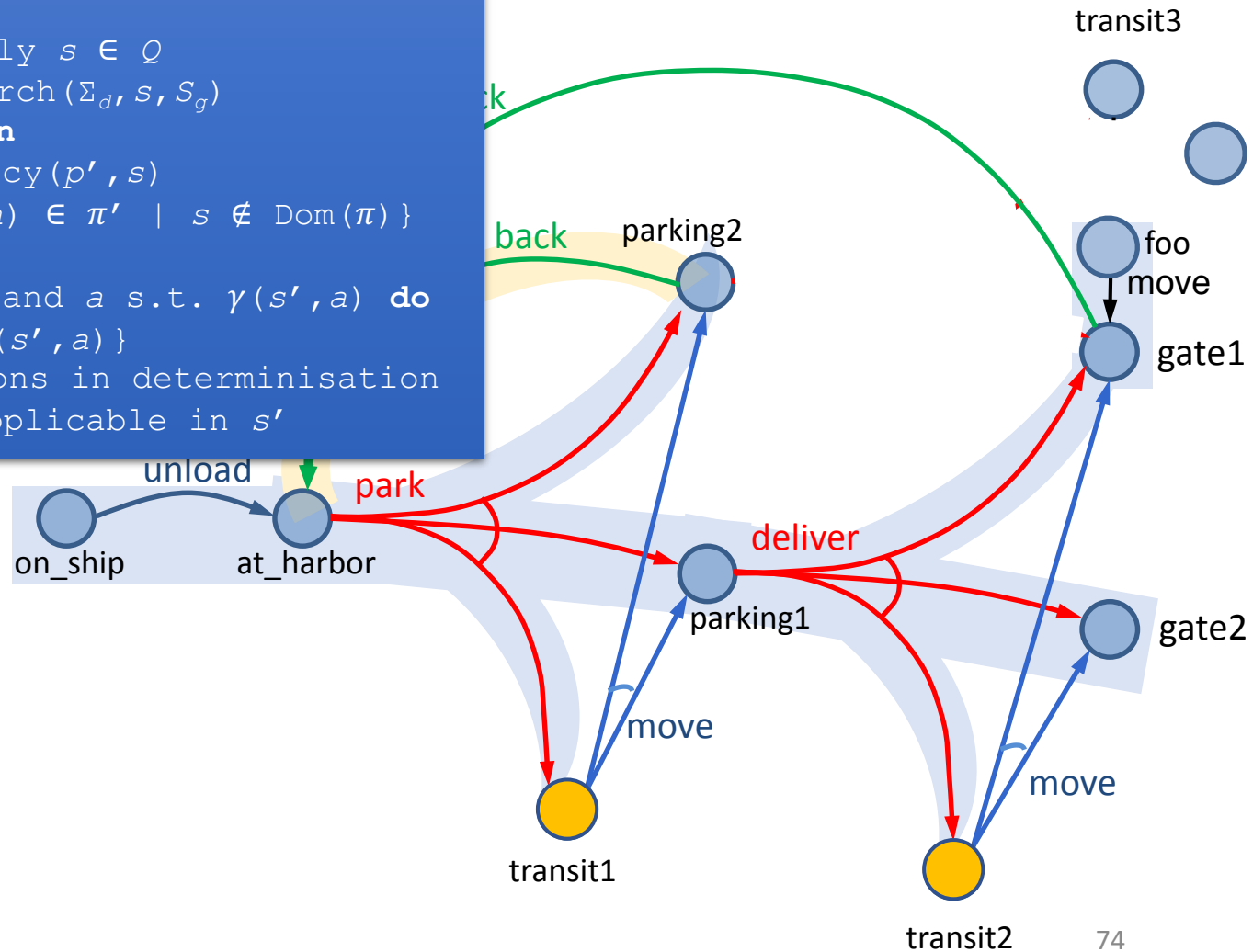
Modify Σ_d to make move inapplicable



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
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  if  $Q = \emptyset$  then  
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    return  $\pi$   
  select arbitrarily  $s \in Q$   
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```

