
Intelligent Agents

Dynamic Epistemic Logic – Part 2

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Today's lecture based on

- The AAMAS 2019 Tutorial „EPISTEMIC REASONING IN MULTI-AGENT SYSTEMS“, Part 4: Dynamic Epistemic Logic
<http://people.irisa.fr/Francois.Schwarzentruber/2019AAMAStutorial/>



MODEL CHECKING

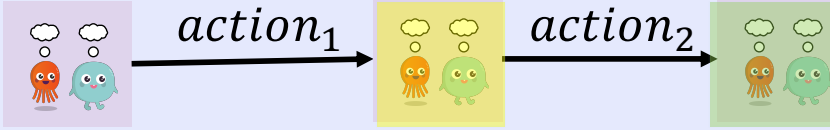


Model checking with actions

Definition

The model checking problem is given by :

- Input: an epistemic state
- A formula, e.g., $\langle action_1, action_2 \rangle K_a p$

- Output: yes if 
no otherwise

Model checking complexity

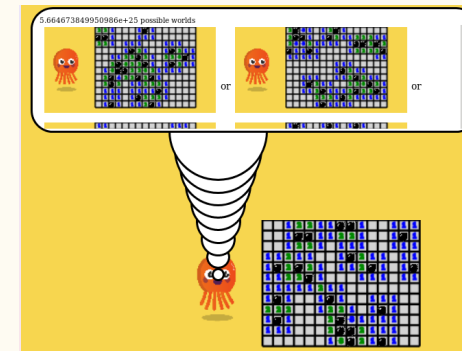
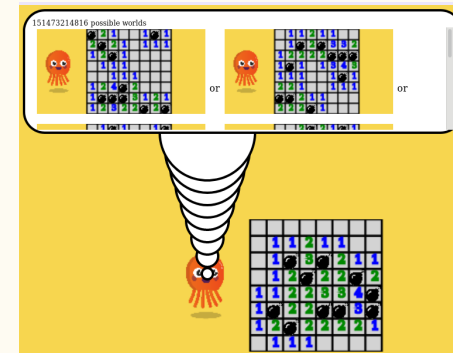
- Public actions: P-complete (van Benthem 2011)
- Any type of action : PSPACE-complete (Aucher/Schwarzentruher 2013), (Pol et al. 2015)

State explosion problem

Example

Minesweeper

- 8×8 with 10 bombs:
> 10^{12} possible worlds
- 10×12 with 20 bombs:
> 10^{25} possible worlds



State explosion problem

- See (Benthem et al. 2015), (Benthem et al. 2018)
- Also see: (Charrier/S. 2017), (Charrier/S. 2018)
 - Succinct representations of epistemic states **and** actions
 - Easy to specify by means of accessibility programs;
 - Succinct model checking Pspace-complete (and so stays in PSPACE as for non-succinct case).

Impact

- Theoretical

Theorem (Maubert et al. 2019)

Existence of a (uniform) strategy in bounded¹⁾ imperfect info games is in PSPACE.

1) Example: public announcements do not expand the epistemic model

- Practical: Symbolic model checking implemented in Hintikka's world
 - S. Gamblin and A. Niveau
 - Using BDDs (binary decision diagrams)

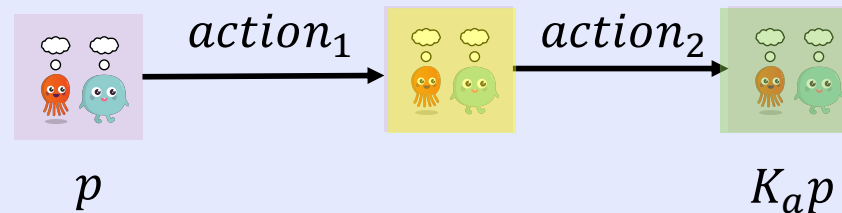
THEOREM PROVING



Theorem proving (another point of view)

Motivation: parametrized verification

For all epistemic states in which p holds



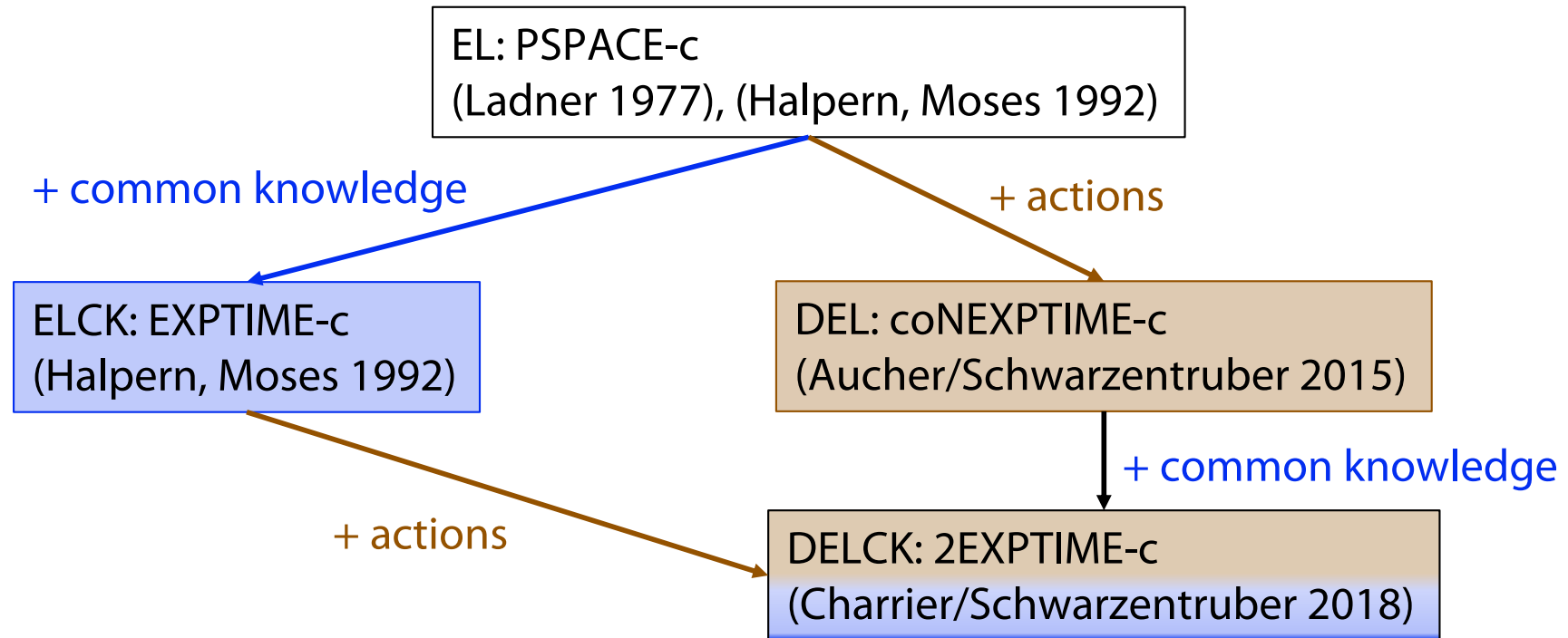
So: $p \rightarrow \langle action_1; action_2 \rangle K_a p$ is a theorem (i.e. true in all states)

