Intelligent Agents Topic Analysis: LDA

Ralf Möller Universität zu Lübeck Institut für Informationssysteme



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Summary and Agenda

- IR Agents
 - Task/goal: Information retrieval
 - Agents visit document repositories and returns doc recommendations
 - Means:
 - Vector space (bag-of-words)
 - Dimension reduction (LSI)

Non-standard Databases and Data Mining

- Probability based retrieval (binary)
 - Formal Foundation of TF.IDF
- Today: Language models with dimension reduction
 - Latent Dirichlet Allocation (LDA): Topic Models
- Soon:
 - What agents can take with them
 - What agents leave at the repository (win-win)



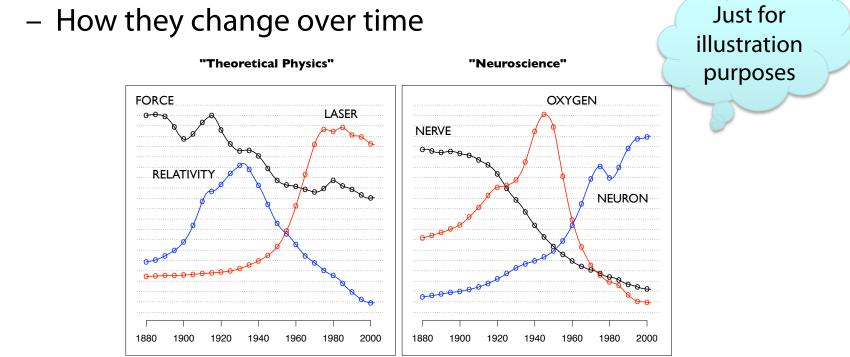
Acknowledgments

Ramesh M. Nallapati presentation on Generative Topic Models for Community Analysis & Sina Miran presentation on Probabilistic Latent Semantic Indexing (PLSI) & David M. Blei presentation on Probabilistic Topic Models



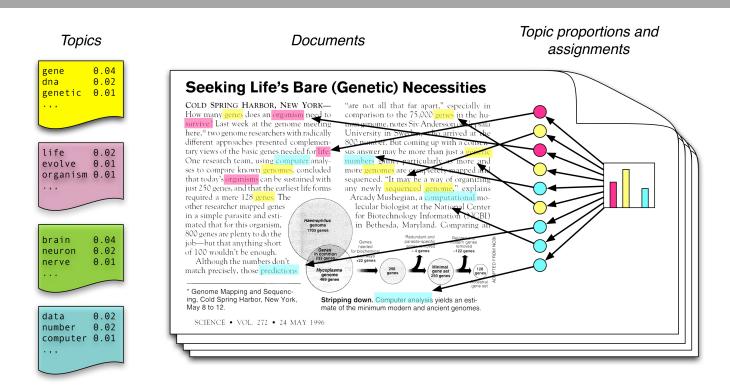
Topic Models

- Statistical methods that analyze the words of texts in order to:
 - Discover the themes that run through them (topics)
 - How those themes are connected to each other





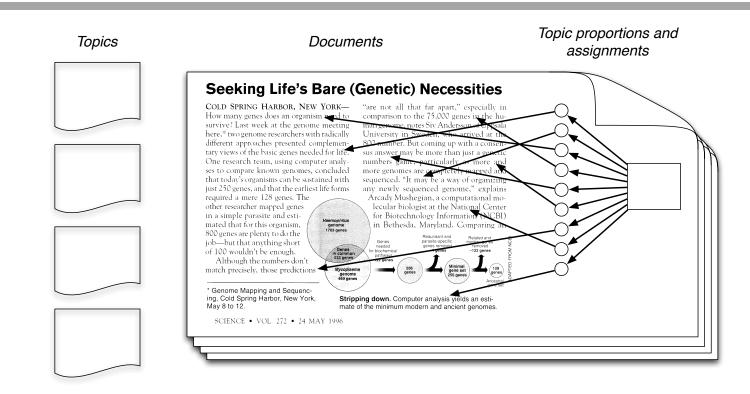
Topic Modeling Scenario



- Each topic is a distribution over words
- Each document is a mixture of corpus-wide topics
- Each word is drawn from one of those topics



Topic Modeling Scenario



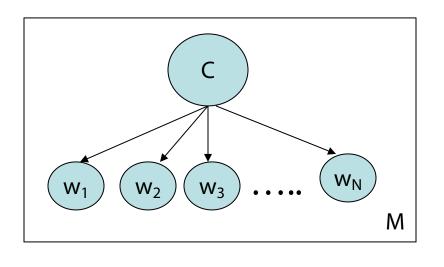
- In reality, we only observe the documents
- The other structures are hidden variables
- Topic modeling algorithms infer these variables from data



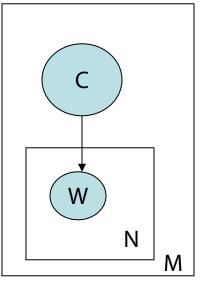
Plate Notation

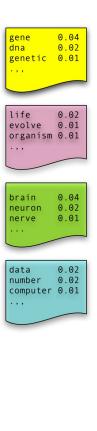
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- Naïve Bayes Model: Compact representation
 - C = topic/class (name for a word distribution)
 - N = number of words in document
 - W_i one specific word in corpus
 - M documents, W now words in documents



Idea: Generate doc from P(W, C)





Generative vs. Descriptive Models

- Generative models: Learn P(x, y)
 - Tasks:
 - Predict (infer) new data
 - Transform P(x,y) into P(y | x) for classification
 - Advantages
 - Assumptions and model are explicit
 - Use well-known algorithms
- Descriptive models: Learn P(y | x)
 - Task: Classify data
 - Advantages

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- Fewer parameters to learn
- Better performance for classification

Input: Bayesian network

 $X = \{X_1, \dots, X_N\}, N- #nodes, T - # samples$ Output: T samples

Process nodes in topological order – first process the ancestors of a node, then the node itself:

- 1. For t = 0 to T
- $2. \quad For i = 0 to N$
- 3. $X_i \leftarrow \text{sample } x_i^t \text{ from } P(x_i | pa_i)$

M. Henrion, "Propagating uncertainty in Bayesian networks by probabilistic logic sampling", Uncertainty in AI, pp. = 149-163, **1988**



What does it mean to sample x_i^t from $P(X_i | pa_i)$?

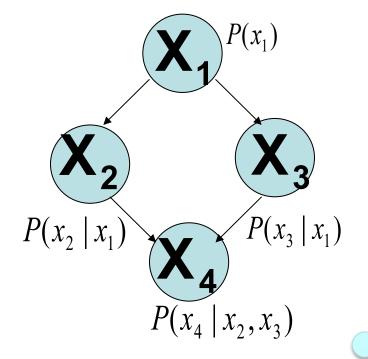
- Assume $Dom(X_i) = \{0,1\}$
- Assume $P(X_i | pa_i) = (0.3, 0.7)$



Draw a random number **r** from [0,1]
 If **r** falls into [0,0.3], set X_i = 0
 If **r** falls into (0.3,1], set X_i=1



Forward Sampling (Example)



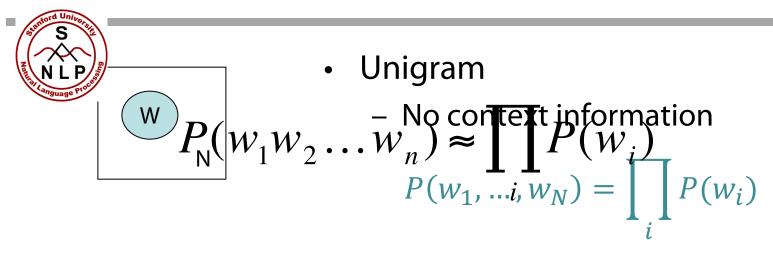
Evidence : $X_3 = 0$

// generate sample k 1. Sample x_1 from $P(x_1)$ 2. Sample x_2 from $P(x_2 | x_1)$ 3. Sample x_3 from $P(x_3 | x_1)$ 4. If $x_3 \neq 0$, reject sample and start from 1, otherwise 5. sample x_4 from $P(x_4 | x_2, x_3)$

Rejection sampling (rather inefficient)



Earlier Topic Models: Topics Known



fifth, an, of, futures, the, an, incorporated, a, a, the, inflation, most, dollars, quarter, in, is, mass