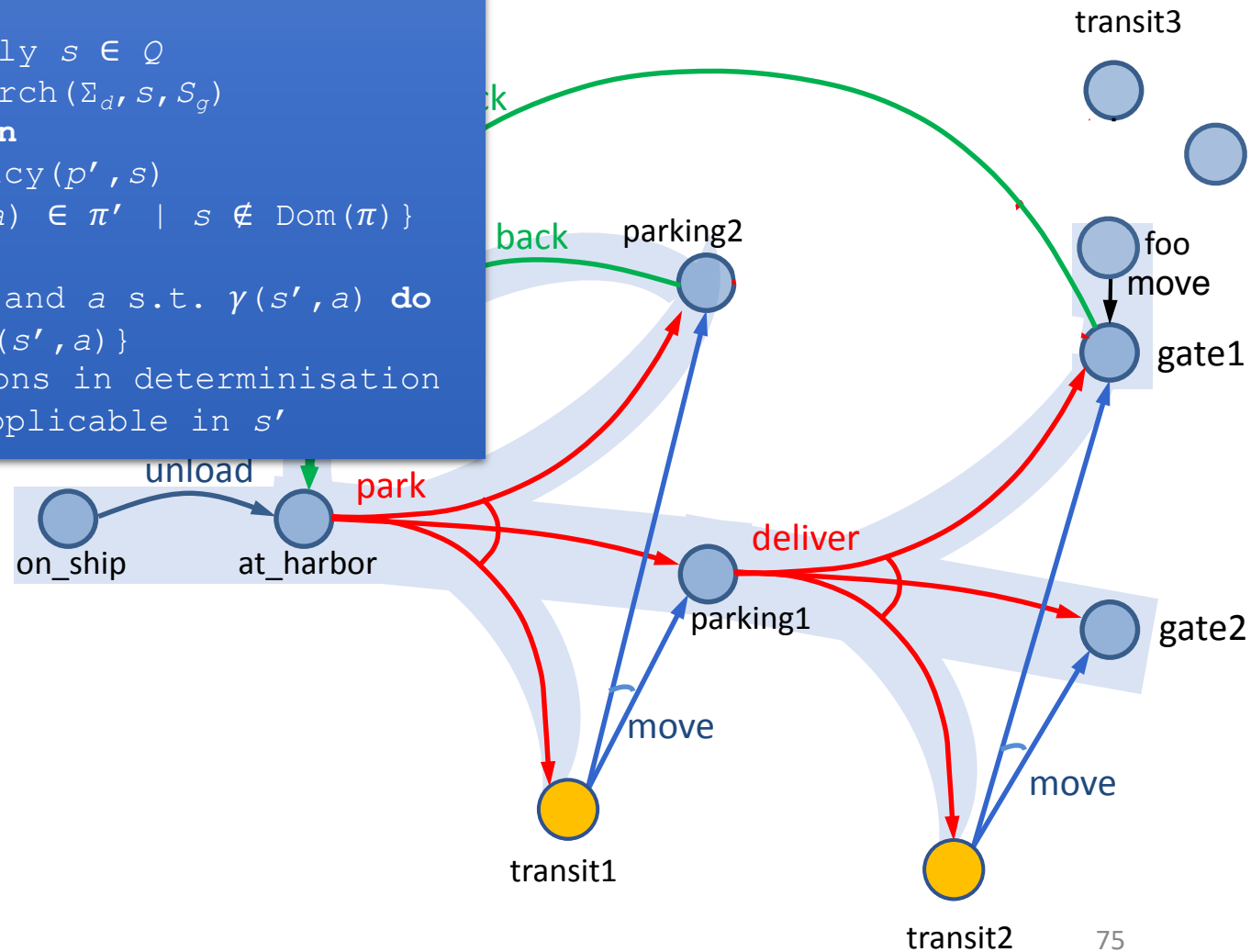
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
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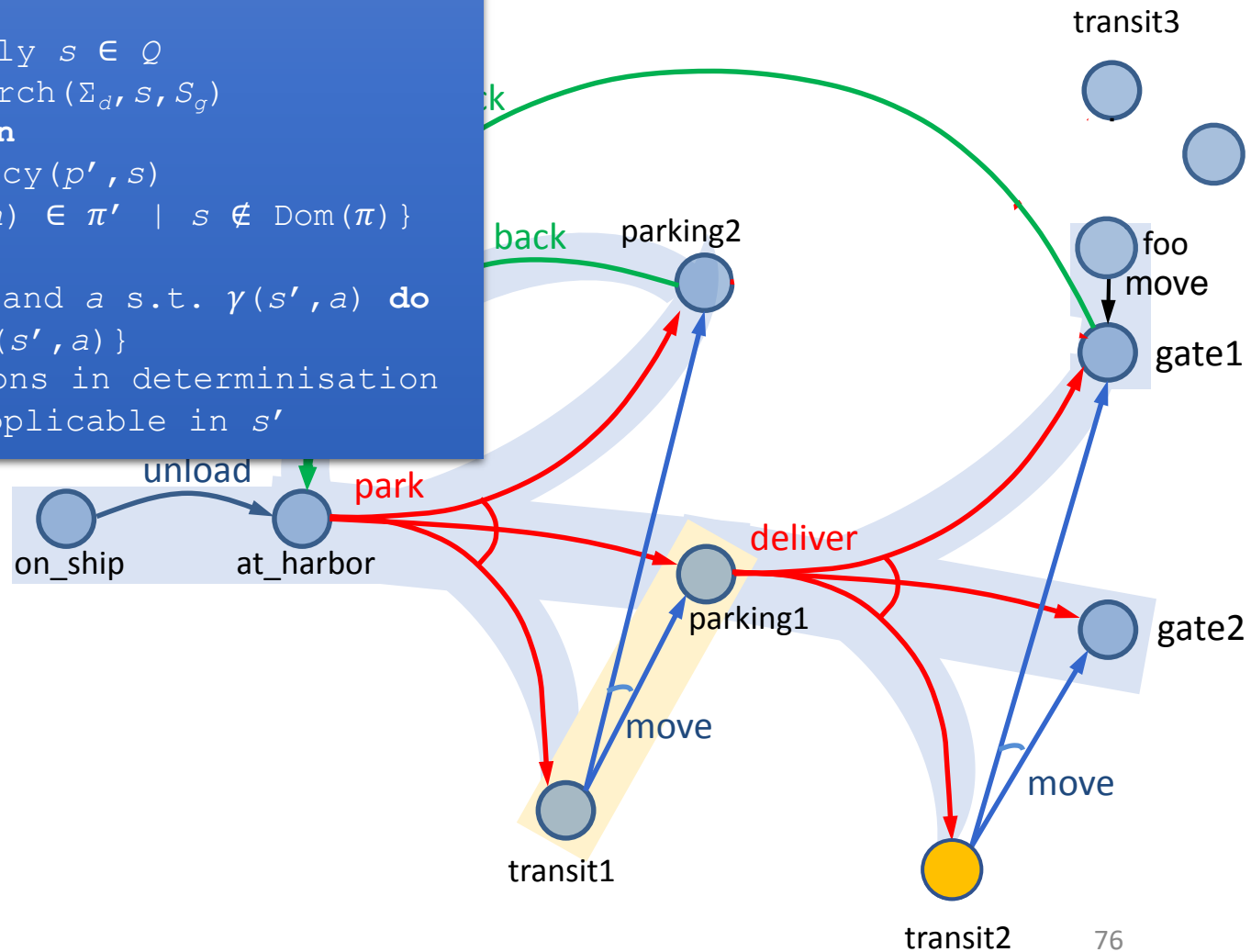
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
loop  
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$   
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```

