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Ontology Change II

Lecture 11: Revision for Ontology Change
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Informationssysteme CS4130
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Recap of Lecture 9

- ▶ Considered postulates and concrete operators for change operators on belief-sets
 - ▶ Belief-Sets = logically closed sets over given language
 - ▶ change operators: expansion (just adding and closing), contraction (eliminating), revision (adding and consistency)
 - ▶ Different ways to construct operators: we considered partial-meet based operators

- ▶ Criticisms: discussed recovery, minimality, success

- ▶ Need for extensions and adaptations from ontology change perspective
 - ▶ Finiteness: (Finite) Belief bases instead of belief sets
 - ▶ Syntax sensitive revision
 - ▶ Continue today with semantic belief revision for belief bases

End of Recap

Semantical Belief-Base Revision

- ▶ Semantical belief-revision demands syntax insensitivity in both arguments: trigger and also the belief base
- ▶ In this scenario: belief bases = knowledge bases

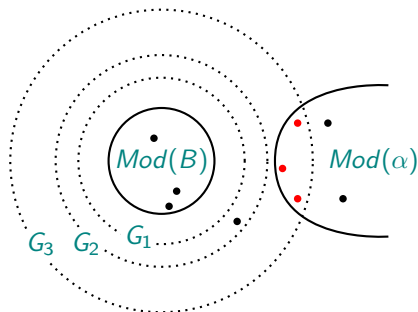
Schema for semantical belief revision

$$B * \alpha = \text{FinRep}(\text{Mod}(B) *_{sem} \text{Mod}(\alpha))$$

- ▶ $\text{Mod}(X)$ = Models of X
- ▶ $*_{sem}$ a semantical revision operator operating on pairs of sets of models
- ▶ $\text{FinRep}(M)$ = Formula or finite set of formulae that hold in all models in M

Approach 1 to Semantical Revision: Generalization

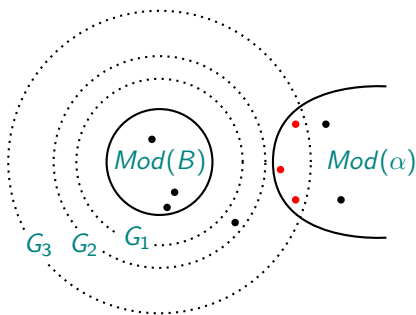
- ▶ Generalize (weaken) your belief base B' minimally s.t. enlarged set of models G_i intersects with Models of trigger
- ▶ Dalal's approach
 - ▶ Defined for propositional logic models • •
 - ▶ G_i = models with Hamming distance $\leq i$ to models in $Mod(B)$



Lit: M. Dalal. Investigations into a theory of knowledge base revision: preliminary report. In AAI-88, pages 475–479, 1988.

Approach 1 to Semantical Revision: Generalization

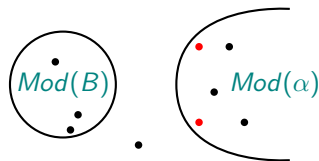
- ▶ Generalize (weaken) your belief base B' minimally s.t. enlarged set of models G_i intersects with Models of trigger
- ▶ Groves's approach: spheres
 - ▶ Defined on possible worlds ••
 - ▶ Possible world = maximally consistent set w.r.t. logic (\mathcal{L}, Cn)
 - ▶ G_i = sphere = set of possible worlds
- ▶ **Note:** Maximal consistent sets correspond to models
- ▶ “Semantics” also possible in logics defined by (\mathcal{L}, Cn)



Lit: A. Grove. Two modellings for theory change. *Journal of Philosophical Logic*, 17:157–170, 1988.

Approach 2 to Semantical Revision: Minimal distance

- ▶ Dual but more general approach to generalization: minimality
- ▶ Find trigger models α with “minimal distance” to $Mod(B)$
 $B * \alpha = FinRep(Min_{\leq Mod(B)}(Mod(\alpha)))$
- ▶ Various ways to specify minimal distance
 - ▶ incorporating order, cardinality, etc.



Lit: K. Satoh. Nonmonotonic reasoning by minimal belief revision. In FGCS-88, 455–462, 1988.

Lit: A. Borgida. Language features for flexible handling of exceptions in information systems. ACM Trans. Database Syst., 10(4):565–603, 1985.

Lit: A. Weber. Updating propositional formulas. In Expert Database Conf., pp. 487–500, 1986.