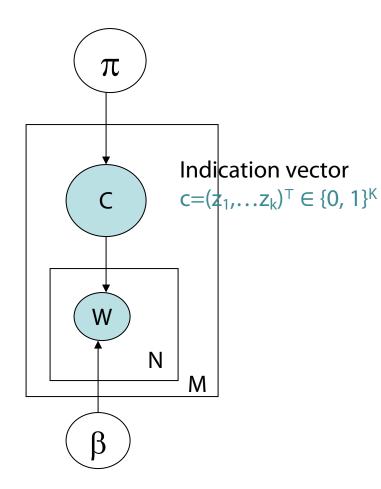
thrift, did, eighty, said, hard, 'm, july, bullish

that, or, limited, the

Automatically generated sentences from a unigram model



Multinomial Naïve Bayes





- How to specify Domain(C)?
 - Domain(C) = $\{1, 2, ..., k\}$ or
 - Domain(C) = $\{0, 1\}^k$
- How to specify $P(c_d)$?
 - Define a table

	P(C)
1	p_1
•••	•••
К	p_K

- or use parameterized distribution $\pi = (p_1, ..., p_K)$

• $P(C=c|\pi) = \prod_{k=1}^{K} \pi_k^{z_k}$

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Recap: Binomial Distribution

- Describes the number of successes in a series of independent trials with two possible outcomes "success" or "no success"
- n = #trials

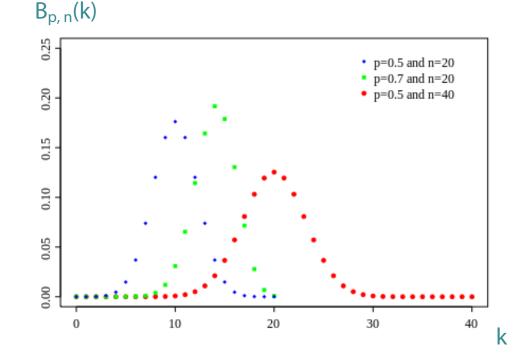
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- p = #successful trials / n
- Description of frequency of having exactly k successful trials as a function

$$\mathsf{B}_{\mathsf{p,n}}(\mathsf{k}) = \binom{n}{k} p^k (1-p)^{n-k}$$

- It holds: $\sum_{i=0} B_{p,n}(i) = 1$
- If n=1: Bernoulli distribution



Multinomial Distribution Mult(n | π)

- Generalization of binomial distribution
 - K possible outcomes instead of 2 (success or no success)
 - Probability mass function
 - n = number of trials
 - $x_j \in \{0, 1\}$ a count for how often class j occurs $\sum_{i=1}^k x_i = n$
 - p_i = probability of class j occurring $Mult(x_1, \dots, x_K; p_1, \dots, p_K) = \frac{\Gamma(\sum_i x_i + 1)}{\prod_i \Gamma(x_i + 1)} \prod_{i=1}^{K} p_i^{x_i}$

- Here, the input to $\Gamma(\cdot)$ is a positive integer, $\Gamma(n) = (n-1)!$
- If n=1: called categorial distribution ("multinoulli")
 - Often written $Mult(.; p_1, ..., p_K)$ or $Mult(. | p_1, ..., p_K)$
 - Generates a one-hot vector

Sampling

- A variable value a can be sampled from a discrete distribution π = (p₁, ..., p_K)
- Notation: a ~ Mult($| \pi \rangle$
- Generate random number *x* from (0, 1]
- Find $l \in \{1, 2, ..., k\}$ such that $\sum_{i=1}^{l-1} p_i < x \le \sum_{i=1}^{l} p_i$

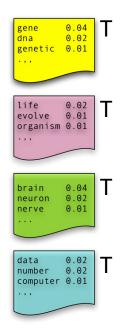
One-hot vector to be generated with position probability of indicator controlled by π

• Return $(z_1, ..., z_K)$ such that $z_l = 1$ and $z_i = 0$ für $i \neq l$



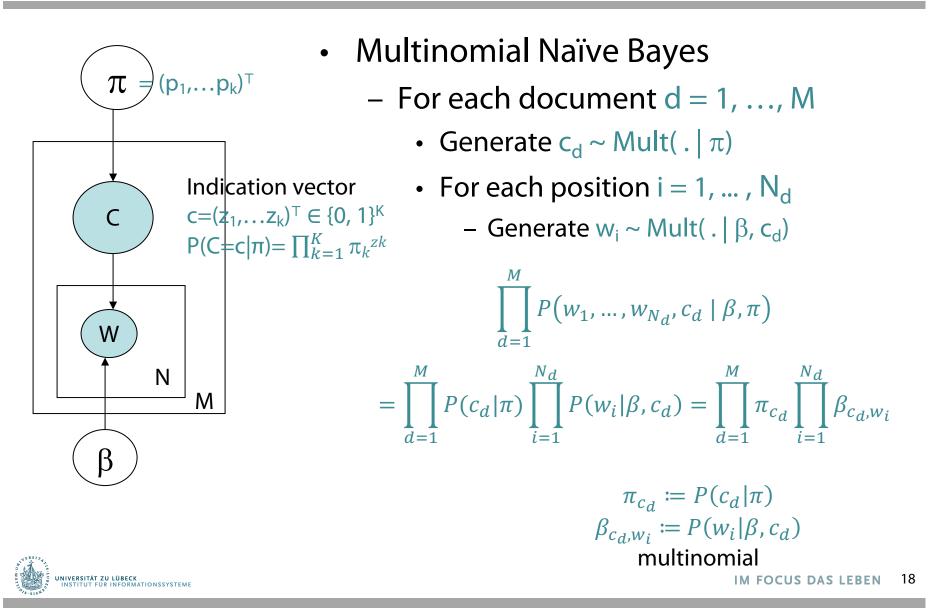
Multinomial with Matrices

- Let β be a $K \times V$ matrix (V vocabulary size), each row denotes a word distribution of a topic
- Select row k before applying multinomial:
 - Notation: Mult(. $|\beta_k$) or Mult(. $|\beta, k$) or Mult(. $|k, \beta$)

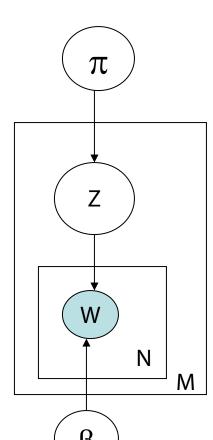




Mixture of Unigrams: Known Topics



Mixture of Unigrams: Unknown Topics



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- Topics/classes are hidden
 - Joint probability of words and classes

$$\prod_{d=1}^{M} P(w_1, \dots, w_{N_d}, z_d \mid \beta, \pi) = \prod_{d=1}^{M} \pi_{z_d} \prod_{i=1}^{N_d} \beta_{z_d, w_i}$$

Sum over topics (K = number of topics)

$$\prod_{d=1}^{M} P(w_1, \dots, w_{N_d} | \beta, \pi) = \prod_{d=1}^{M} \sum_{k=1}^{K} \pi_{Z_k} \prod_{i=1}^{N_d} \beta_{Z_k, w_i}$$

Kamal Nigam, Andrew Kachites Mccallum, Sebastian Thrun & Tom Mitchell, Learning to Classify Text from Labeled and Unlabeled Documents, Proc. AAAI 98, Pages 792–799, **1998**.

Kamal Nigam, Andrew Kachites Mccallum, Sebastian Thrun & Tom Mitchell Text Classification from Labeled and Unlabeled Documents using EM Journal of Machine Learning volume 39, pages 103–134, **2000**.

$$\pi_{z_k} \coloneqq P(z_k | \pi)$$

$$\beta_{z_k, w_i} \coloneqq P(w_i | \beta, z_k)$$

Mixture of Unigrams: Learning

• Learn parameters π and β $argmax_{\beta\pi}\prod_{d=1}^{M} P(w_1, ..., w_{N_d} | \beta, \pi)$

$$P(w_1, ..., w_{N_d} | \beta, \pi) = \sum_{k=1}^{K} \pi_{z_k} \prod_{i=1}^{N_d} \beta_{z_k, w_i}$$

Convex

• Use likelihood

$$\sum_{d=1}^{M} \log P(w_1, \dots, w_{N_d} | \beta, \pi) = \sum_{d=1}^{M} \log \sum_{k=1}^{K} \pi_{z_k} \prod_{i=1}^{N_d} \beta_{z_k, w_i}$$