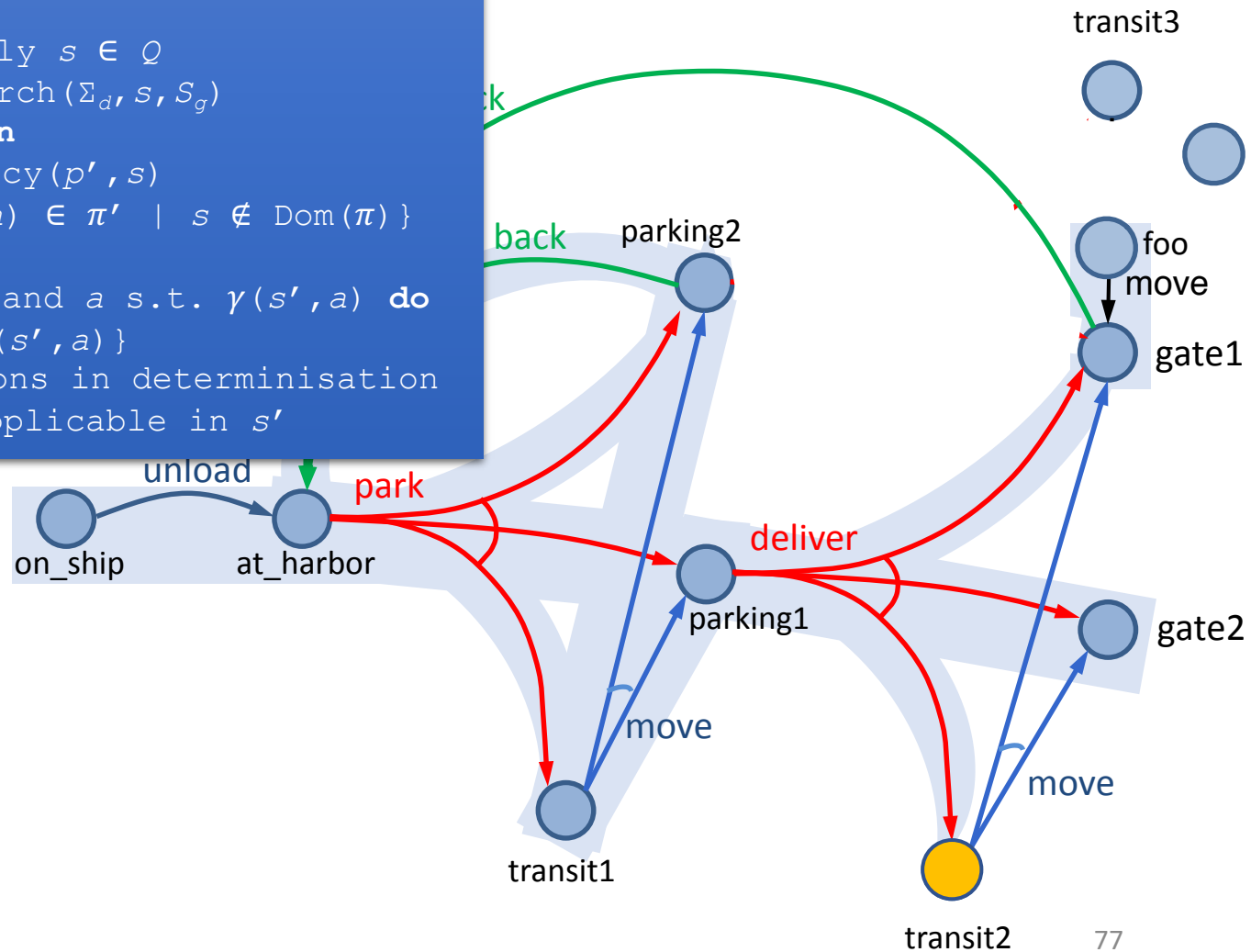
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
loop  
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     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$   
    return  $\pi$   
  select arbitrarily  $s \in Q$   
   $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$   
  if  $p' \neq \text{fail}$  then  
     $\pi \leftarrow \text{Plan2policy}(p', s)$   
     $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$   
  else if ... else  
    for every  $s'$  and  $a$  s.t.  $\gamma(s', a)$  do  
       $\pi \leftarrow \pi \setminus \{(s', a)\}$   
      make actions in determinisation  
      not applicable in  $s'$ 
```

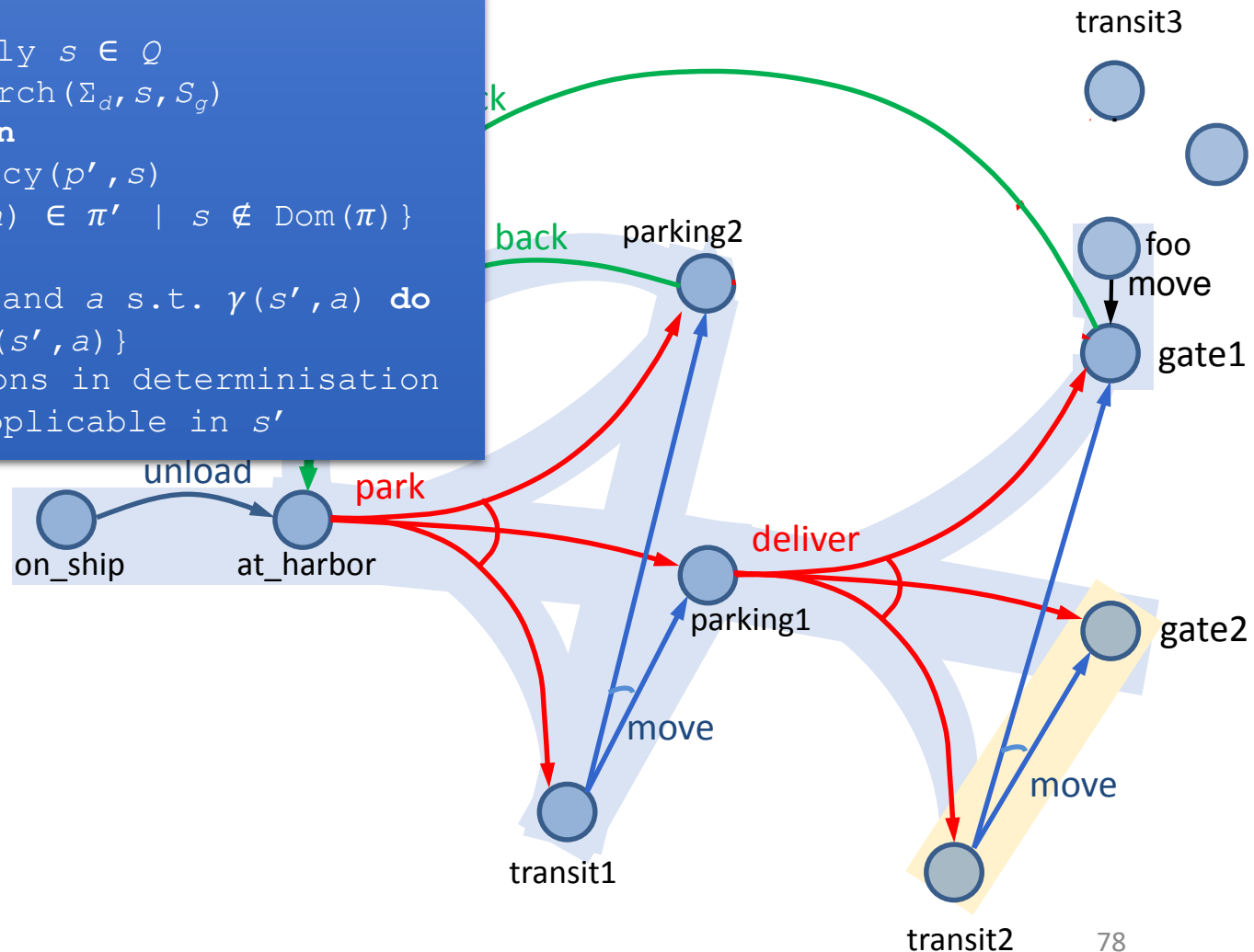
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
loop  
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$   
  if  $Q = \emptyset$  then  
     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$   
    return  $\pi$   
  select arbitrarily  $s \in Q$   
   $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$   
  if  $p' \neq \text{fail}$  then  
     $\pi \leftarrow \text{Plan2policy}(p', s)$   
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      make actions in determinisation  
      not applicable in  $s'$ 
```