Lit: M. Winslett. Updating Logical Databases. Cambridge University Press, 1990.

Lit: K. D. Forbus. Introducing actions into qualitative simulation. In IJCAI-89, 1273–1278, 1988.

Complexity of Revision

- ▶ A main requirement in implementing BR operators: Feasibility of testing: $B * \alpha \models \beta$.
- ▶ Even for finite proposition B not really feasible
- ▶ Reason: Consistency testing is hard and you have potentially all subsets as culprit candidates
- ▶ Roughly the complexities are between NP and the second level of the polynomial hierarchy (so in $PSPACE$)

Lit: T. Eiter and G. Gottlob. On the complexity of propositional knowledge base revision, updates, and counterfactuals. *Artif. Intell.*, 57:227–270, October 1992.

- ▶ How to react to this?
 - ▶ Restrict logic to be used
 - ▶ Restrict the set of culprits: E.g., allow only culprits in ABox
 - ▶ Restrict other relevant parameters: treewidth, common variables

Lit: A. Pfandler et al. On the parameterized complexity of belief revision. In *IJCAI-15*, pages 3149–3155, 2015.

Further Requirements

- ▶ Trigger is by itself a belief base: [Multiple Belief Revision](#)
- ▶ There is not a single trigger, but a whole sequence: [Iterated revision](#)
- ▶ Learning ontologies: need non-amnestic (dynamic) iterated belief revision (connections to inductive learning)
- ▶ Need different logics (not fulfilling, e.g., Deduction property): Revision for ontologies in DLs
- ▶ Need to revise other structures such as mappings

Ontology Change

Classification of Ontology Change

- ▶ Group 1 (“Overcome Heterogeneity”)
 - ▶ Approaches where the main purpose is to resolve heterogeneity of ontologies by bridging between them
 - ▶ Ontologies are not changed (directly)
 - ▶ But mappings may change
 - ▶ Examples: ontology mapping, o. alignment, o. morphisms etc.
- ▶ Group 2 (“Combine ontologies”)
 - ▶ Build new ontology based on input ontologies
 - ▶ Examples: ontology merge (input ontologies have same domain), ontology integration (input ontologies have similar domains)
- ▶ Group 3 (“Modify ontologies”)
 - ▶ Change ontologies (not necessarily caused by other ontologies)
 - ▶ Examples: ontology debugging, ontology repair, ontology evolution

Lit: G. Flouris et al. *Ontology change: classification and survey*. *The Knowledge Engineering Review*, 23(2):117–152, 2008.

Requirements due to Ontology Merge (and others)

Ontology Merge (Flouris et al. 08)

Purpose: Fuse knowledge from ontologies over same domain

Input: Two ontologies (from identical domains)

Output: An ontology

Properties: Fuse knowledge to describe domain more accurately

Requirements for OC operators

- ▶ Trigger by itself is a belief base: [multiple revision](#)

Requirements due to Ontology Merge (and others)

Ontology Merge (Flouris et al. 08)

Purpose: Fuse knowledge from ontologies over same domain

Input: Two ontologies (from identical domains)

Output: An ontology

Properties: Fuse knowledge to describe domain more accurately

Requirements for OC operators

- ▶ Trigger by itself is a belief base: [multiple revision](#)
- ▶ Belief base formulated in non-FOL (such as DLs)
 - ▶ Notion of AGM compliant contraction/revision
Lit: G. Flouris, D. Plexousakis, and G. Antoniou. Generalizing the AGM postulates: preliminary results and applications. NMR-04, pp. 171–179, 2004.
 - ▶ Different postulates (to capture e.g. minimality):
Lit: M. M. Ribeiro and R. Wassermann. Minimal change in AGM revision for non-classical logics. In KR-14, 2014.

AGM-Compliance

- ▶ Remember the additional properties on Cn required by AGM
 - ▶ **Language expressivity:** Language \mathcal{L} should contain all propositional connectors
 - ▶ **Supra-classicality:** If α can be derived from X by propositional logic, then $\alpha \in Cn(X)$
 - ▶ **Compactness:** If $\alpha \in Cn(X)$, then $\alpha \in Cn(X')$ for some finite $X' \subseteq X$.
 - ▶ **Deduction:** $\beta \in Cn(X \cup \{\alpha\})$ iff $(\alpha \rightarrow \beta) \in Cn(X)$
 - ▶ **Disjunction in premisses:** If $\gamma \in Cn(X \cup \{\alpha\}) \cap Cn(X \cup \{\beta\})$, then $\gamma \in Cn(X \cup \{\alpha \vee \beta\})$.