Solve

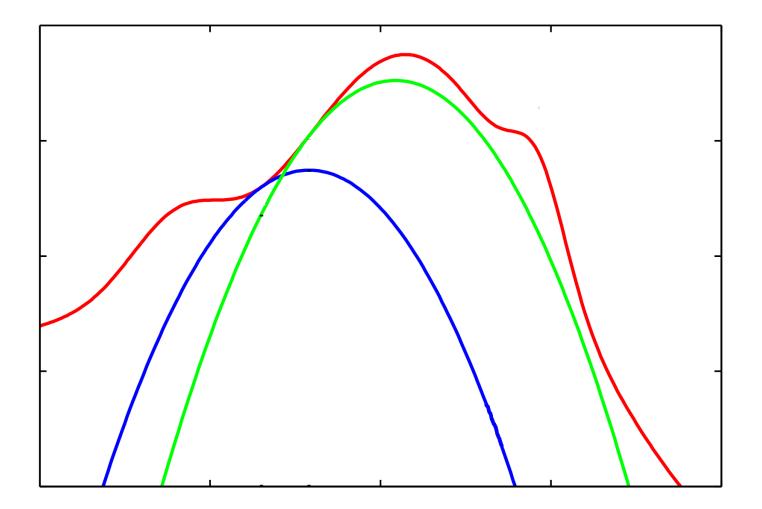
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- $argmax_{\beta\pi}\sum_{d=1}^{M}\log\sum_{k=1}^{K}\pi_{z_{k}}\prod_{i=1}^{N_{d}}\beta_{z_{k},w_{i}}$
- Not a concave/convex function
- Note: a non-concave/non-convex function is not necessarily convex/concave
- Possibly no unique max, many saddle or turning points No easy way to find roots of derivative

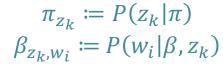
Concave

Trick: Optimize Lower Bound





Mixture of Unigrams: Learning



a, b

distribution

The problem

$$argmax_{\beta\pi}\sum_{d=1}^{M}\log\sum_{k=1}^{K}\pi_{z_{k}}\prod_{i=1}^{N_{d}}\beta_{z_{k},w_{i}}$$

- Optimize w.r.t. each document
- **Derive lower bound**

Derive lower bound vectors

$$\log \sum_{i} \gamma_{i} x_{i} \geq \sum_{i} \gamma_{i} \log x_{i} \text{ where } \gamma_{i} \geq 0 \land \sum_{i} \gamma_{i} = 1 \qquad \text{Jensen's inequality} \\ \log(\mathbf{a} \cdot \mathbf{b}) \geq \mathbf{a} \cdot \log \mathbf{b}$$

 $H(\gamma)$

$$x_{i} = \log \sum_{i} \gamma_{i} \frac{x_{i}}{\gamma_{i}} \ge \sum_{i} (\gamma_{i} \log x_{i} - \gamma_{i} \log \gamma_{i})$$

Entropy of γ_{i}
Sometimes

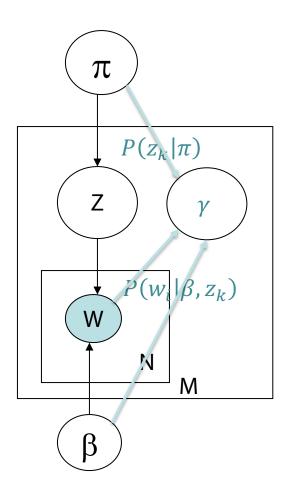
$$\log \sum_{k=1}^{K} \pi_{z_{k}} \prod_{i=1}^{N_{d}} \beta_{z_{k},w_{i}} \ge \sum_{k=1}^{K} \left(\gamma_{k} \log(\pi_{z_{k}} \prod_{i=1}^{N_{d}} \beta_{z_{k},w_{i}}) \right) + H(\gamma)$$



log

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The model



$$\pi_{z_k} \coloneqq P(z_k | \pi)$$

$$\beta_{z_k, w_i} \coloneqq P(w_i | \beta, z_k)$$



Mixture of Unigrams: Learning

Optimization problem for each document

 $argmax_{\beta\pi}\sum_{k=1}^{K}\left(\gamma_k\log(\pi_{z_k}\prod_{i=1}^{N_d}\beta_{z_k,w_i})\right)+H(\gamma)$

Convex? Concave?

- We have introduced a new latent variable γ to approximate the original functional to be optimized
- Each document is assumed to be associated with a latent variable $\gamma \in [0,1]^{K}$, $\Sigma_{k} \gamma_{k} = 1$ independent of other random variables
- Can be seen as a class in the new space $\gamma_k, \pi_{z_k}, \beta_{z_k, w_i}$



Mixture of Unigrams: Learning

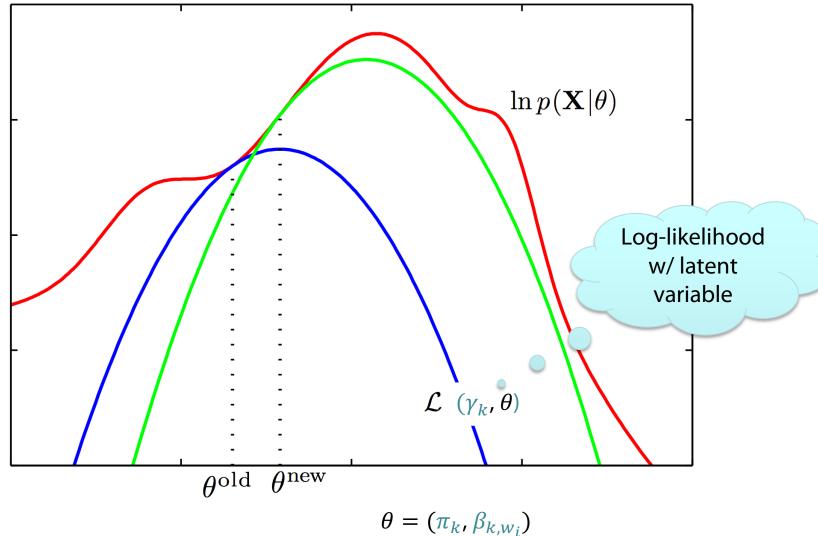
• New optimization problem:

$$argmax_{\beta\pi}\sum_{k=1}^{K} \left(\gamma_k \log(\pi_{z_k} \prod_{i=1}^{N_d} \beta_{z_k, w_i})\right) + H(\gamma)$$

- Solution: Expectation Maximization
 - Iterative algorithm to find local optimum
 - Guess values of γ_k , π_{z_k} , β_{z_k,w_i}
 - Compute $\gamma_k = P(\gamma_k | \pi_{z_k}, \beta_{z_k, w_i})$ according to model
 - Use maximum-likelihood estimation to optimize π_{Z_k} , β_{Z_k,w_i} until no further improvement
- Guaranteed to maximize a lower bound on the loglikelihood of the observed data
- Use π_{z_k} , β_{z_k,w_i} to estimate $P(z_k|\pi)$, $P(w_i|\beta, z_k)$, respectively

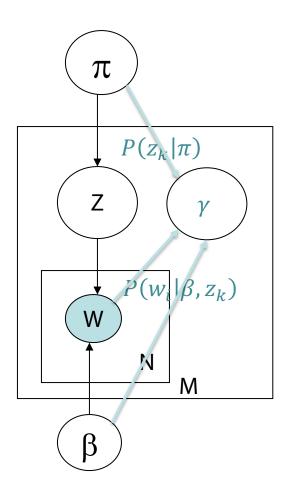


Graphical Idea of the EM Algorithm





The model



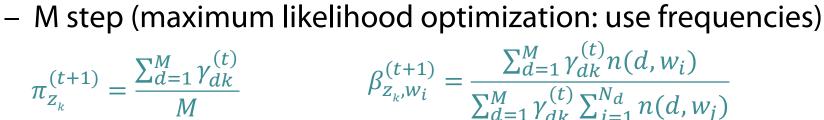
$$\pi_{z_k} \coloneqq P(z_k | \pi)$$

$$\beta_{z_k, w_i} \coloneqq P(w_i | \beta, z_k)$$





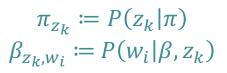
 $n(d, w_i)$ number of times word w_i occurs in document d



$$\gamma_{k}^{(t+1)} = \frac{\gamma_{k}^{(t)} \pi_{Z_{k}}^{(t)} \prod_{i=1}^{N_{d}} \beta_{Z_{k},w_{i}}^{(t)}}{\sum_{j=1}^{K} \gamma_{Z_{dj}}^{(t)} \pi_{Z_{j}}^{(t)} \prod_{i=1}^{N_{d}} \beta_{Z_{j},w_{i}}^{(t)}} \qquad \qquad \text{Independence}$$
assumption

– E step (compute $\gamma_k = P(\gamma_k | \pi_{z_k}, \beta_{z_k, w_i})$)