Definition

The theorem proving problem is given by :

- Input: a formula ϕ
- Output: yes if ϕ is a theorem , no otherwise

Theorem proving is highly intractable



General Insights

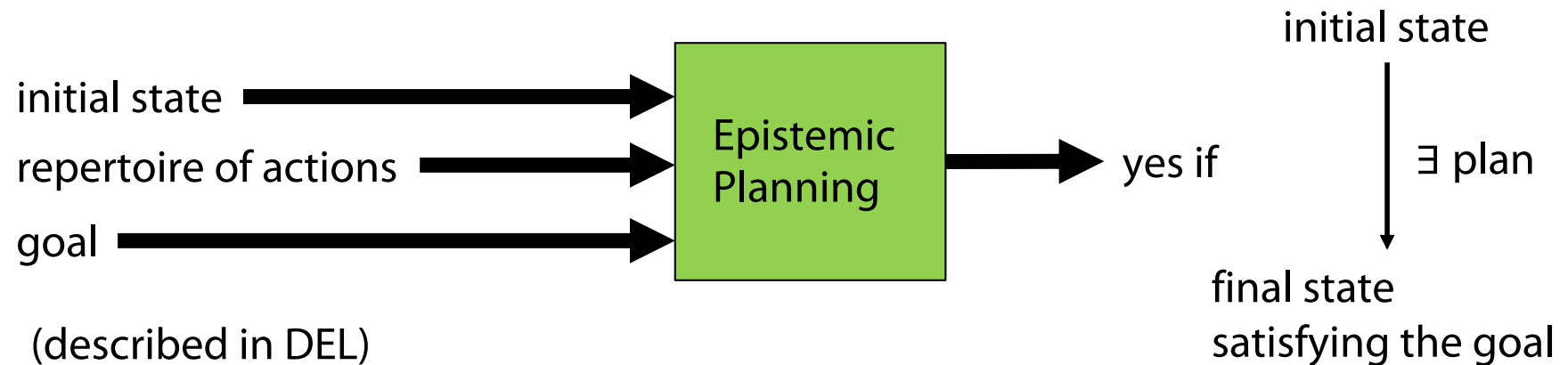
- Semi-product modal logics have high complexities (Gabbay et al. 2003)
- Model checking more practical than theorem proving (Halpern/Vardi 1991)

EPISTEMIC PLANNING



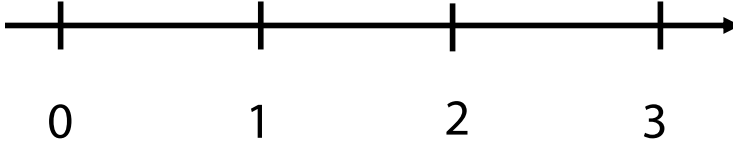
The general scenario of epistemic planning

(Bolander/Andersen 2011)