- ▶ Are these really **necessary** in order to define a contraction operator fulfilling all six basic postulates?
 - (C1) $K \div \alpha \in BS_{\mathcal{L}}$ (Closure)
 - (C2) $K \div \alpha \subseteq K$ (Inclusion)
 - (C3) If $\alpha \notin K$, then $K = K \div \alpha$ (Vacuity)
 - (C4) If $\alpha \notin Cn(\emptyset)$, then $\alpha \notin K \div \alpha$. (Success)
 - (C5) If $\alpha \in K$, then $K \subseteq (K \div \alpha) + \alpha$. (Recovery)
 - (C6) If $\alpha \leftrightarrow \beta \in Cn(\emptyset)$, then $K \div \alpha = K \div \beta$. ((Right) Extensionality)

- ▶ **AGM Compliance**

AGM compliance and Main Theorem

Definition

(\mathcal{L}, Cn) is called **AGM-compliant** iff there is a contraction operator \div fulfilling all six basic AGM contraction postulates (C1)–(C6).

Definition

Let X, K be sets of formulae s.t.

- ▶ $K = Cn(K)$ and
- ▶ $Cn(\emptyset) \subsetneq Cn(X) \subsetneq K$

Define

$$K^-(X) = \{K' \mid Cn(K') \subsetneq Cn(K) \text{ and } Cn(K' \cup X) = Cn(K)\}$$

(\mathcal{L}, Cn) is called **decomposable** iff for any X, K the set $K^-(X)$ is not empty.

Theorem (Flouris et al. 16)

A logic is AGM compliant iff it is decomposable

- ▶ So we have a simple criterion (not many such as deduction, supraclassicality etc.) to test for AGM-compliance.
- ▶ Observation: Most DLs are not AGM compliant
- ▶ Hence: Cannot transfer AGM results directly to DLs
- ▶ This is hot research topic.
 - ▶ Contraction/revision for expressive DLs:
Lit: M. M. Ribeiro and R. Wassermann. Base revision for ontology debugging. *Journal of Logic and Computation*. Advanced Access, published September 5, 2008, 2008.
 - ▶ Contraction/revision for lightweight DLs
Lit: Z. Zhuang, Z. Wang, K. Wang, and G. Qi. DI-lite contraction and revision. *J. Artif. Intell. Res.*, 56:329–378, 2016.

Requirements due to Ontology Merge (and others)

Ontology Merge (Flouris et al. 08)

Purpose: Fuse knowledge from ontologies over same domain

Input: Two ontologies (from identical domains)

Output: An ontology

Properties: Fuse knowledge to describe domain more accurately

Requirements for OC operators

- ▶ Belief base formulated in non-FOL (such as DLs)
 - ▶ Need to consider generalizations of consistency such as coherence or even arbitrary integrity constraints

Requirements due to Ontology Mapping

Ontology Mapping (Flouris et al. 08)

Purpose: Heterogeneity resolution, interoperability of ontologies

Input: Two (heterogeneous) ontologies

Output: A mapping between the ontologies' vocabularies

Properties: The output identifies related vocabulary entities

Requirements for OC operators

- ▶ Mappings should not lead to inconsistencies
- ▶ Change of mappings in design time or due to change in ontologies
- ▶ **Lit:** C. Meilicke and H. Stuckenschmidt. Reasoning support for mapping revision. *Journal of Logic and Computation*, 2009.
- ▶ **Lit:** G. Qi, Q. Ji, and P. Haase. A conflict-based operator for mapping revision. In DL-09, volume 477 of *CEUR Workshop Proceedings*, 2009.