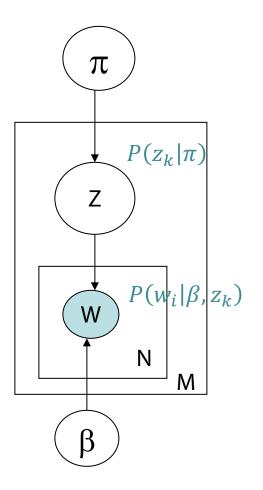
Mixture of Unigrams: Learning





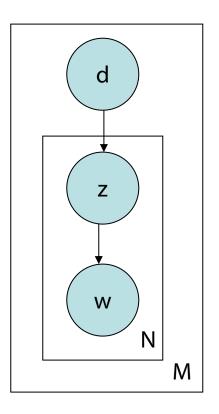
Back to Topic Modeling Scenario

- Documents are associated with a single topic
- Words do not depend on context
 - Bag-of-words model





Probabilistic LSI



- Select a document d with probability P(d)
- For each word of d in the training set
 - Choose a topic z with probability $P(z \mid d)$
 - Generate a word with probability P(w | z)

$$P(d, w_i) = P(d) \sum_{k=1}^{K} P(w_i | z_k) P(z_k | d)$$

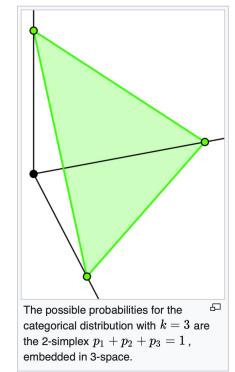
Documents can have multiple topics



Thomas Hofmann, Probabilistic Latent Semantic Indexing, Proceedings of the 22nd Annual International <u>SIGIR</u> Conference on Research and Development in Information Retrieval (SIGIR-99), **1999**

Prior Distribution for Topic Mixture

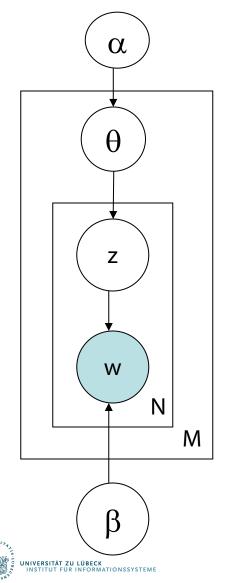
- Goal: topic mixture proportions for each document drawn from some distribution
 - Distribution on multinomials (k-tuples of non-negative numbers that sum to one)
- The space of all of these multinomials can be interpreted geometrically as a (k-1)-simplex
 - K-1 independent values
 - Simplex = Generalization of a triangle to (k-1) dimensions
- Criteria for selecting our prior:
 - It needs to be defined for a (k-1)-simplex
 - Should have nice properties





[Wikipedia]

Model – Parameters



Proportions parameter

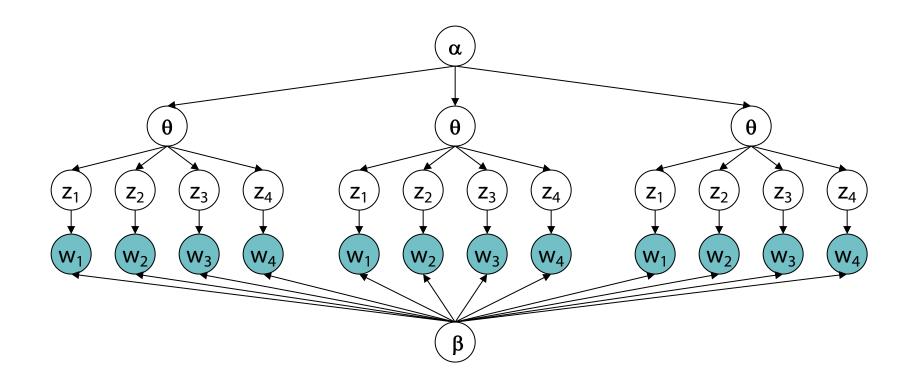
- (k-dimensional vector of real numbers)
- ← Per-document topic distribution (*k*-dimensional vector of probabilities summing up to 1)
- ← Per-word topic assignment (number from 1 to k)

← Observed word

(number from 1 to v, where v is the number of words in the vocabulary)

← Word "prior" (v-dimensional)

LDA Model





Latent Dirichlet Allocation

 Document = mixture of topics according to a Dirichlet prior



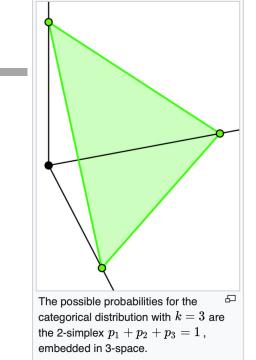
D. Blei, A. Ng, and M. Jordan. Latent Dirichlet Allocation. Journal of Machine Learning Research, 3:993-1022, January **2003**

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Dirichlet Distributions

$$p(\theta|\alpha) = \frac{\Gamma(\sum_{i} \alpha_{i})}{\prod_{i} \Gamma(\alpha_{i})} \prod_{i=1}^{K} \theta_{i}^{\alpha_{i}-1}$$

- Defined over a (k-1)-simplex
 - Takes K non-negative arguments which sum to one.
 - Consequently it is a natural distribution to use over multinomial distributions.

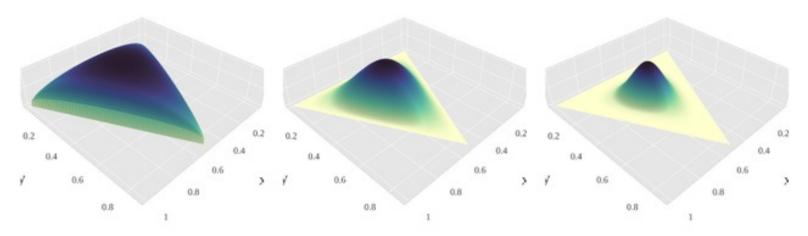


- The Dirichlet parameter α_i can be thought of as a prior count of the ith class

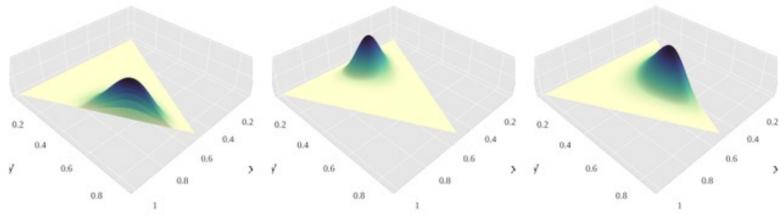
$$Dir(x_{1}, ..., x_{K}; p_{1}, ..., p_{K}) = \frac{\Gamma(\sum_{i} x_{i} + 1)}{\prod_{i} \Gamma(x_{i} + 1)} \prod_{i=1}^{K} p_{i}^{x_{i}}$$



Dirichlet Distribution over a 2-Simplex

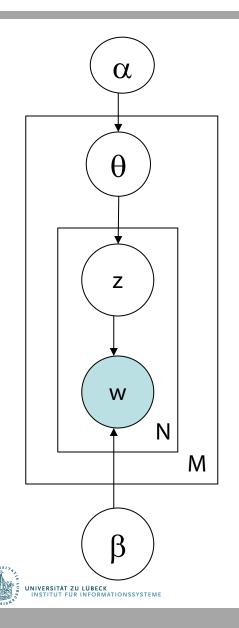


A panel illustrating probability density functions of a few Dirichlet distributions over a 2-simplex, for the following α vectors (clockwise, starting from the upper left corner): (1.3, 1.3, 1.3), (3,3,3), (7,7,7), (2,6,11), (14, 9, 5), (6,2,6). [Wikipedia]





LDA Model – Plate Notation



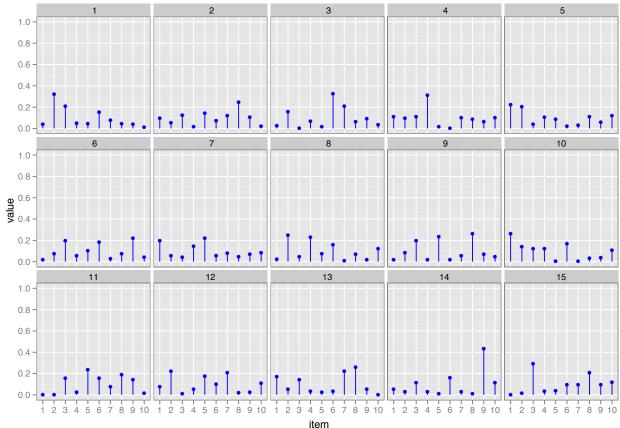
- For each document d,
 - Generate $\theta_d \sim \text{Dirichlet}(\alpha)$
 - For each position $i = 1, ..., N_d$
 - Generate a topic $z_i \sim Mult(\cdot | \theta_d)$
 - Generate a word $w_i \sim Mult(\cdot | z_{i'}\beta)$

$$P(\beta, \theta, z_1, \dots, z_{N_d}, w_1, \dots, w_{N_d})$$

= $\prod_{d=1}^{M} P(\theta_d | \alpha) \prod_{i=1}^{N_d} P(z_i | \theta_d) P(w_i | \beta, z_i)$