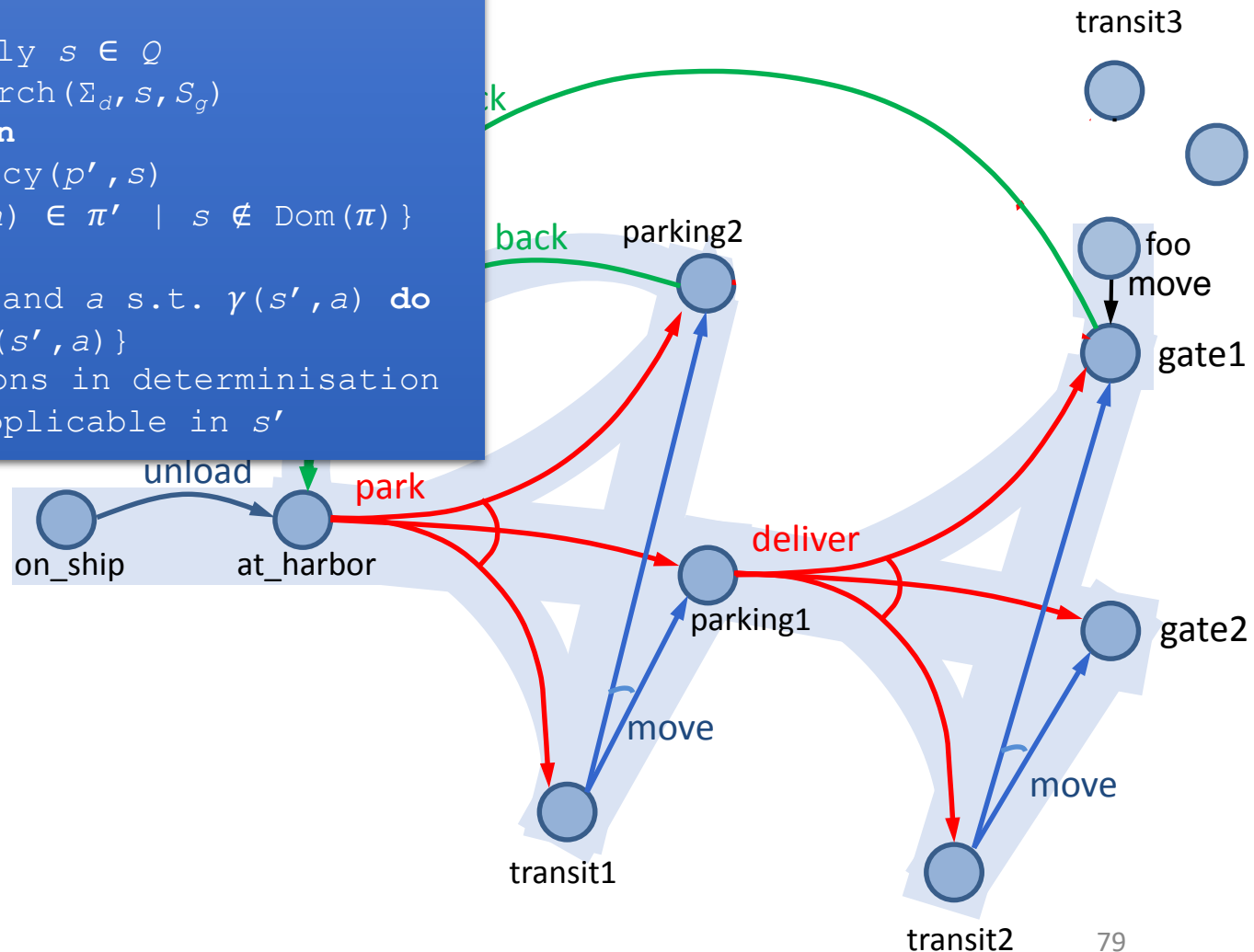
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
loop  
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$   
  if  $Q = \emptyset$  then  
     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$   
    return  $\pi$   
  select arbitrarily  $s \in Q$   
   $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$   
  if  $p' \neq \text{fail}$  then  
     $\pi \leftarrow \text{Plan2policy}(p', s)$   
     $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$   
  else if ... else  
    for every  $s'$  and  $a$  s.t.  $\gamma(s', a)$  do  
       $\pi \leftarrow \pi \setminus \{(s', a)\}$   
      make actions in determinisation  
      not applicable in  $s'$ 
```

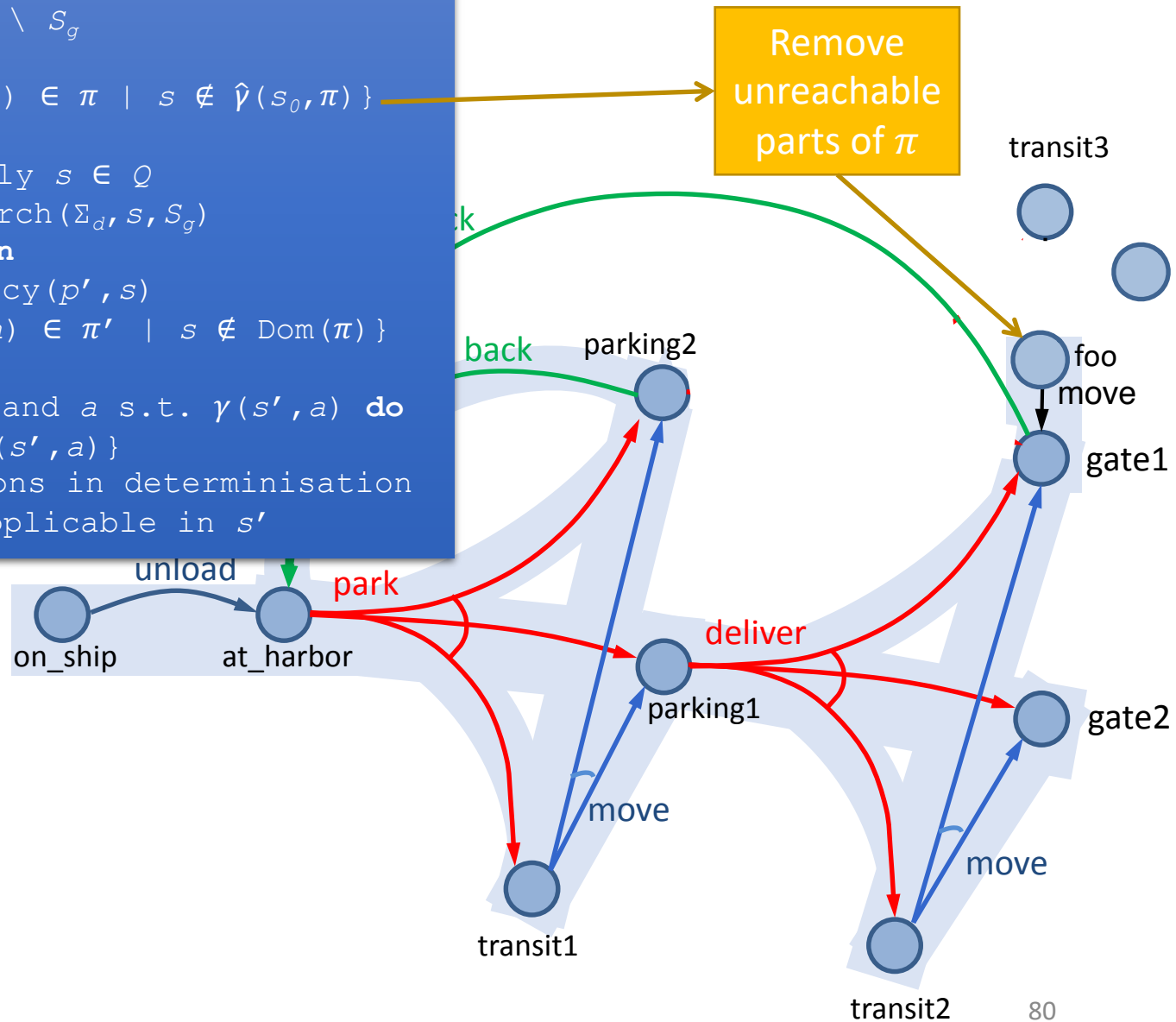
Example



Find-Safe-Solution-by-Determinisation (Σ, s_0, S_g)

```
...  
 $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$   
loop  
   $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$   
  if  $Q = \emptyset$  then  
     $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\gamma}(s_0, \pi)\}$   
    return  $\pi$   
  select arbitrarily  $s \in Q$   
   $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$   
  if  $p' \neq \text{fail}$  then  
     $\pi \leftarrow \text{Plan2policy}(p', s)$   
     $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$   
  else if ... else  
    for every  $s'$  and  $a$  s.t.  $\gamma(s', a)$  do  
       $\pi \leftarrow \pi \setminus \{(s', a)\}$   
      make actions in determinisation  
      not applicable in  $s'$ 
```

Example



Making Actions Inapplicable