(Un-)Decidability of epistemic planning

no postconditions :	yes	?	no	no
Boolean postcondition:	yes	no	no	no

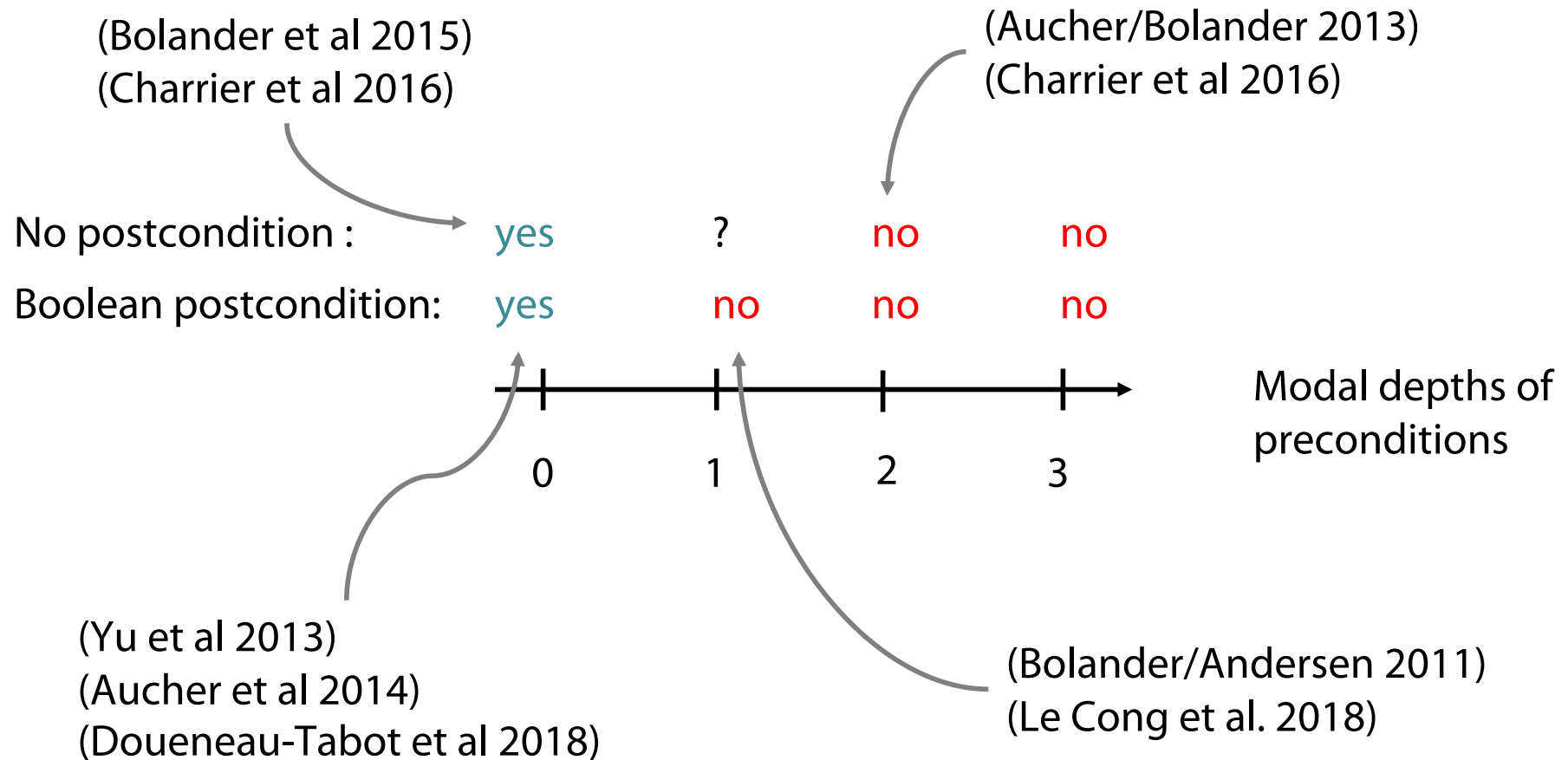


modal depths of
preconditions

e.g. $\text{md}(K_a K_b K_a p) = 3$



(Un-)Decidability of epistemic planning



Undecidability

Theorem (Bolander/Andersen 2011)

Epistemic planning is undecidable for

- two agents
- Boolean post conditions
- $md(pre) \leq 1$

Theorem (Le Cong et al 2018)

Epistemic planning is undecidable for

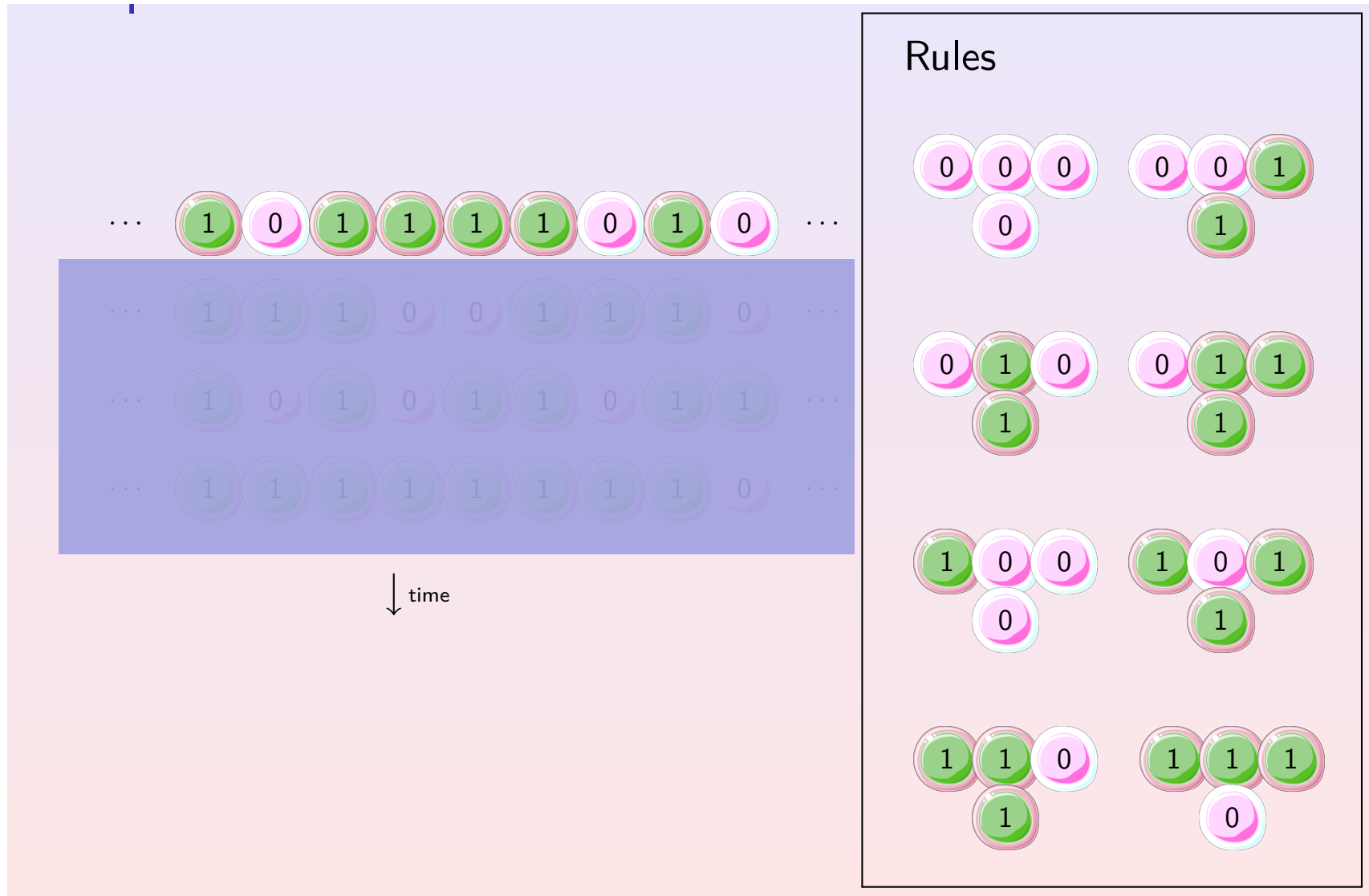
- two agents
- Boolean post conditions
- $md(pre) \leq 1$