Mappings for Ontologies

- ▶ Data exchange provided mappings between schemata
- ▶ Here: Mappings between mappable “elements” of an ontology
- ▶ No unique representation format for ontology mappings

Definition (Mappings according to (Meilicke et al. 09))

$$(e_1, e_2, c, deg)$$

- ▶ $e_1 \in$ mappable elements of first ontology \mathcal{O}_1
(e.g. concept symbols of \mathcal{O}_1)
- ▶ $e_2 \in$ mappable elements of second ontology \mathcal{O}_2
- ▶ c : type of mapping
(e.g. c is equivalence or subsumption if e_i concepts)
- ▶ deg : degree of trust in the mapping

Example (Incompatible ontologies)

\mathcal{O}_A

A1 $Article_A \equiv \exists publ_A. Journal_A$

A2 $Journal_A \sqsubseteq \neg Proceedings_A$

A3 (*func publ_A*)

\mathcal{O}_B

B1 $Article_B \equiv \exists publ_B. Journal_B$
 $\sqcup Proceedings_B$

B2 $publish_B(ab, procXY)$

B3 $Proceedings_B(procXY)$

► Following set of mappings \mathcal{M}_2 is consistent with $\mathcal{O}_A \cup \mathcal{O}_B$

- $(Article_A, Article_B, \sqsubseteq, 1)$
- $(Journal_A, Journal_B, \equiv, 1)$
- $(Proceedings_A, Proceedings_B, \equiv, 1)$
- $(publ_A, publ_B, \equiv, 1)$

\implies Can use revision on mappings to get from \mathcal{M}_1 to \mathcal{M}_2 .

Requirements due to Ontology Evolution

Ontology Evolution (Flouris et al. 08)

Purpose: Respond to a change in the domain or its conceptualization

Input: An ontology and a (set of) change operation(s)

Output: An ontology

Properties: Implements a (set of) change(s) to the source ontology

Requirements for OC operators

- ▶ Change in domain due to change in environment:
update vs. revision
- ▶ Evolution calls for iterative revision

Requirements due to Ontology Learning

Ontology Learning (my addition)

Purpose: Respond to new bits of information from sender

Input: A start ontology and a potentially infinite sequence of information

Output: An ontology (sequence)

Properties: Learns an ontology from a sequence

- ▶ Related to evolution: but emphasis on change of informedness and potential infinity
- ▶ **Requirements for OC operators**
 - ▶ Informed iterated revision on potentially infinite sequences
 - ▶ Notion of learning success (e.g. stabilization, reliability)
 - Lit:** D. Zhang and N. Y. Foo. Convergency of learning process. In AI-02, vol 2667 of LNCS, pp. 547-556, 2002.
 - Lit:** K. T. Kelly. Iterated belief revision, reliability, and inductive amnesia. *Erkenntnis*, 50:11-58, 1998.

Update vs. Revision

- ▶ Early CS work related to BR in Database Theory

Lit: A. M. Keller and M. Winslett. On the use of an extended relational model to handle changing incomplete information. IEEE Transactions on Software Engineering, 11(7):620–633, 1985.

- ▶ Problem: Preserve integrity constraints when DB is updated
- ▶ Two main differences to BR
 - ▶ In DB: Not a theory to update but a structure
 - ▶ Update operators \diamond fulfill different postulates
- ▶ Reason is: different conflict diagnostics
 - ▶ Revision: Conflict caused by false information
 - ▶ Update: Conflict caused by outdated information
 - ▶ In ontology change even a third diagnostics is possible: different terminology

Lit: H. Katsuno and A. Mendelzon. On the difference between updating a knowledge base and revising it. In KR-91, pages 387–394,1991.

Example (Winslett 1988)

- ▶ Input belief set: There is either a book on the table or a magazine

$$Cn(\alpha \leftrightarrow \neg\beta)$$

- ▶ Trigger information: A book is put on the table

$$\alpha$$

- ▶ Apply revision operator fulfilling Postulates (R3) and (R4)

$$(R3): K * \alpha \subseteq K + \alpha$$

$$(R4): \text{If } \neg\alpha \notin K, \text{ then } K + \alpha \subseteq K * \alpha.$$

(Vacuity)

- ▶ Output belief set: There is a book on the table and no magazine.

$$Cn(\{\alpha \leftrightarrow \neg\beta\} \cup \{\alpha\}) = Cn(\alpha \wedge \neg\beta)$$

- ▶ Alternative postulate instead of vacuity

$$\text{If } \alpha \in K, \text{ then } K \diamond \alpha = K$$

Lit: M. Winslett. Reasoning about action using a possible models approach. In Proc. of the 7th National Conference on Artificial Intelligence (AAAI-88), pp. 89–93, 1988.