```
Find-Safe-Solution-by-Determinisation( $\Sigma, s_0, S_g$ )
  if  $s_0 \in S_g$  then
    return  $\emptyset$ 
  if  $\text{Applicable}(s_0) = \emptyset$  then
    return failure
   $\pi \leftarrow \emptyset$ 
   $\Sigma_d \leftarrow \text{mk-deterministic}(\Sigma)$ 
  loop
     $Q \leftarrow \text{leaves}(s_0, \pi) \setminus S_g$ 
    if  $Q = \emptyset$  then
       $\pi \leftarrow \pi \setminus \{(s, a) \in \pi \mid s \notin \hat{\nu}(s_0, \pi)\}$ 
      return  $\pi$ 
    select arbitrarily  $s \in Q$ 
     $p' \leftarrow \text{Forward-search}(\Sigma_d, s, S_g)$ 
    if  $p' \neq \text{fail}$  then
       $\pi \leftarrow \text{Plan2policy}(p', s)$ 
       $\pi \leftarrow \pi \cup \{(s, a) \in \pi' \mid s \notin \text{Dom}(\pi)\}$ 
    else if  $s = s_0$  then
      return failure
    else
      for every  $s'$  and  $a$  s.t.  $\gamma(s', a)$  do
         $\pi \leftarrow \pi \setminus \{(s', a)\}$ 
        make the actions in the
          determinisation not
          applicable in  $s'$ 
```

- Modify Σ_d to make actions inapplicable
 - worst-case exponential time
- Better:
table of bad state-action pairs
 - For every (s', a) s.t. $s \in \gamma(s', a)$,
$$\text{Bad}[s'] \leftarrow \text{Bad}[s'] \cup \text{determinization}(a)$$
- Modify classical planner to take the table as an argument
 - if s is current state, only choose actions in $\text{Applicable}(s) \setminus \text{Bad}(s)$

Intermediate Summary

- Determinisation Techniques
 - Guided-find-safe-solution
 - call find-solution to get an unsafe solution
 - call find-solution additional times on the leaves
 - Find-safe-solution-by-determinization
 - use determinized actions
 - call classical planner rather than find-solution
 - if dead-ends are encountered, modify actions that lead to them

Outline per the Book

5.2 Planning Problem

- Planning domains
- Plans as policies
- Planning problems and solutions

5.3 And/Or Graph Search

- Planning by forward search

5.5 Determinisation Techniques

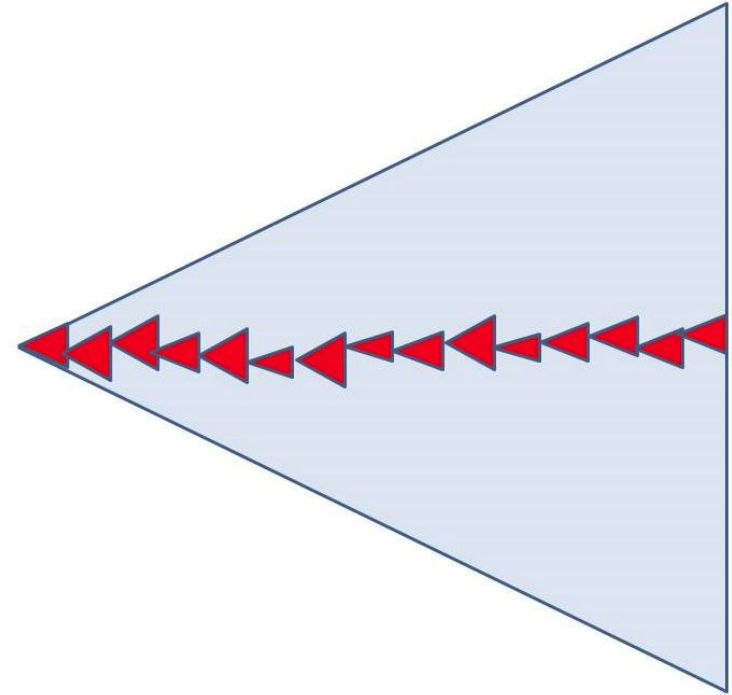
- Guided planning for safe solutions
- Planning for safe solutions by determinisation

5.6 Online Approaches

- Lookahead
- Lookahead by Determinisation
- Lookahead with a bounded number of steps

Online Approaches

- Motivation
 - Planning models are approximate – execution seldom works out as planned
 - Large problems may require too much planning time
- 2nd motivation even more stronger in nondeterministic domains
 - Nondeterminism makes planning exponentially harder
 - Exponentially more time, exponentially larger policies



Offline vs Runtime
Search Spaces

Online Approaches

- Need to identify **good** actions without exploring entire search space
 - Can be done using heuristic estimates
- Some domains are **safely explorable**
 - Safe to create partial plans, because goal states are reachable from all situations
- Other domains contain dead-ends, partial planning will not guarantee success
 - Can get trapped in dead ends that we would have detected if we had planned fully
 - No applicable actions
 - Robot goes down a steep incline and can't come back up
 - Applicable actions, but caught in a loop
 - Robot goes into a collection of rooms from which there's no exit
 - However, partial planning can still make success more likely

Lookahead-Partial-Plan

- Adaptation of Run-Lazy-Lookahead (Chapter 2)
- Lookahead is any planning algorithm that returns a policy π
 - π may be partial solution, or unsafe solution
 - Lookahead-Partial-Plan executes π as far as it will go, then calls Lookahead again
 - θ context-dependent vector of parameters to restrict in some way the search for a solution

```
Lookahead-Partial-Plan( $\Sigma, s_0, S_g$ )
```

```
 $s \leftarrow s_0$   
while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do  
   $\pi \leftarrow \text{Lookahead}(s, \theta)$   
  if  $\pi = \emptyset$  then  
    return failure  
  else  
    perform partial plan  $\pi$   
     $s \leftarrow$  observe current state
```

FS-Replan

- Adaptation of Run-Lookahead (Ch. 2)
- Calls Forward-Search (Ch. 2) on determinized domain, converts to a policy
 - Unsafe solution
- Generalization:
 - Lookahead can be any planning algorithm that returns a policy π

```
FS-Replan( $\Sigma, s, S_g$ )
```

```
 $\pi_d \leftarrow \emptyset$ 
```

```
while  $s \notin S_g$  and Applicable( $s$ )  $\neq \emptyset$  do
```

```
  if  $\pi_d$  undefined for  $s$  then
```

```
     $\pi_d \leftarrow$  Plan2policy(Forward-search( $\Sigma_d, s, S_g$ ),  $s$ )
```