even if

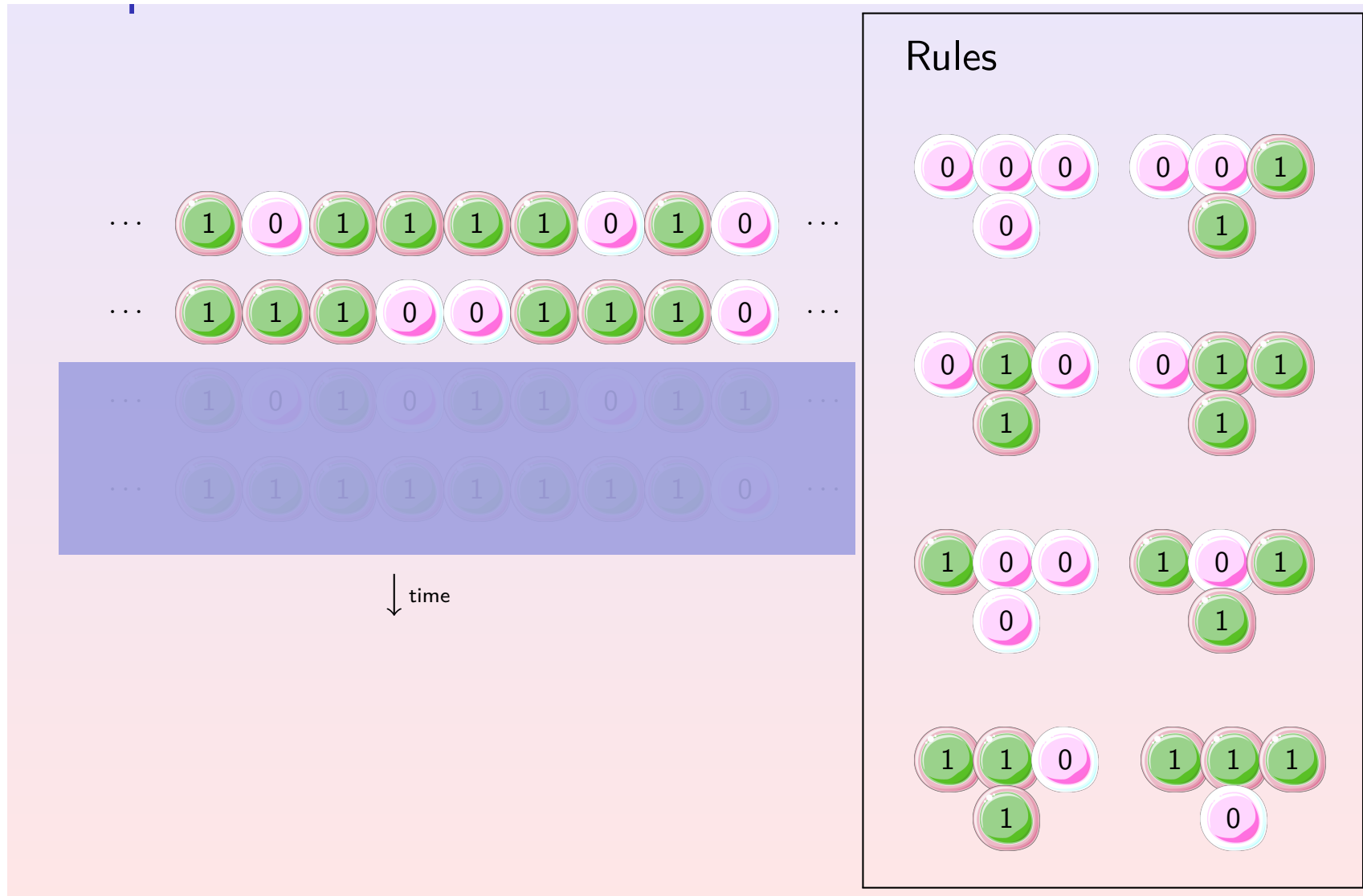
- there is only a fixed repertoire of one action and
- There are at most 6 atomic propositions

Proof idea: Reduction from halting problem of a small universal cellular automaton

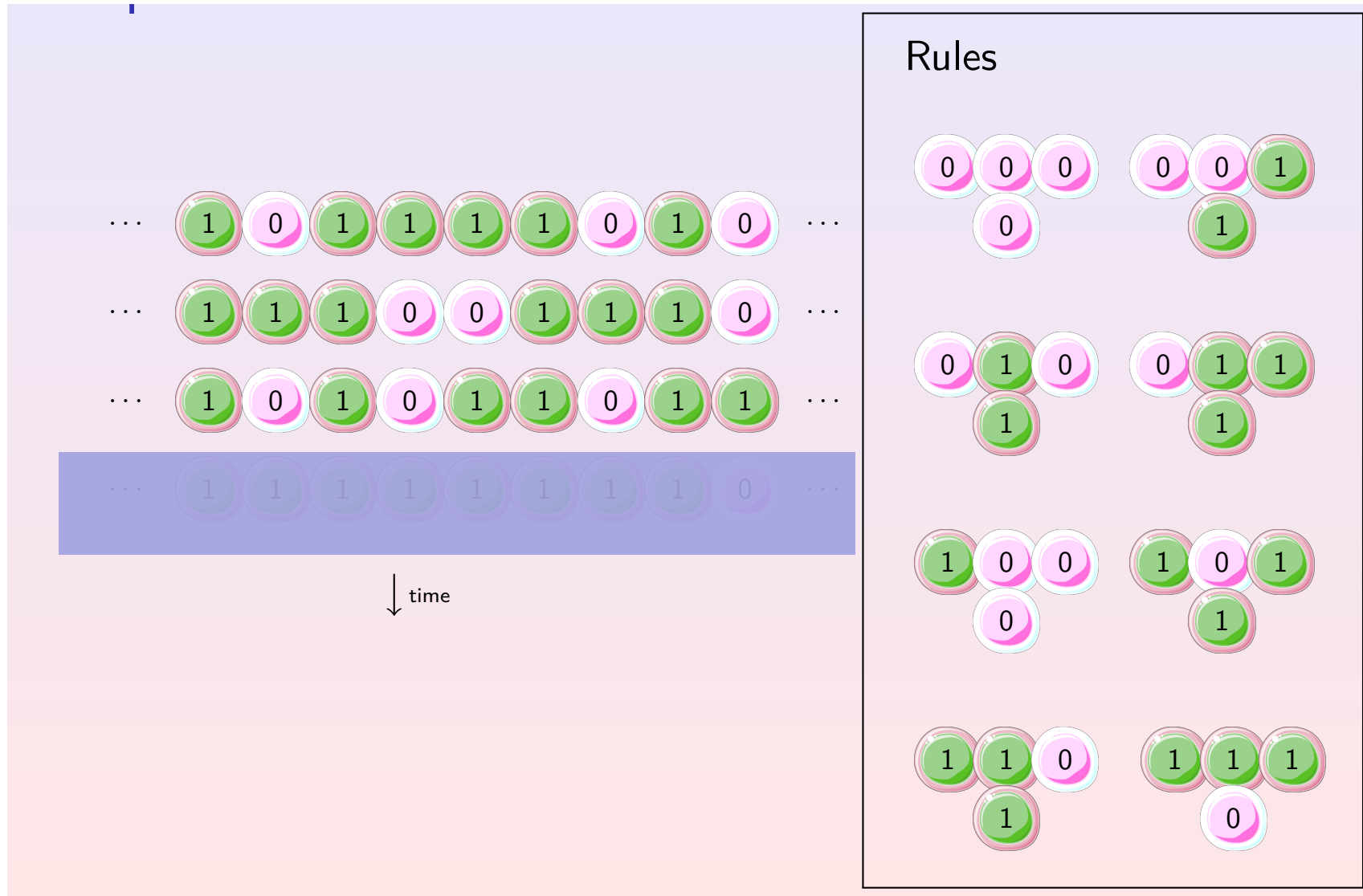
Example: the 110 Rule cellular automaton