Iterated Belief Revision

Iterating

- ▶ Aim: Apply change operators on sequence of triggers
 $\alpha_1, \alpha_2, \dots$

- ▶ **Static approach**: same operator in every step on revision result

$$(\dots((B * \alpha_1) * \alpha_2) * \dots) * \alpha_n$$

- ▶ **Dynamic Approach**

- ▶ operator may change depending on history

$$(\dots((B *_1 \alpha_1) *_2 \alpha_2) *_3 \dots) *_n \alpha_n$$

- ▶ Belief base may encode history

Iterated AGM Revision

- ▶ AGM BR not tailored towards iteration:
Considers only postulates for arbitrary but fixed belief set
- ▶ Only one interesting result for iterated AGM revision:

Proposition

If $$ fulfills all AGM revision postulates (R1)–(R8), then it fulfills*

$$\text{If } \neg\beta \notin K * \alpha, \text{ then } (K * \alpha) * \beta = K * (\alpha \wedge \beta)$$

- ▶ In words: If second trigger compatible with revision result with first trigger, then revising with both triggers is the same as revising with conjunction

Need for Iteration Postulates

- ▶ Systematic study of iterated revision started in 1994

Lit: A. Darwiche and J. Pearl. On the logic of iterated belief revision. In TARK-94, 5–23, 1994.

Example (Darwiche, Pearl 94)

- ▶ Agent hears an animal X barking like a dog
- ▶ So he thinks X is not a bird and cannot fly.

$$K \equiv \neg Bird \wedge \neg Flies$$

- ▶ But if he were told that X is a bird, he would assume that it flies.

$$K * Bird \equiv Bird \wedge Flies$$

- ▶ If agent were to come to know that X can fly, then he should still believe: If X were a bird, then X would fly. Formally: $(K * Flies) * Bird \models Bird \wedge Flies$.
- ▶ But one can construct AGM-conform revision $*$ (say amnesic revision) s.t.:

$$(K * Flies) * Bird \equiv Bird$$

Iteration Postulates (First Try)

DP1 If $\alpha \in Cn(\beta)$, then $(K * \alpha) * \beta = K * \beta$.

“If second trigger stronger than first, then second trigger overrides effects of first”.

DP2 If $\neg\alpha \in Cn(\beta)$, then $(K * \alpha) * \beta = K * \beta$.

“For incompatible triggers the second one overrides the first one’s effects”

DP3 If $\alpha \in K * \beta$, then $\alpha \in (K * \alpha) * \beta$.

“If revision only by second trigger entails first trigger, then the sequential revision with both triggers does too.”

DP4 If $\neg\alpha \notin K * \beta$, then $\neg\alpha \notin (K * \alpha) * \beta$.

“If revision only by second trigger is compatible with first trigger, then sequential revision with both triggers is too.”

Wake-Up-Question

Which one of the DP Postulates rules out the bird example?

DP1 If $\alpha \in Cn(\beta)$, then $(K * \alpha) * \beta = K * \beta$.

DP2 If $\neg\alpha \in Cn(\beta)$, then $(K * \alpha) * \beta = K * \beta$.

DP3 If $\alpha \in K * \beta$, then $\alpha \in (K * \alpha) * \beta$.

DP4 If $\neg\alpha \notin K * \beta$, then $\neg\alpha \notin (K * \alpha) * \beta$.

Example (Darwiche, Pearl 94)

- ▶ $K \equiv \neg Bird \wedge \neg Flies$
- ▶ $K * Bird \equiv Bird \wedge Flies$
- ▶ $(K * Flies) * Bird \equiv Bird \wedge Flies$

Need More Information

- ▶ (DP2) cannot be fulfilled by any AGM revision operator for belief sets [Freund/Lehmann, 02]
- ▶ Reason is mainly: AGM allows for inconsistent belief sets
- ▶ Reaction by [Darwiche/Pearl 97]: consider postulates with epistemic states Ψ instead of belief sets
- ▶ Allows dynamic (state-based) iteration: history encoded in state Ψ and not captured by logic
 - ▶ Every state Ψ induces belief set $BS(\Psi)$
 - ▶ But revision depends on state Ψ not induced belief set $BS(\Psi)$
 - ▶ In particular: $\Psi_1 * \alpha \neq \Psi_2 * \alpha$ possible even if $BS(\Psi_1) = BS(\Psi_2)$.

Lit: M. Freund and D. J. Lehmann. Belief revision and rational inference. Computing Research Repository (CoRR), cs.AI/0204032, 2002.

Lit: A. Darwiche and J. Pearl. On the logic of iterated belief revision. Artificial intelligence, 89:1–29, 1997.