```
    if  $\pi_d =$  failure then
```

```
      return failure
```

```
  perform action  $\pi_d(s)$ 
```

```
   $s \leftarrow$  observe resulting state
```

```
Generalised-FS-Replan( $\Sigma, s, S_g$ )
```

```
 $\pi_d \leftarrow \emptyset$ 
```

```
while  $s \notin S_g$  and Applicable( $s$ )  $\neq \emptyset$  do
```

```
  if  $\pi_d$  undefined for  $s$  then
```

```
     $\pi_d \leftarrow$  Lookahead( $s, \theta$ )
```

```
    if  $\pi_d =$  failure then
```

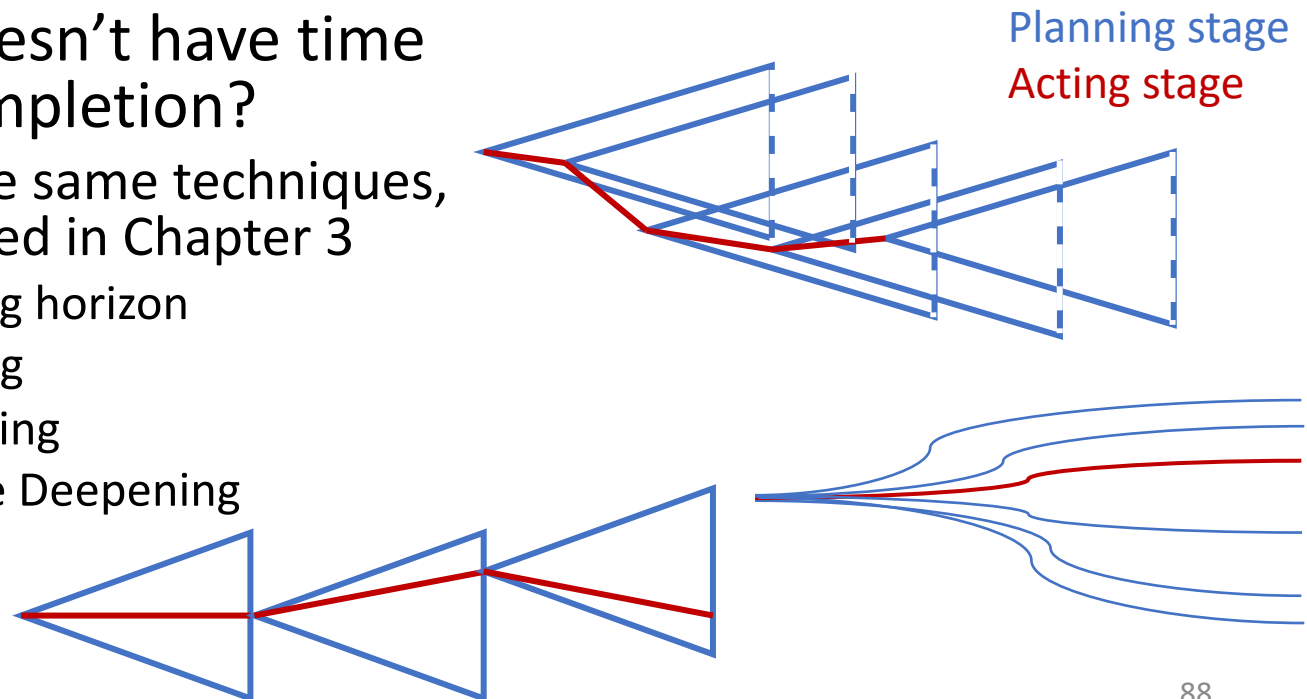
```
      return failure
```

```
  perform action  $\pi_d(s)$ 
```

```
   $s \leftarrow$  observe resulting state
```

Possibilities for Lookahead

- Lookahead could be one of the algorithms we discussed earlier
 - Find-Safe-Solution
 - Find-Acyclic-Solution
 - Guided-Find-Safe-Solution
 - Find-Safe-Solution-by-Determinization
- What if it doesn't have time to run to completion?
 - Can use the same techniques, we discussed in Chapter 3
 - Receding horizon
 - Sampling
 - Subgoaling
 - Iterative Deepening



Possibilities for Lookahead (ct'd)

- Full horizon, limited breadth:
 - Look for solution that works for *some* of the outcomes
 - E.g., modify Find-Acyclic-Solution to examine i outcomes of every action
- Iterative broadening:
 - For $i = 1$ by 1 until time runs out
 - Look for a solution that handles i outcomes per action

$T \leftarrow i$ elements
of $\gamma(s, a) \setminus \text{Dom}(\pi)$
 $\text{Frontier} \leftarrow \text{Frontier} \cup T$

```
Find-Acyclic-Solution( $\Sigma, s_0, S_g$ )
   $\pi \leftarrow \emptyset$ 
   $\text{Frontier} \leftarrow \{s_0\}$ 
  for every  $s \in \text{Frontier} \setminus S_g$  do
     $\text{Frontier} \leftarrow \text{Frontier} \setminus \{s\}$ 
    if Applicable( $s$ ) =  $\emptyset$  then
      return failure
    nondeterministically choose  $a \in \text{Applicable}(s)$ 
     $\pi \leftarrow \pi \cup (s, a)$ 
     $\text{Frontier} \leftarrow \text{Frontier} \cup (\gamma(s, a) \setminus \text{Dom}(\pi))$ 
    if has-loops( $\pi, s, \text{Frontier}$ ) then
      return failure
  return  $\pi$ 
```

Safely Explorable Domains

- **Safely explorable** domain
 - For every state s , at least one goal state is reachable from s
- Suppose
 - We use Lookahead-Partial-Plan or FS-Replan in a safely explorable domain
 - Lookahead never returns failure
 - No “unfair” executions
- Then we will eventually reach a goal
- What would happen if we just chose a random action each time?

Min-Max LRTA*

Assumes each action
has cost 1
Can easily be modified
to use cost $\neq 1$

Min-Max-LRTA* (Σ, s_0, S_g)

$s \leftarrow s_0$

while $s \notin S_g$ and $\text{Applicable}(s) \neq \emptyset$ **do**

$a \leftarrow \text{argmin}_{a \in \text{Applicable}(s)} \max_{s' \in \gamma(s,a)} h(s')$

$h(s) \leftarrow \max\{h(s), 1 + \max_{s' \in \gamma(s,a)} h(s')\}$

perform action a

$s \leftarrow$ the current state

- Loop

- choose an action a that (according to h) has optimal worst-case cost

- Update $h(s)$ to use a 's worst-case cost
- Perform a

- In safely explorable domains with no “unfair” executions, guaranteed to reach a goal

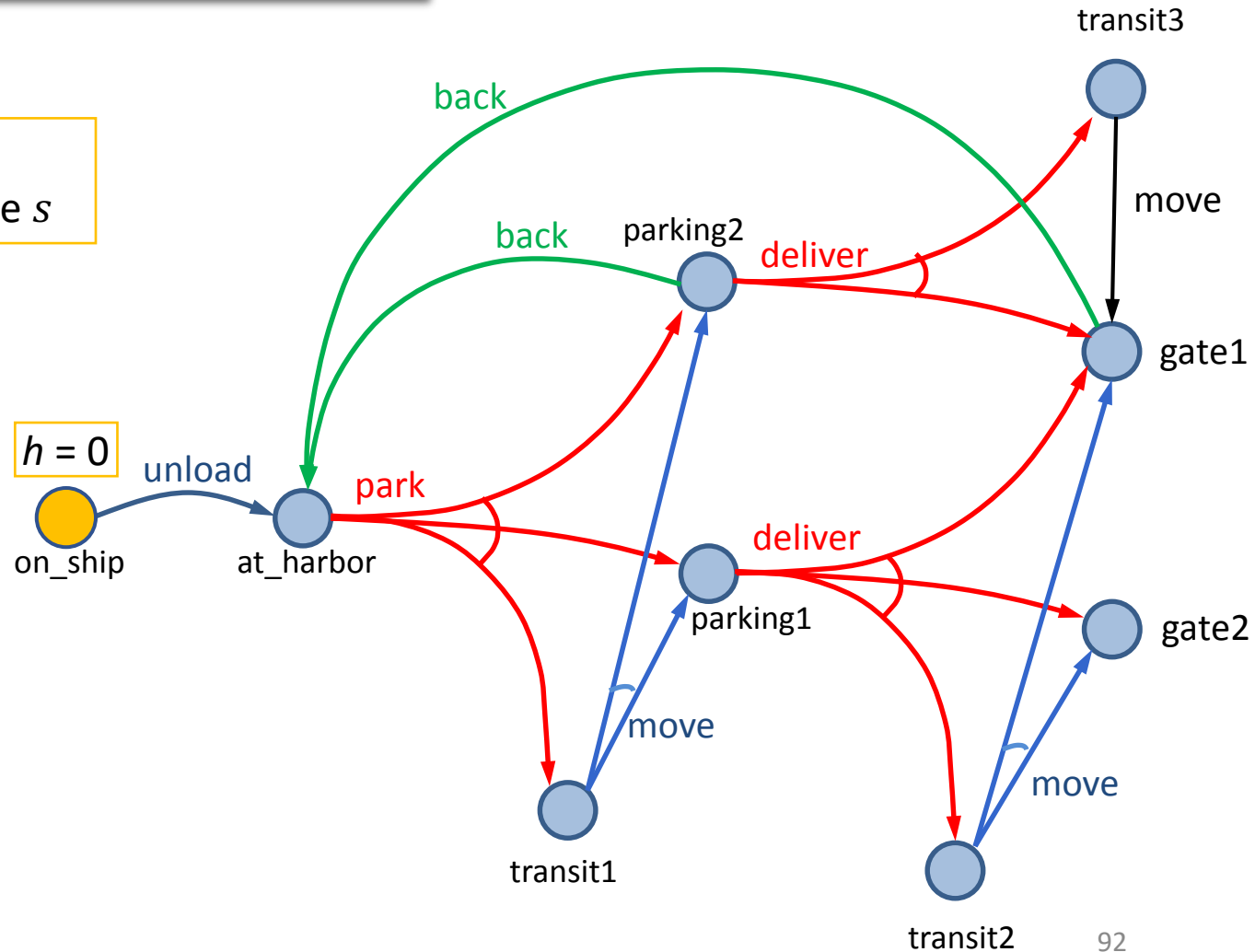
Min-Max-LRTA* (Σ, s_0, S_g)

$s \leftarrow s_0$