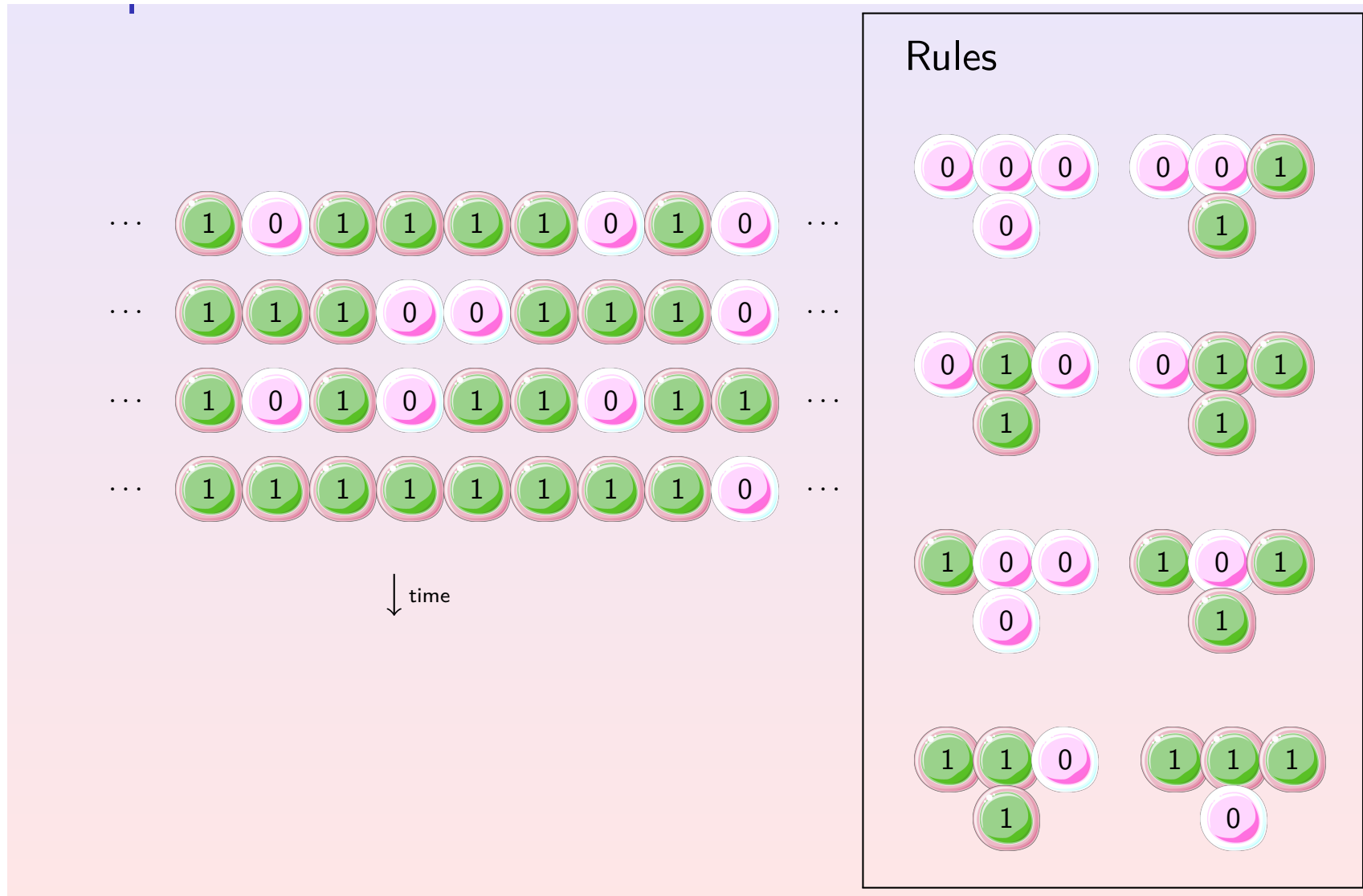
Example: the 110 Rule cellular automaton



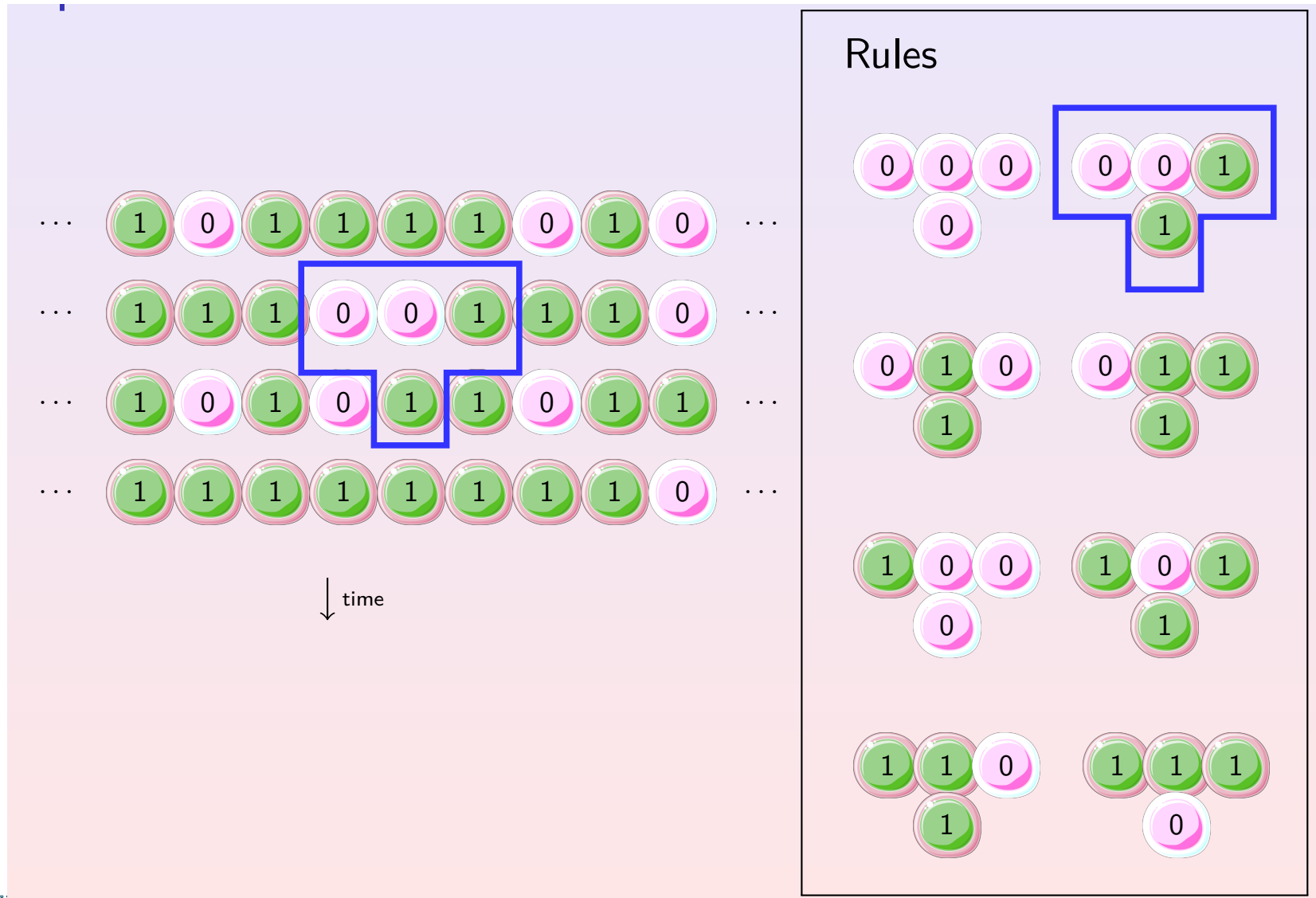
Example: the 110 Rule cellular automaton