Corpus-level Parameter α (uniform: $\alpha_{i} = \alpha_{j}$)

- Let $\alpha = 1$
- Per-document topic distribution: K = 10, D = 15

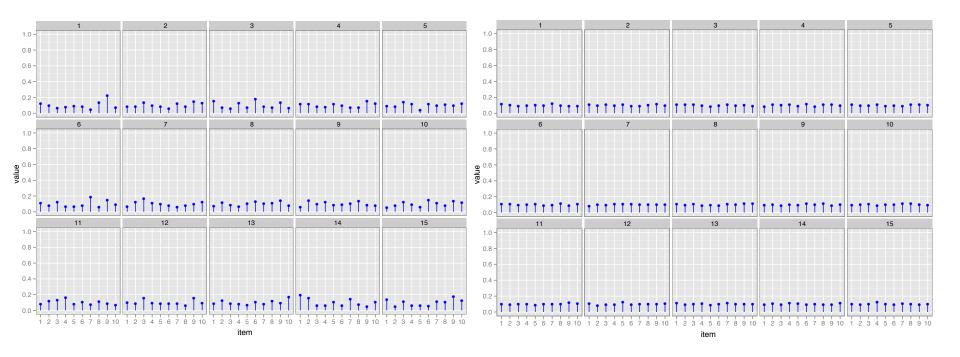




Corpus-level Parameter *α*

• $\alpha = 10$

• $\alpha = 100$

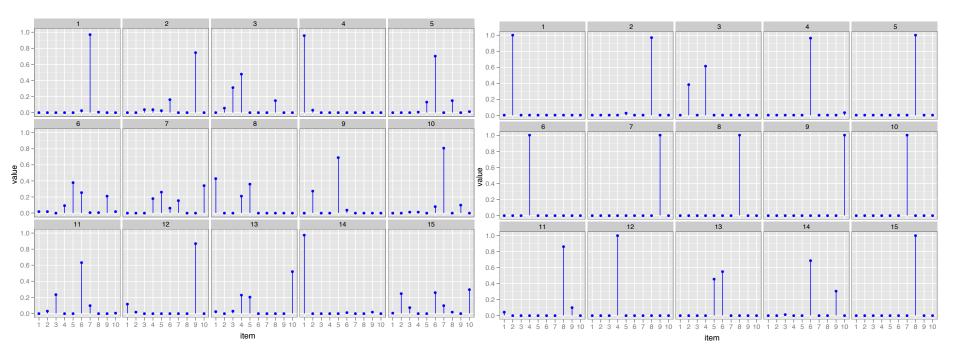




Corpus-level Parameter α

• $\alpha = 0.1$

• $\alpha = 0.01$

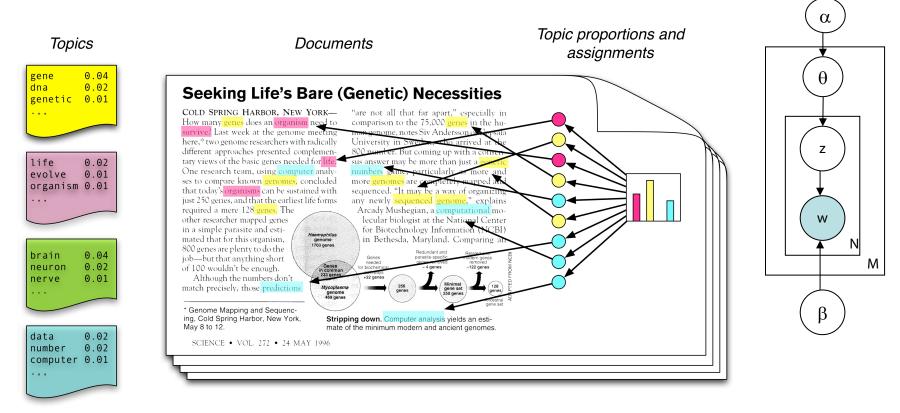




Back to Topic Modeling Scenario

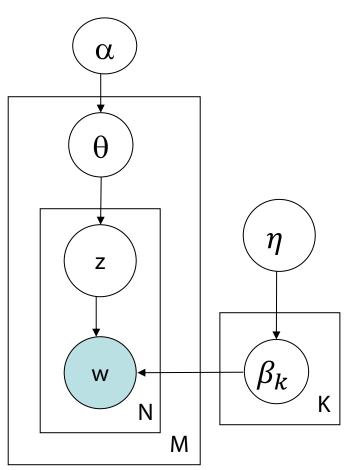
What are the words' topics and word distribs of topics?

- $P(\beta, \theta, \boldsymbol{z} | \boldsymbol{w}, \alpha)$





Topic-specific Words: "Smoothed" LDA Model



- Give a different word distribution to each topic
 - β is $K \times V$ matrix (V vocabulary size), each row denotes word distribution of a topic
- For each document d
 - Choose $\theta_d \sim \text{Dirichlet}(\alpha)$
 - Choose $\beta_k \sim \text{Dirichlet}(\eta)$
 - For each position $i = 1, ..., N_d$
 - Generate a topic $z_k \sim Mult(\cdot \mid \theta_d)$
 - Generate a word $w_i \sim Mult(\cdot | z_{k'}\beta_{zk})$

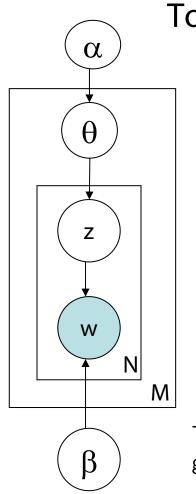


But why does LDA actually work?

- Trade-off between two goals
 - 1. For each document, allocate its words to as few topics as possible
 - 2. For each topic, assign high probability to as few terms as possible
- These goals are at odds
 - Putting a document in a single topic makes #2 hard:
 All of its words must have non-negligible probability under that topic
 - Putting very few words in each topic makes #1 hard:
 To cover a document's words, it must assign many topics to it
- Trading off these goals finds groups of tightly co-occurring words



Query Answering Problem (non-smoothed version)



To which topics does a given document belong?

$$P(\theta, \mathbf{z} | \mathbf{w}, \alpha, \beta) = \frac{P(\theta, \mathbf{z}, \mathbf{w} | \alpha, \beta)}{P(\mathbf{w} | \alpha, \beta)}$$

$$P(\theta, \mathbf{z}, \mathbf{w} | \alpha, \beta) = P(\theta | \alpha) \prod_{i=1}^{N} P(z_i | \theta) P(w_i | z_i, \beta)$$

$$P(\mathbf{w} | \alpha, \beta) = \int \sum_{k=1}^{K} P(\mathbf{w}, \theta, \mathbf{z} | \alpha, \beta) \ d\theta = \int \sum_{k=1}^{K} P(\theta | \alpha) \prod_{i=1}^{N} P(z_i | \theta) P(w_i | z_i, \beta) \ d\theta = \int \sum_{k=1}^{K} P(\theta | \alpha) \prod_{i=1}^{N} \sum_{k=1}^{K} \prod_{j=1}^{V} (\theta_k \beta_{kj})^{w_i^j} \ d\theta$$

This not only looks awkward, but is as well *computationally intractable* in general. Coupling between θ and β_{ij} . Solution: *Approximations*.

 $p(\theta | \alpha) = \frac{\Gamma(\sum_{i} \alpha_{i})}{\prod_{i} \Gamma(\alpha_{i})} \prod_{i=1}^{K} \theta_{i}^{\alpha_{i}-1}$



LDA Learning

- Parameter learning:
 - Variational Inference / EM
 - Numerical approximation using lower-bounds
 - Results in biased solutions
 - Convergence has numerical guarantees
 - Gibbs Sampling
 - Stochastic simulation
 - Unbiased solutions
 - Stochastic convergence

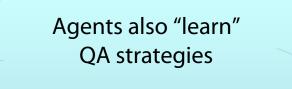
We have a lecture on Approximation Algorithms for Probabilistic Models !