```
while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do  
   $a \leftarrow \text{argmin}_{a \in \text{Applicable}(s)} \max_{s' \in \gamma(s,a)} h(s')$   
   $h(s) \leftarrow \max\{h(s), 1 + \max_{s' \in \gamma(s,a)} h(s')\}$   
  perform action  $a$   
   $s \leftarrow$  the current state
```

Example

Suppose that initially,
 $h(s) = 0$ for every state s

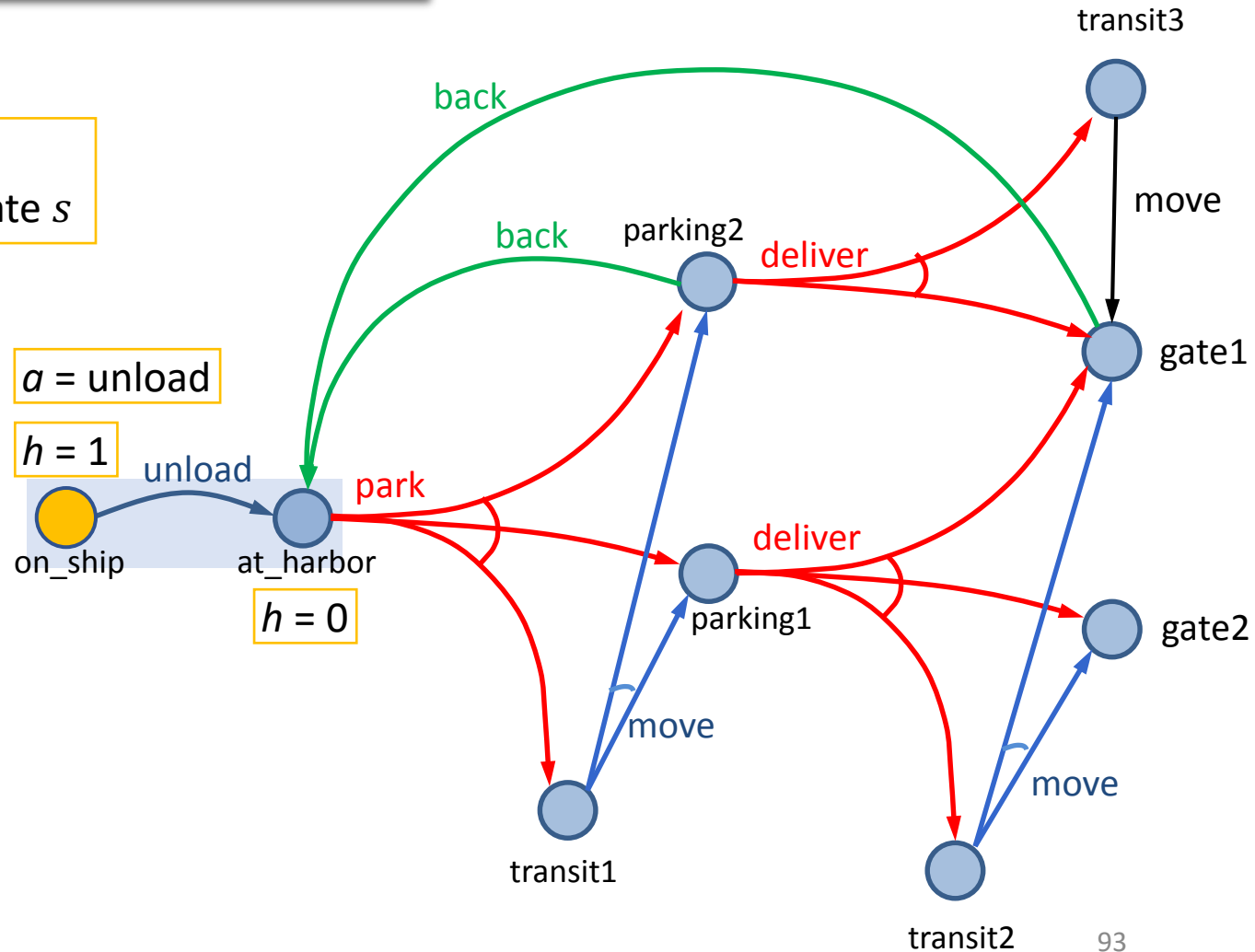


Min-Max-LRTA* (Σ, s_0, S_g)

$s \leftarrow s_0$