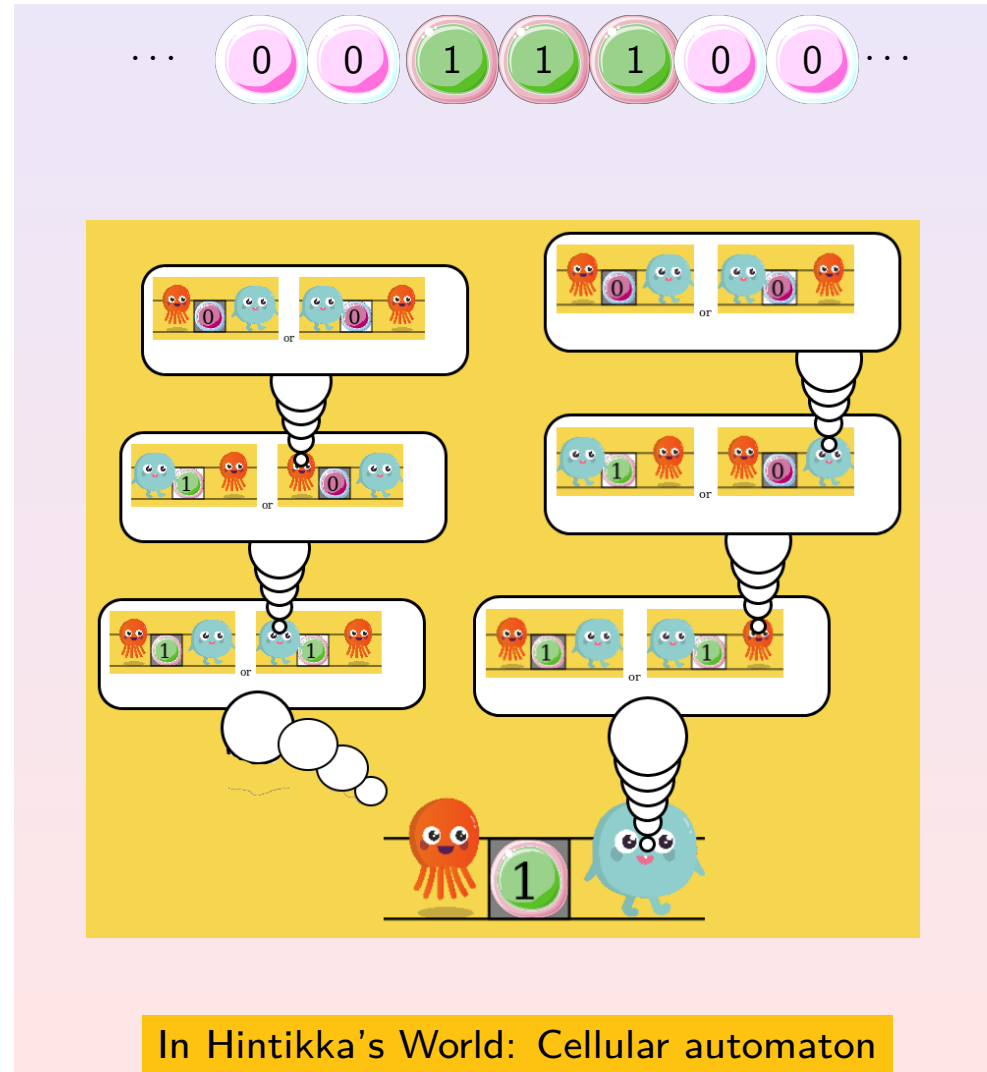
Example: the 110 Rule cellular automaton