Epistemic States

- ▶ Epistemic states are described in the postulates as abstract entities
 - ▶ Situation is the same as, say, in modal (temporal) logic or finite automata etc.
- ▶ But in order to construct concrete operators one has to construct epistemic states.
- ▶ There is a very popular approach based on **ranking functions** developed by W. Spohn in a series of papers and in a book.
- ▶ Ranking function κ : Assigns ordinal numbers to possible worlds (e.g., truth assignments in propositional logic)
- ▶ Does not give ranking only but also specifies plausibility distances.

Lit: W. Spohn. *The Laws of Belief: Ranking Theory and Its Philosophical Applications*. Oxford University Press, 2012.

Dynamic Operators

- ▶ Other approaches stick to belief sets (or belief bases) but allow dynamic revision operators.
- ▶ **Lit:** D. J. Lehmann. Belief revision, revised. In IJCAI-95, 1534–1540, 1995.
- ▶ **Lit:** A. C. Nayak, M. Pagnucco, and A. Sattar. Changing conditional beliefs unconditionally. In TARK-96, 119–135, 1996.

Infinite Iteration

Formal Learning Theory for Infinite Revision

- ▶ Iterable revision operators applied to potentially infinite sequence of triggers
- ▶ Define principles (postulates) that describe adequate behaviour
- ▶ Minimality ideas and other principles of BR are not sufficient
- ▶ Hence, instead: Let you guide by principles of inductive learning and **formal learning theory**
 - ▶ Compare PAC (Probably Approximately Correct) framework
 - ▶ Compare FOIL (First-Order Inductive Learning) framework

The Scientist-Nature-Scenario

- ▶ Class of possible worlds (one of them the real world = nature)
- ▶ Scientist has to answer queries regarding the real world
- ▶ He gets stream of data compatible with the real world
- ▶ Conjectures according to some strategy at every new arrival of trigger a hypothesis on the correct answer
- ▶ Success: Sequence of answers stabilizes to a correct hypothesis.
 - ▶ Various stabilization criteria

Lit: E. Martin and D. Osherson: Elements of Scientific Inquiry. The MIT Press, 1998

Lit: K. T. Kelly. The Logic of Reliable Inquiry. Oxford University Press, 1995.

Example: The Scientist-Nature-Scenario for Orders

- ▶ Class of possible worlds

Example (Components of Order Example)

$Strict(\mathbb{N}) =$ Strict total orders $<$ of \mathbb{N}

- ▶ $0, 1, 2, 3, \dots$ (isomorphic to $\omega = \{0, 1, 2, 3, \dots\}$ with natural ordering)
- ▶ $1, 0, 2, 3, \dots$ (isomorphic to ω)
- ▶ $\dots 3, 2, 1, 0$ (isomorphic to $\omega^* = \{\dots 3, 2, 1, 0\}$ with inverse natural ordering)
- ▶ $0, 2, 4, 6, \dots, 1, 3, 5, 7, \dots$ (isomorphic to $\omega\omega$)

Example: The Scientist-Nature-Scenario for Orders

- ▶ He gets stream of data compatible with the real world

Example (Components of Order Example)

Stream of data made up by facts (called **environments e**)

- ▶ $R(2,3), R(1,2), R(0,2), R(1,4) \dots$
(for world: $0,1,2,3, \dots$)
- ▶ $R(4,3), R(5,2), \dots$
(for world: $\dots 3,2,1,0$)

Example: The Scientist-Nature-Scenario for Orders

- ▶ Scientist answers query regarding the real world (problem)

Example (Components of Order Example)

Problem set: orders that are isomorphic (\sim) to ω or to ω^*

- ▶ $0,1,2,3, \dots$ is isomorphic to ω
- ▶ $\dots 3,2,1,0$ is isomorphic to ω^* .
- ▶ Problem query: Has order a least element (i.e., is it isomorphic to ω)?

Example: The Scientist-Nature-Scenario for Orders

- ▶ Success: Sequence of answers stabilizes to a correct hypothesis.

Example (Components of Order Example)

Scientist solves problem P iff for every order $< \in P$ and every environment e :

- ▶ If $<$ has least element, then cofinitely often scientist says yes on $e(n)$ (= n -prefix of environment e)
- ▶ If $<$ has no least element, then for cofinitely many n scientist says no on $e(n)$

Example: The Scientist-Nature-Scenario for Orders

- ▶ Conjectures—according to some strategy—at every new arrival of trigger a hypothesis on the correct answer
- ▶ Success: Sequence of answers stabilizes to a correct hypothesis.