D. Blei, A. Ng, and M. Jordan. Latent Dirichlet Allocation. Journal of Machine Learning Research, 3:993-1022, January **2003**

Back to Agents

- Agents not only use models
- Agents *build* models that are appropriate to fulfil the agents' goals ...
 - ... or maximize the utilities derived from preference structures and goals
- Agents need to *derive approximation algorithms* for query answering on the models they find appropriate





LDA Application: Reuters Data

- Setup
 - 100-topic LDA trained on a 16,000 documents corpus of news articles by Reuters
 - Some standard stop words removed
- Top-7 words from some of the P(w|z)

"Arts"	"Budgets"	"Children"	"Education"
new	million	children	school
film	tax	women	students
show	program	people	schools
music	budget	child	education
movie	billion	years	teachers
play	federal	families	high
musical	year	work	public



LDA Application: Reuters Data

Result

Again: "Arts", "Budgets", "Children", "Education".

The William Randolph Hearst Foundation will give \$1.25 million to Lincoln Center, Metropolitan Opera Co., New York Philharmonic and Juilliard School. "Our board felt that we had a real opportunity to make a mark on the future of the performing arts with these grants an act every bit as important as our traditional areas of support in health, medical research, education and the social services," Hearst Foundation President Randolph A. Hearst said Monday in announcing the grants.



Measuring Performance

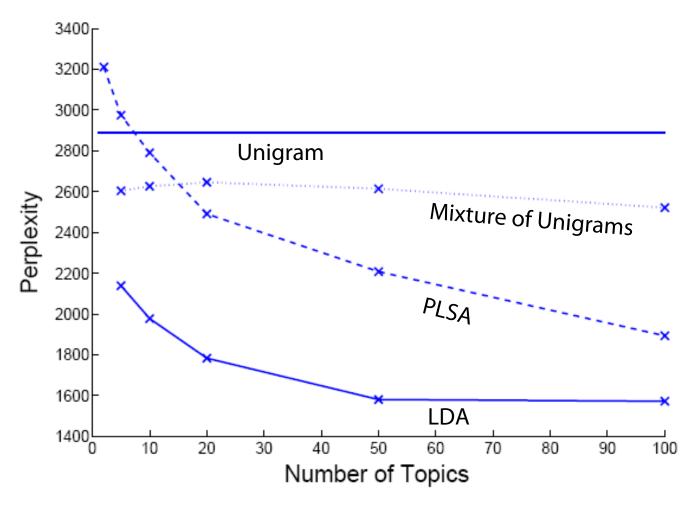
- Perplexity of a probability model
- Describe how well a probability distribution or probability model predicts a sample
 - q: Model of an unknown probability distribution p
 based on a training sample drawn from p
 - Evaluate q by asking how well it predicts a separate test sample x_1, \dots, x_N also drawn from p
 - Perplexity of q w.r.t. sample x_1, \ldots, x_N defined as

 $2^{-\frac{1}{N}\sum_{i=1}^{N}\log_2 q(x_i)}$

- A better model q will tend to assign higher probabilities to $q(x_i)$
 - \rightarrow lower perplexity ("less surprised by sample")



Perplexity of Various Models





Use of LDA

- A widely used topic model (Griffiths, Steyvers, 04)
- Complexity is an issue
- Use in IR:
 - Ad hoc retrieval (Wei and Croft, SIGIR 06: TREC benchmarks)
 - Improvements over traditional LM (and LSI techniques)
 - But no consensus on whether there is any improvement over a relevance model, i.e., model with relevance feedback (relevance feedback part of the TREC tests)

T. Griffiths, M. Steyvers, Finding Scientific Topics. Proceedings of the National Academy of Sciences, 101 (suppl. 1), 5228-5235. **2004**

Xing Wei and W. Bruce Croft. LDA-based document models for ad-hoc retrieval. In *Proceedings of the 29th annual international ACM SIGIR conference on Research and development in information retrieval* (SIGIR '06). ACM, New York, NY, USA, 178-185. **2006**.



TREC=Text REtrieval Conference

Topic modelling

Tomoharu Iwata



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Social annotation services

- Delicious, Flickr, CiteULike, youtube, Last.fm, Technorati, Hatena
- Users can attach annotations freely to objects, and share the annotations.

delicious social bookmarking If's Reed All your stuff in one place. Get to your bookmarks from any computer, anywhere. If your stuff in one place.	Jain Noor Sign In	flickr		Create Your Account Only Like a moment with your Yahari ID Share your photos.
Converte Delicover	HOE INTRO Q	By xdjio 2.641 uploads in the last	minute • 160,129 hings lagged with morning • 2.5	watch the world.
See more Popular bookmarks Watch TV Online - Full Episodes save Watch TV Online - Full Episodes save tv tree onter beenaon votes Het webdesign schetsboek - Webdesign inventis Web Architects save	Popular Tags delign blog video software			
wedanupi design settion grai prec Image: More than a setting to the setting of the	tools music programming webdesign reterence tubriel art	Add George as a contact? Share & stay in touch	الله عنهم عنهم عنهم عنهم عنهم عنهم عنهم عنه	
DevHub • Free Web Hosted Publishing Platform suve 112 webdesign toxing geweignert business platition	web howto jevecript tree linux web2.0 devetopment	Crop, fix, edit	Explore	



Derive content-unrelated annotations

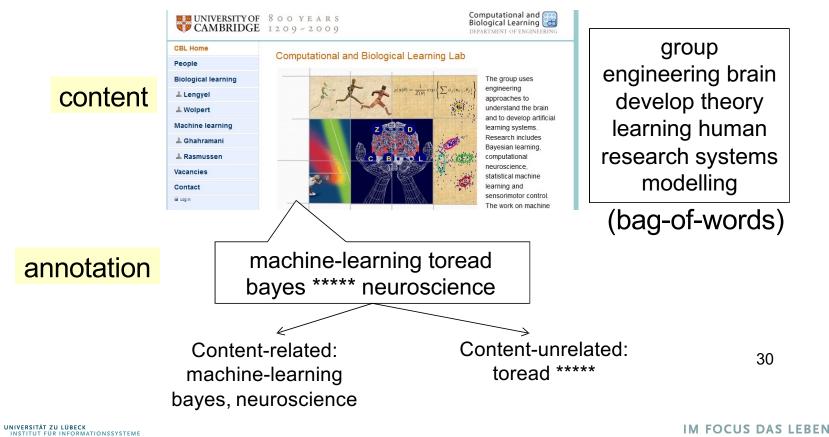
- manufacturer of camera that took the photo – 'nikon', 'canon'
- when they were taken
 - '2008', 'november'
- remind the annotator
 - 'toread'
- qualities
 - 'great', '****'
- ownership



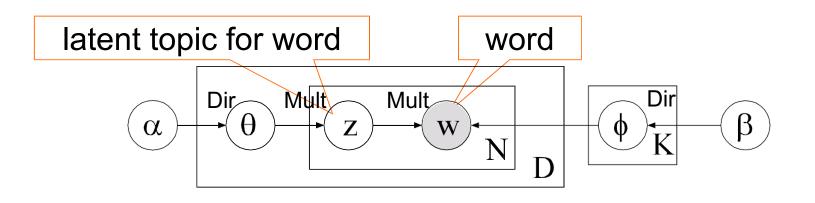
29

Proposed model

- generative model for contents (words) and annotations with relevance based on topic models
- infer relevance to the content for each annotation



Latent Dirichlet allocation

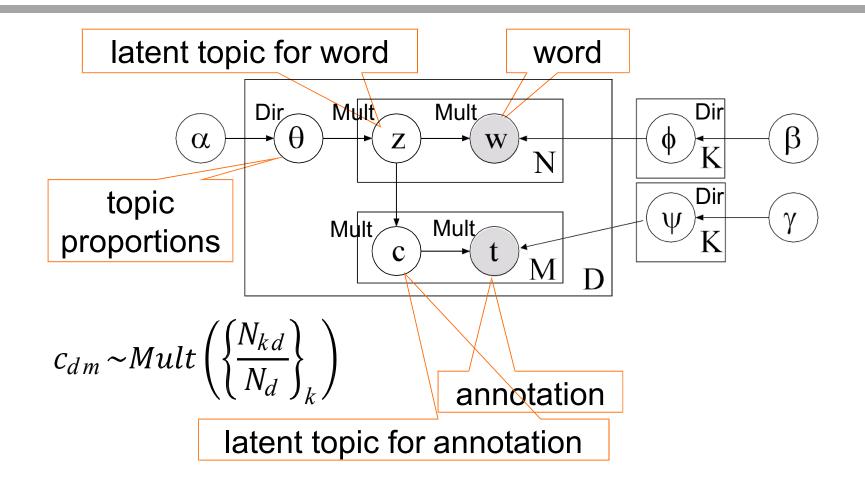


[Blei et. al. Latent Dirichlet Allocation, JMLR2003]