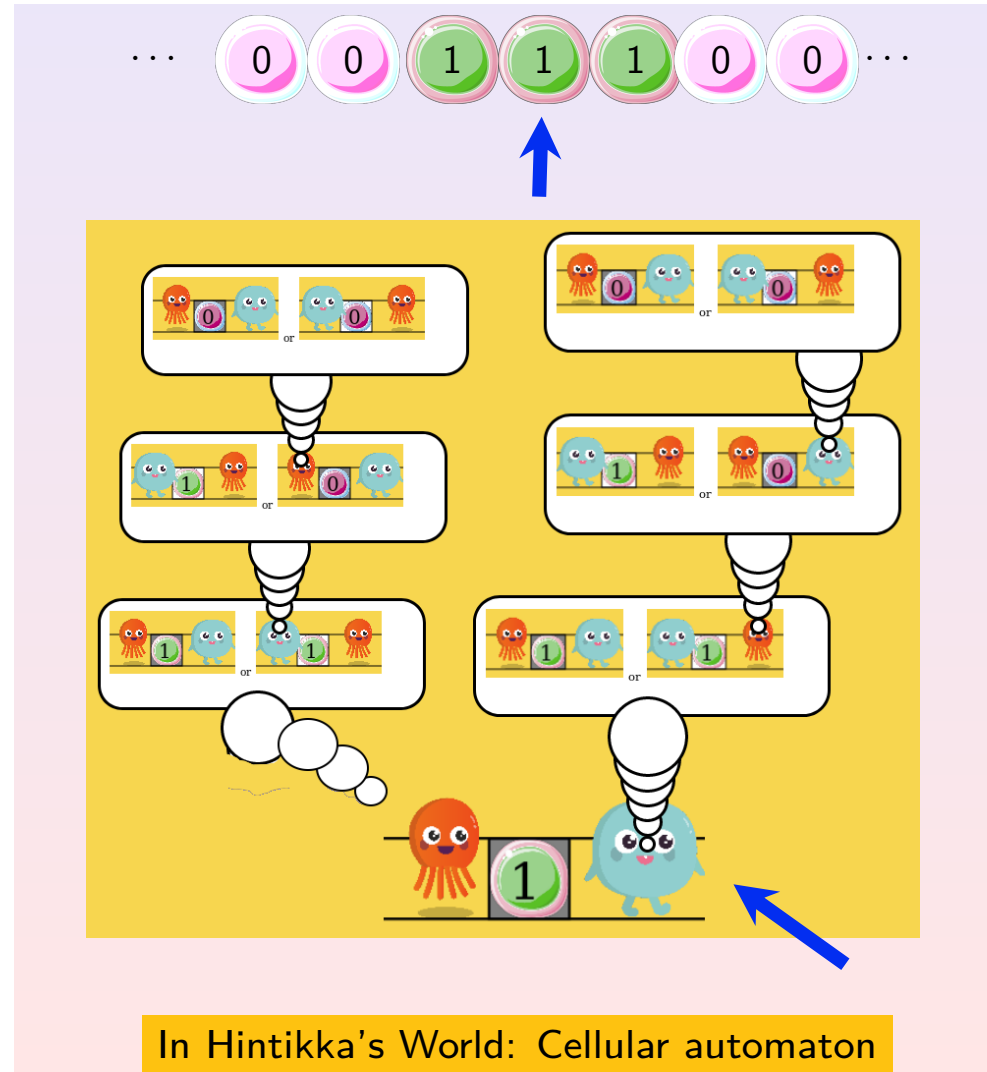
Example: the 110 Rule cellular automaton



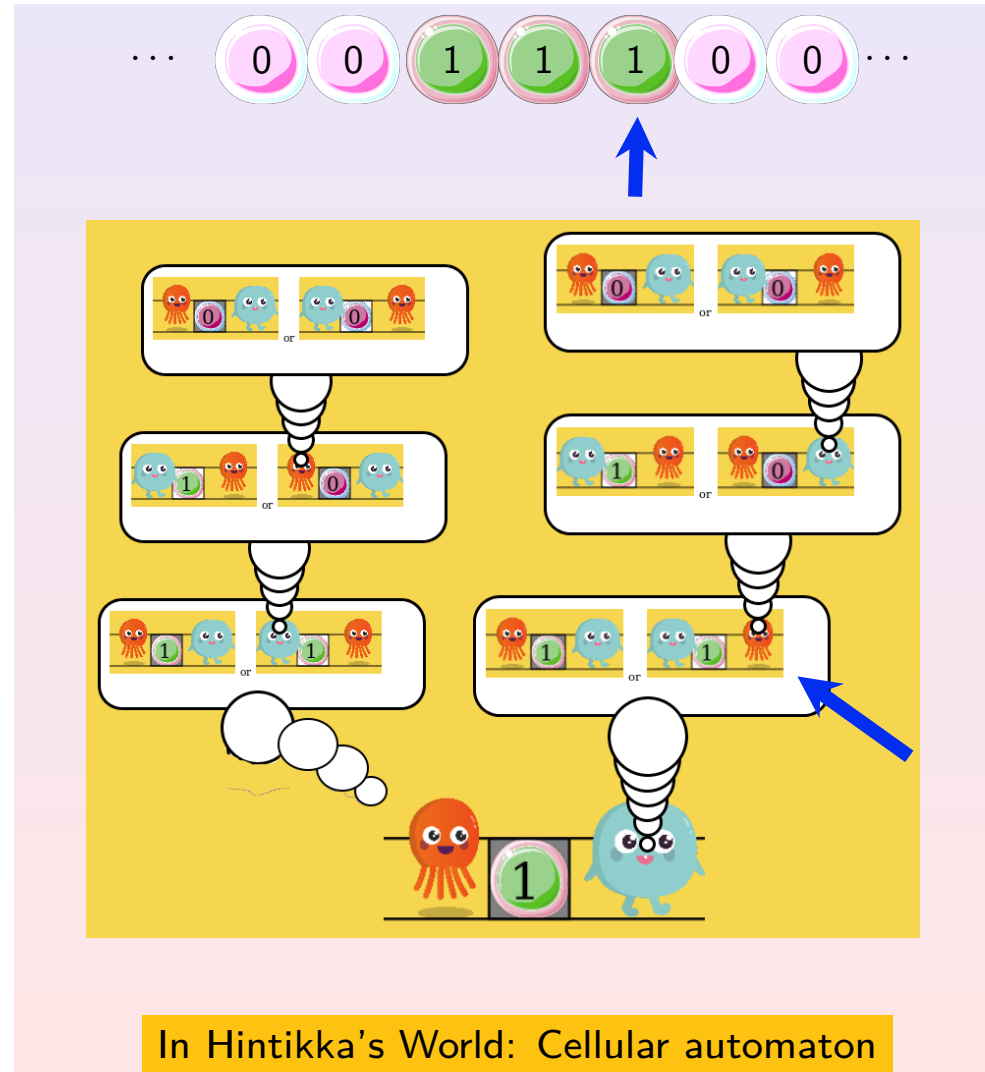
Encoding automaton configuration in a state