```
while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do  
   $a \leftarrow \text{argmin}_{a \in \text{Applicable}(s)} \max_{s' \in \gamma(s,a)} h(s')$   
   $h(s) \leftarrow \max\{h(s), 1 + \max_{s' \in \gamma(s,a)} h(s')\}$   
  perform action  $a$   
   $s \leftarrow$  the current state
```

Suppose that initially,
 $h(s) = 0$ for every state s



Example

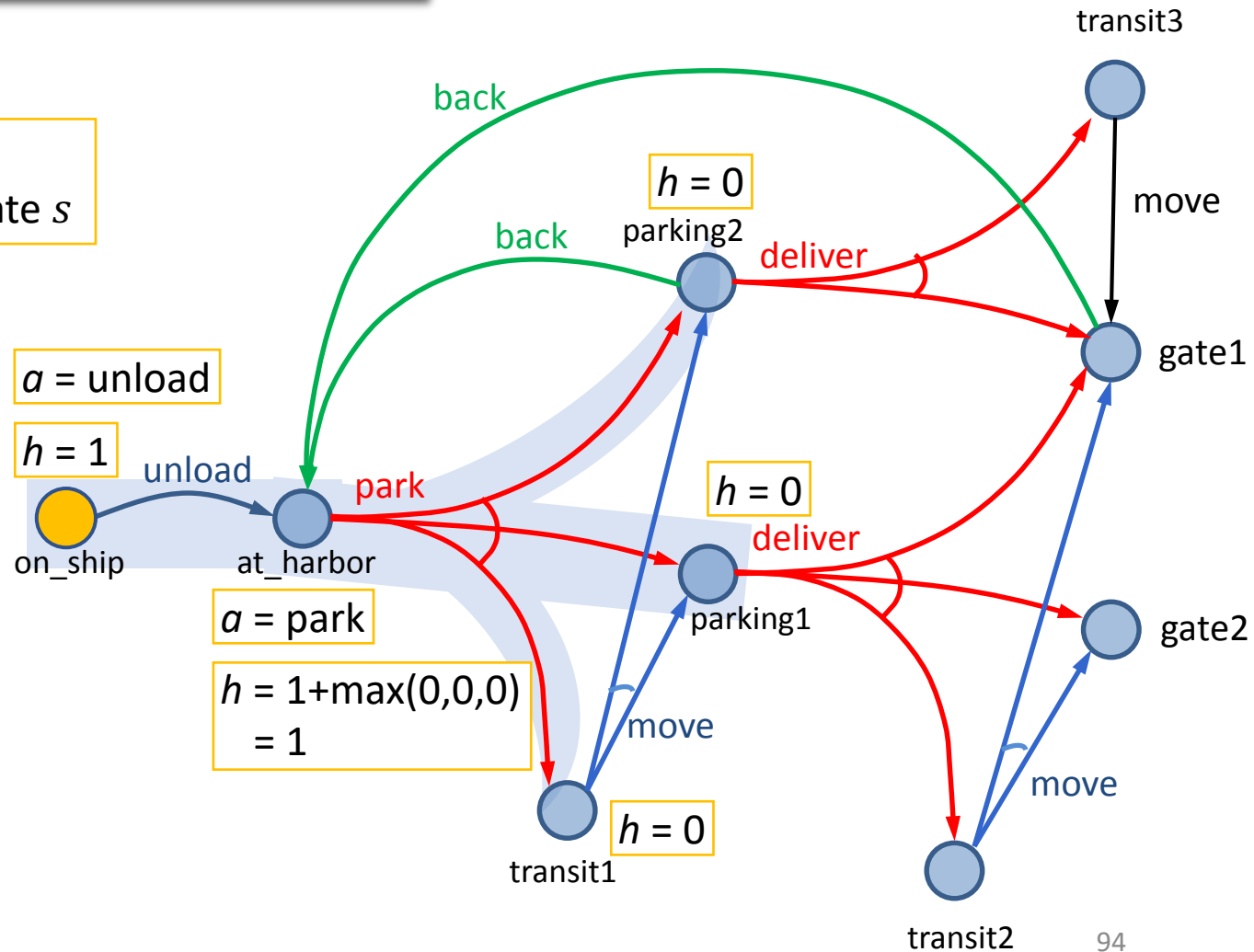
Min-Max-LRTA* (Σ, s_0, S_g)

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```
while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do  
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   $h(s) \leftarrow \max\{h(s), 1 + \max_{s' \in \gamma(s,a)} h(s')\}$   
  perform action  $a$   
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```

Example

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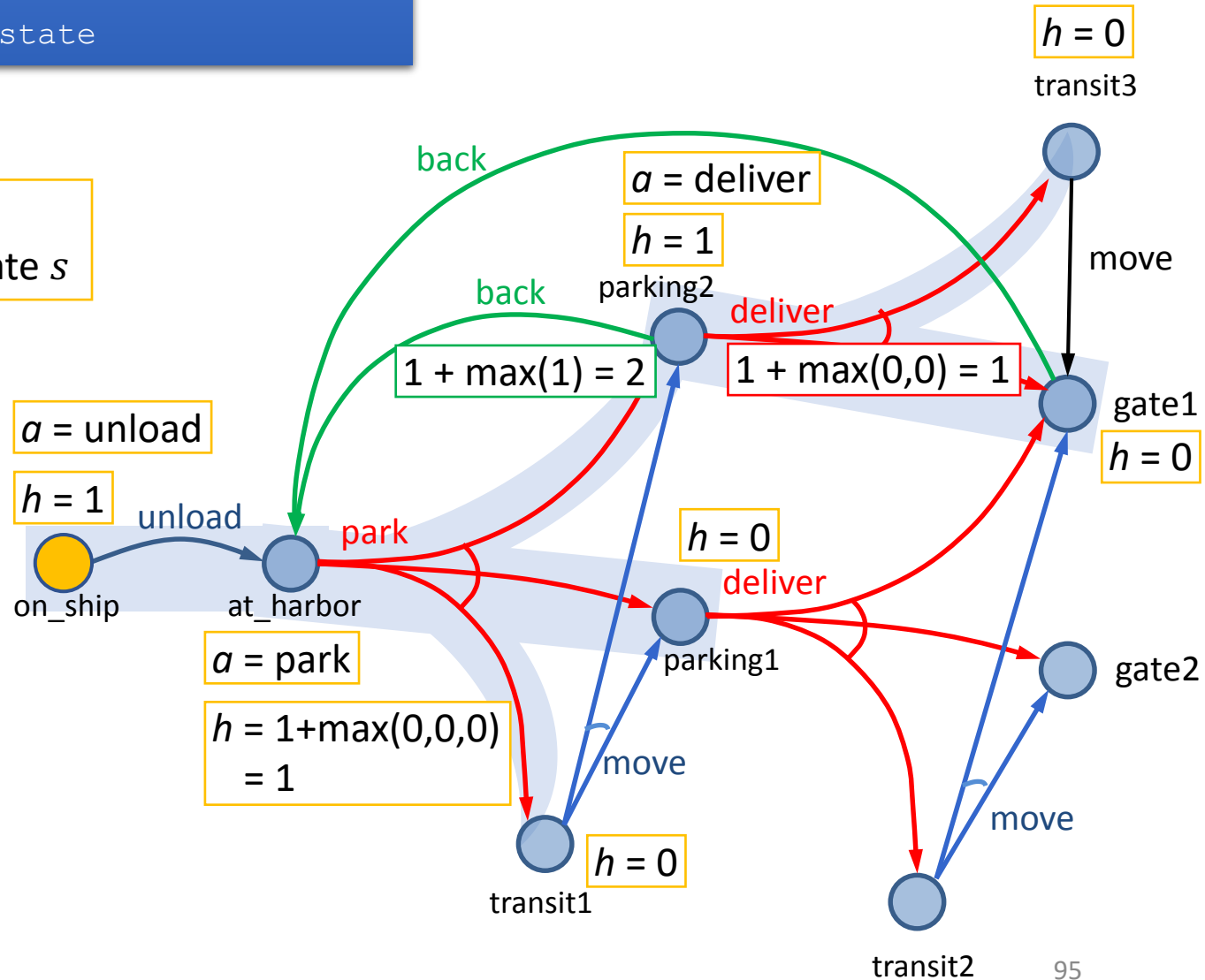


Min-Max-LRTA* (Σ, s_0, S_g)

$s \leftarrow s_0$

```
while  $s \notin S_g$  and  $\text{Applicable}(s) \neq \emptyset$  do  
   $a \leftarrow \text{argmin}_{a \in \text{Applicable}(s)} \max_{s' \in \gamma(s,a)} h(s')$   
   $h(s) \leftarrow \max\{h(s), 1 + \max_{s' \in \gamma(s,a)} h(s')\}$   
  perform action  $a$   
   $s \leftarrow$  the current state
```

Suppose that initially,
 $h(s) = 0$ for every state s



Intermediate Summary

- Online approaches
 - Lookahead-partial-plan
 - Adaptation of Run-Lazy-Lookahead
 - FS-replan
 - Adaptation of Run-Lookahead
- Ways to do the lookahead
 - Full breadth with limited depth
 - iterative deepening
 - Full depth with limited breadth
 - iterative broadening
 - Convergence in safely explorable domains
- Min-Max-LRTA*

Can also adapt
Run-Concurrent-Lookahead

Can put bounds on both
depth and breadth

Outline per the Book

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5.5 Determinisation Techniques

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- Planning for safe solutions by determinisation

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- Lookahead by Determinisation
- Lookahead with a bounded number of steps

⇒ Next: Making Simple Decisions