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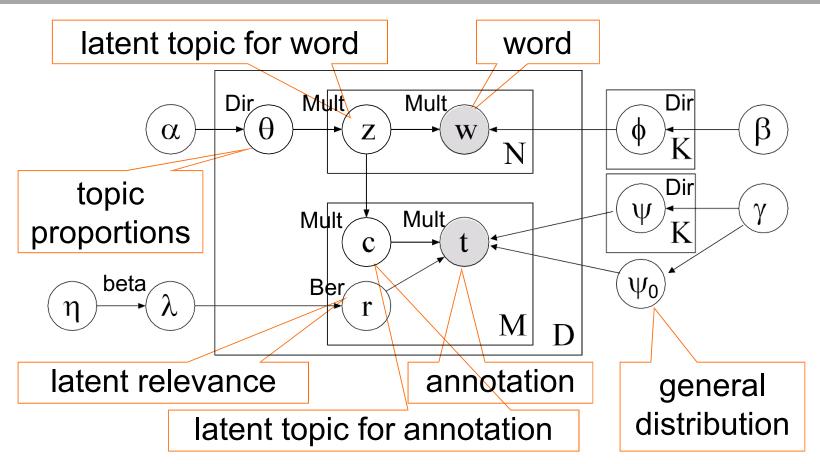
Correspondence LDA



David M. Blei and Michael I. Jordan. Modeling annotated data. In Proceedings of the 26th annual international ACM SIGIR conference on Research and development in information retrieval (SIGIR '03). Association for Computing Machinery, New York, NY, USA, 127–134. **2003**.

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Proposed model



- N: #words, M: #annotations, D: #documents, K: #topics
- each annotation is associated with a latent variable r, r=1 if content-related, r=0 otherwise

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Topics in Delicious

	unrelated	Topic1	Topic2	Торіс3	Topic4	Topic5
	reference	money	video	opensource	food	windows
\sim	web	finance	music	software	recipes	linux
Ч	imported	economics	videos	programming	recipe	sysadmin
n	design	business	fun	development	cooking	Windows
ō	internet	economy	entertainment	linux	Food	security
ជ	online	Finance	funny	tools	Recipes	computer
Ē.	cool	financial	movies	rails	baking	microsoft
annotation	toread	investing	media	ruby	health	network
\supset	tools	bailout	Video	webdev	vegetarian	Linux
	blog	finances	film	rubyonrails	diy	ubuntu
	15 E	money	music	project	recipe	windows
C		financial	video	code	food	system
Dr		credit	link	server	recipes	microsoft
h		market	tv	ruby	make	linux
D D		economic	movie	rails	wine	software
ſ		october	itunes	source	made	file
\$		economy	film	file	add	server
content word		banks	amazon	version	love	user
r		government	play	files	eat	files
5		bank	interview	development	good	ubuntu



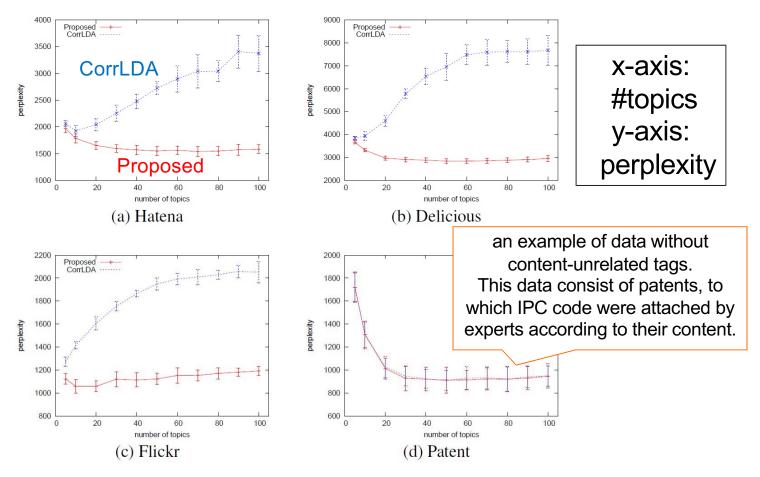
Topics in Flickr

	unrelated	Topic1	Topic2	Topic3	Topic4	Торіс5
	2008	dance	sea	autumn	rock	beach
ດນ	nikon	bar	sunset	trees	house	travel
Ĩ	canon	dc	sky	tree	party	vacation
I	white	digital	clouds	mountain	park	camping
ō	yellow	concert	mountains	fall	inn	landscape
Ť	red	bands	ocean	garden	coach	texas
<u>m</u>	photo	music	panorama	bortescristian	creature	lake
	italy	washingtondc	south	geotagged	halloween	cameraphone
annotation	california	dancing	ireland	mud	mallory	md
	color	work	oregon	natura	night	sun
probable image						



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Perplexity



The proposed method performed better than Corr-LDA ₃₇ in the case of noisy social annotation data.



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Generative Topic Models for Community Analysis

Ramesh Nallapati

http://www.cs.cmu.edu/~wcohen/10-802/lda-sep-18.ppt

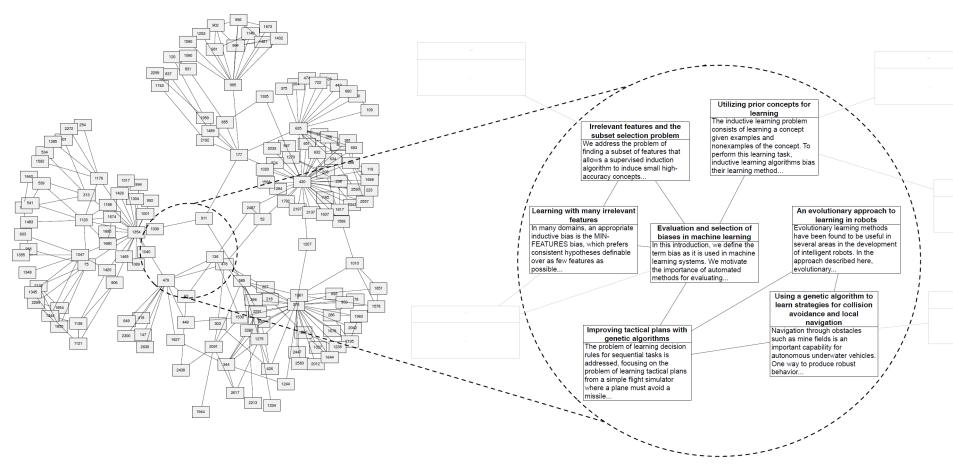
&

Arthur Asuncion, Qiang Liu, Padhraic Smyth:

Statistical Approaches to Joint Modeling of Text and Network Data



What if the corpus has network structure?

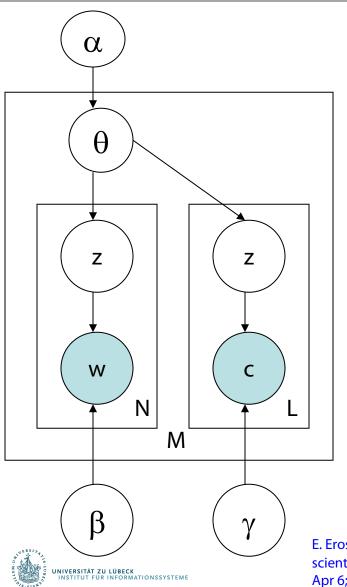


CORA citation network. Figure from [Chang, Blei, AISTATS 2009]



J. Chang, and D. Blei. Relational Topic Models for Document Networks. AISTATS, volume 5 of JMLR Proceedings, page 81-88. JMLR.org, **2009**.