Example (Components of Order Example)

$P = \{ \langle \in \text{Strict}(\mathbb{N}) \mid \langle \text{ is isomorphic to } \omega \text{ or to } \omega^* \} \text{ solvable}$

- ▶ L-score: For any finite prefix of any environment smallest number not occurring in right argument of R
- ▶ G-score: smallest number not occurring in left argument of R
- ▶ Scientist: If L-score lower than G-score on given prefix, say yes, otherwise no.

Example (Proof of solvability)

- ▶ L-score: smallest number not occurring in right argument of R
- ▶ G-score: smallest number not occurring in left argument of R
- ▶ Scientist: If L-score lower than G-score on given prefix, say yes, otherwise no.

- ▶ **Proof** of solvability:
 - ▶ Intuitively: The L-score (G-score) is the best candidate for the least (greatest) element of $<$ (if there is one)
 - ▶ Suppose $< \sim \omega$. Then least element of $<$ appears somewhere as left but never as right element. Hence: L-scores of $e[n]$ is bounded. Every number appears as first argument. Hence: The G-scores of $e[n]$ are unbounded.
 - ▶ Suppose $< \sim \omega^*$. Situation reversed.
 - ▶ Moreover: scores are monotonic w.r.t. increasing prefix.
 - ▶ Hence: If $< \sim \omega$, then coinfinately often L-score is smaller than G score
 - ▶ If $< \sim \omega^*$, then coinfinately often G-score is smaller than L-score

Learning Aims of Scientist-Nature-Scenario

- ▶ Above scenario generalized to arbitrary FOL structures in (Martin/Osherson 1998)
- ▶ Also (Martin/Osherson 1998) consider revision operators for guessing the true world (see next slides)

- ▶ Similar principles as in PAC learning from machine learning
- ▶ But two main differences
 - ▶ Approach of (Martin/Osherson 1998) has not a pre-determined finite set of data items (as is the case for most scientific inquiry situations)
 - ▶ Exact prediction of the real world (not approximate prediction within some tolerance interval as in PAC)

Lit: E. Martin and D. Osherson: *Elements of Scientific Inquiry*. 1998, The MIT Press

Choosing Revision as Strategy

- ▶ Kelly investigates learning based on various revision operators defined for epistemic states
- ▶ Hypotheses = sentences in the belief sets
- ▶ Main (negative) result in (Kelly 98)

Theorem

*Revision operators implementing a minimal (one-step) revision suffer from **inductive amnesia**: If and only if some of the past is forgotten, stabilization is guaranteed.*

Lit: K. T. Kelly. Iterated belief revision, reliability, and inductive amnesia. *Erkenntnis*, 50:11–58, 1998.

Choosing Revision as Strategy

- ▶ Martin/Osherson investigate learning based revision operators defined for finite sequences
- ▶ So their revision operators have always the **whole history** of triggers (they do not have to store the history)
- ▶ This leads to positive results

Theorem

Revision operators provide ideal learning strategies: There is a revision operator a scientist can use to solve every (solvable) problem.

Lit: E. Martin and D. Osherson. Scientific discovery based on belief revision. *Journal of Symbolic Logic*, 62(4):1352–1370, 1997.

Stabilization for Ontology Learning

Example (Book Shopping Agent)

$$\begin{array}{l} O_{rec} \models \text{cheap} \equiv \text{costs} < 5\$, \quad \neg \text{costs} < 5\$('Faust') \\ O_{send} \models \text{cheap} \equiv \text{costs} < 6\$, \quad \text{costs} < 6\$('Faust') \end{array}$$

- ▶ Receiver: “List all cheap books by Goethe”
- ▶ Sender stream: $\alpha_1 = \text{cheap}('Faust')$ ~~?~~, $\alpha_2, \alpha_3, \dots$
- ▶ Integrating stream elements by revision operator \circ gives
Output stream $(O_{rec}^i)_{i \in \mathbb{N}}$:

$$(O_{rec}, O_{rec} \circ \alpha_1, (O_{rec} \circ \alpha_1) \circ \alpha_2, \dots)$$

- ▶ For which operators stabilization?

Lit: Eschenbach and Ö. Ontology revision based on reinterpretation. Logic Journal of the IGPL, 18(4):579–616, 2010.