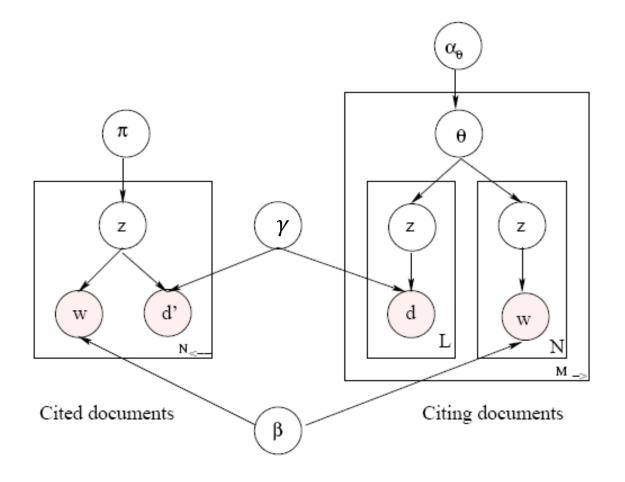
Hyperlink modeling using LDA



- For each document d,
 - Generate $\theta_d \sim \text{Dirichlet}(\alpha)$
 - For each position $i = 1, ..., N_d$
 - Generate a topic $z_i \sim Mult(\cdot | \theta_d)$
 - Generate a word $w_i \sim Mult (\cdot | \beta_{Z_n})$
 - For each citation $j = 1, ..., L_c$
 - Generate $z_i \sim Mult(\theta_d)$
 - Generate $c_i \sim Mult (\cdot | \gamma_{Z_j})$
- Learning using variational EM, Gibbs sampling

E. Erosheva, S Fienberg, J. Lafferty, Mixed-membership models of scientific publications. Proc National Academy Science U S A. 2004 Apr 6;101 Suppl 1:5220-7. Epub **2004** Mar 12.

Topic Influence in Blogs

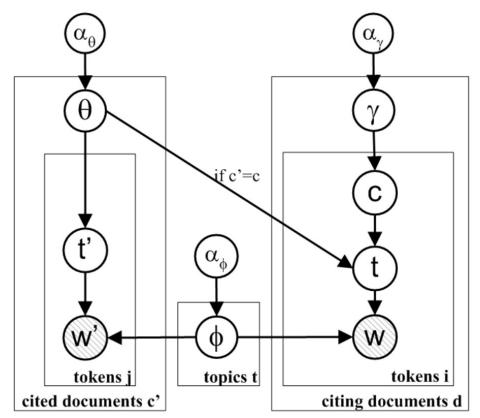




R. Nallapati, A. Ahmed, E. Xing, W.W. Cohen, Joint Latent Topic Models for Text and Citations, In: Proc. KDD, **2008**.

Modeling Citation Influences - Copycat Model

 Each topic in a citing document is drawn from one of the topic mixtures of cited publications

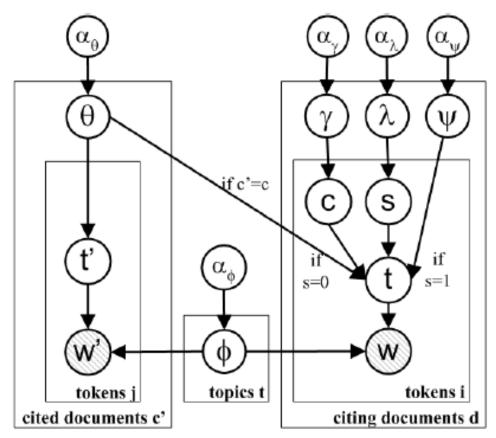




L. Dietz, St. Bickel, and T. Scheffer, Unsupervised Prediction of Citation Influences, In: Proc. ICML **2007**.

Modeling Citation Influences

 Citation influence model: Combination of LDA and Copycat model

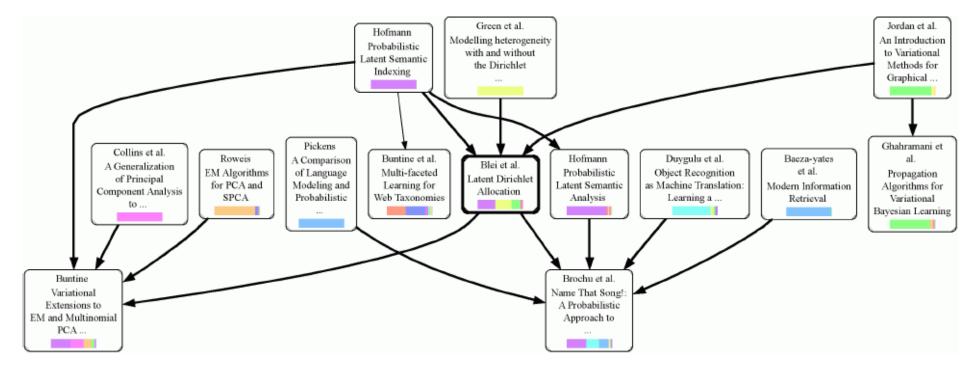




L. Dietz, St. Bickel, and T. Scheffer, Unsupervised Prediction of Citation Influences, In: Proc. ICML **2007**.

Modeling Citation Influences

• Citation influence graph for LDA paper





Modeling Citation Influences

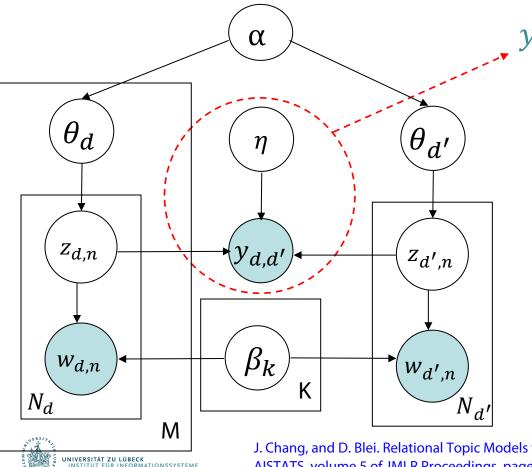
• Words in LDA paper assigned to citations

Cited Title	Associated Words	γ
Probabilistic	text(0.04), latent(0.04),	0.49
Latent Semantic	modeling(0.02), model(0.02),	
Indexing	indexing(0.01), $semantic(0.01)$,	
	document(0.01), collections(0.01)	
Modelling	dirichlet(0.02), mixture(0.02),	0.25
heterogeneity	allocation(0.01), context(0.01),	
with and	variable(0.0135), bayes(0.01),	
without the	continuous(0.01), improves(0.01),	
Dirichlet process	model(0.01), proportions(0.01)	
Introduction to	variational (0.01) , inference (0.01) ,	0.22
Variational	algorithms(0.01), including(0.01),	
Methods for	each(0.01), we(0.01), via(0.01)	
Graphical		
Methods		



Relational Topic Model (RTM) [ChangBlei 2009]

 Same setup as LDA, except now we have observed network information across documents



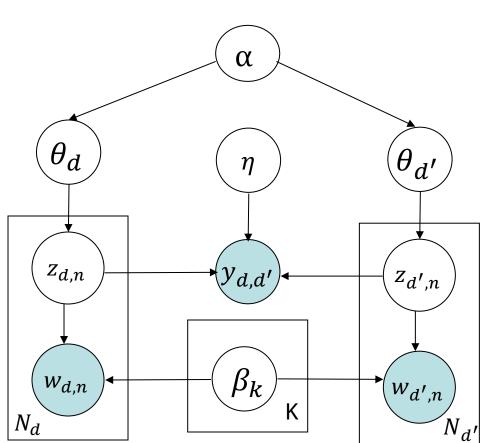
 $y_{d,d'} \sim \psi(y_{d,d'} | z_d, z_{d'}, \eta)$

"Link probability function"

Documents with similar topics are more likely to be linked.

J. Chang, and D. Blei. Relational Topic Models for Document Networks. AISTATS, volume 5 of JMLR Proceedings, page 81-88. JMLR.org, **2009**.

Relational Topic Model (RTM) [ChangBlei 2009]



- For each document d
 - Draw topic proportions $\theta_d | \alpha \sim Dir(\alpha)$
 - For each word $w_{d,n}$
 - Draw assignment $z_{d,n} | \theta_d \sim Mult(\theta_d)$
 - Draw word $w_{d,n}|_{Z_{d,n}}, \beta_{1:K} \sim Mult(\beta_{Z_{d,n}})$
 - For each pair of documents *d*, *d*'
 - Draw binary link indicator $y|z_d, z_{d'} \sim \psi(\cdot | z_d, z_{d'}, \eta)$



	# Docs	# Links	Ave. Doc- Length	Vocab-Size	Link Semantics
CORA	4,000	17,000	1,200	60,000	Paper citation (undirected)
Netflix Movies	10,000	43,000	640	38,000	Common actor/director
Enron (Undirected)	1,000	16,000	7,000	55,000	Communication between person i and person j
Enron (Directed)	2,000	21,000	3,500	55,000	Email from person i to person j



Conclusion

- Topic Modeling
- Relational topic modeling provides a useful start for combining text and network data in a single statistical framework

• RTM can improve over simpler approaches for link prediction

- Opportunities for future work:
 - Faster algorithms for larger data sets
 - Better understanding of non-edge modeling
 - Extended models