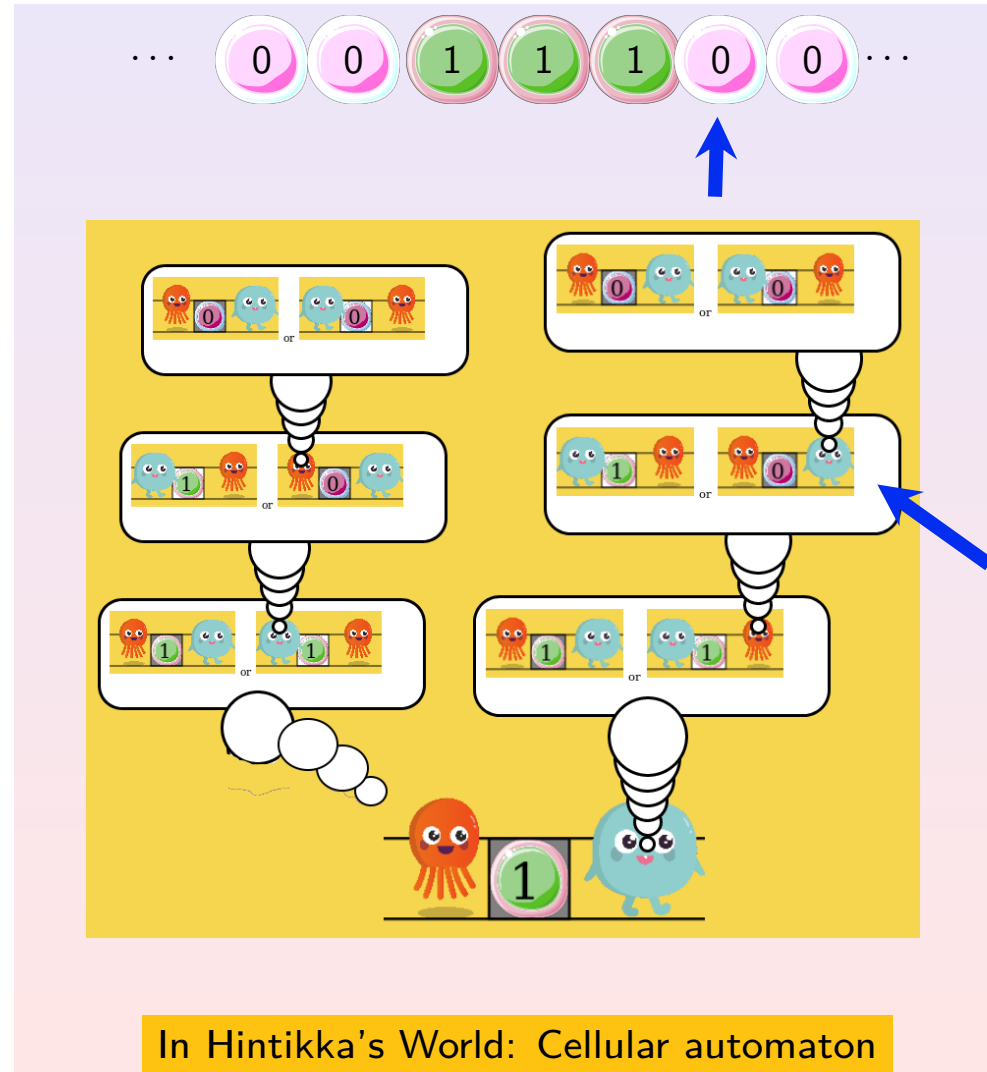
Encoding automaton configuration in a state



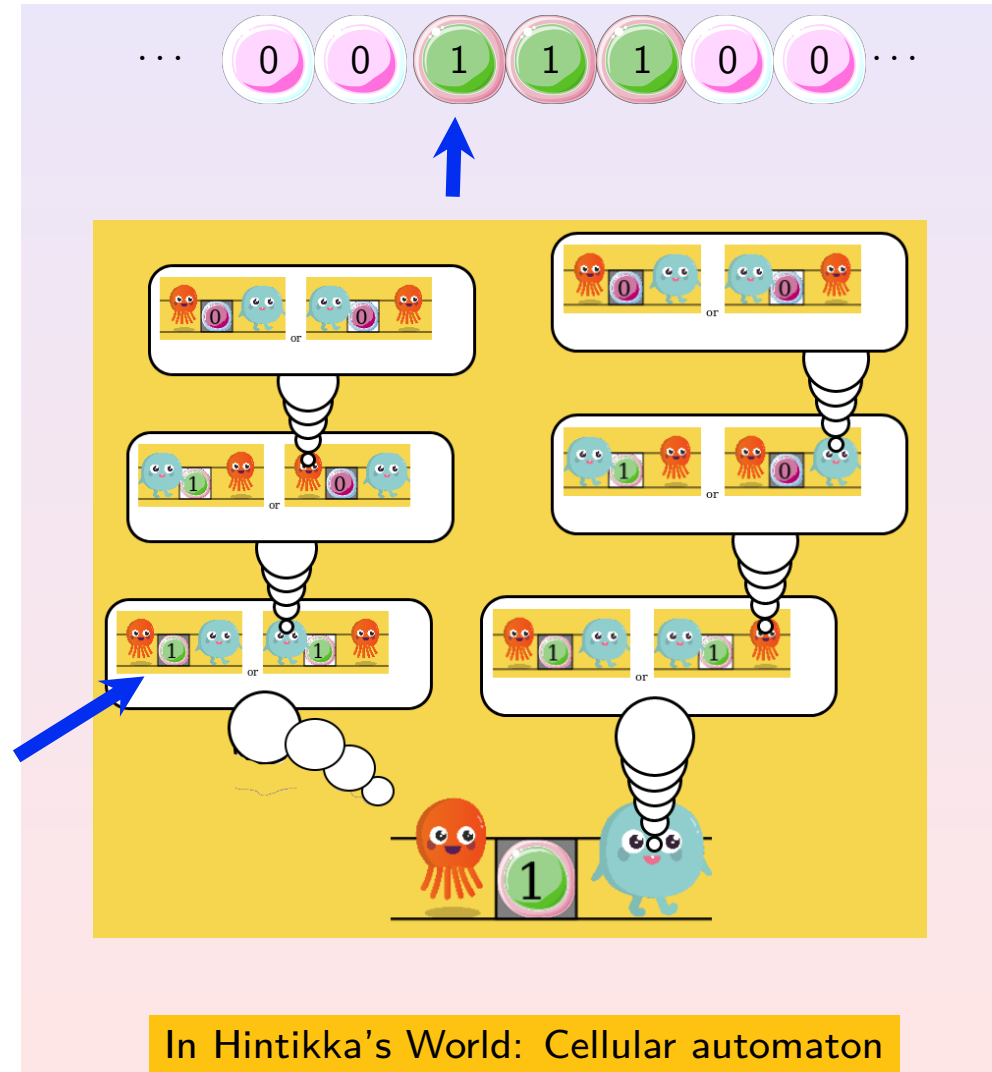
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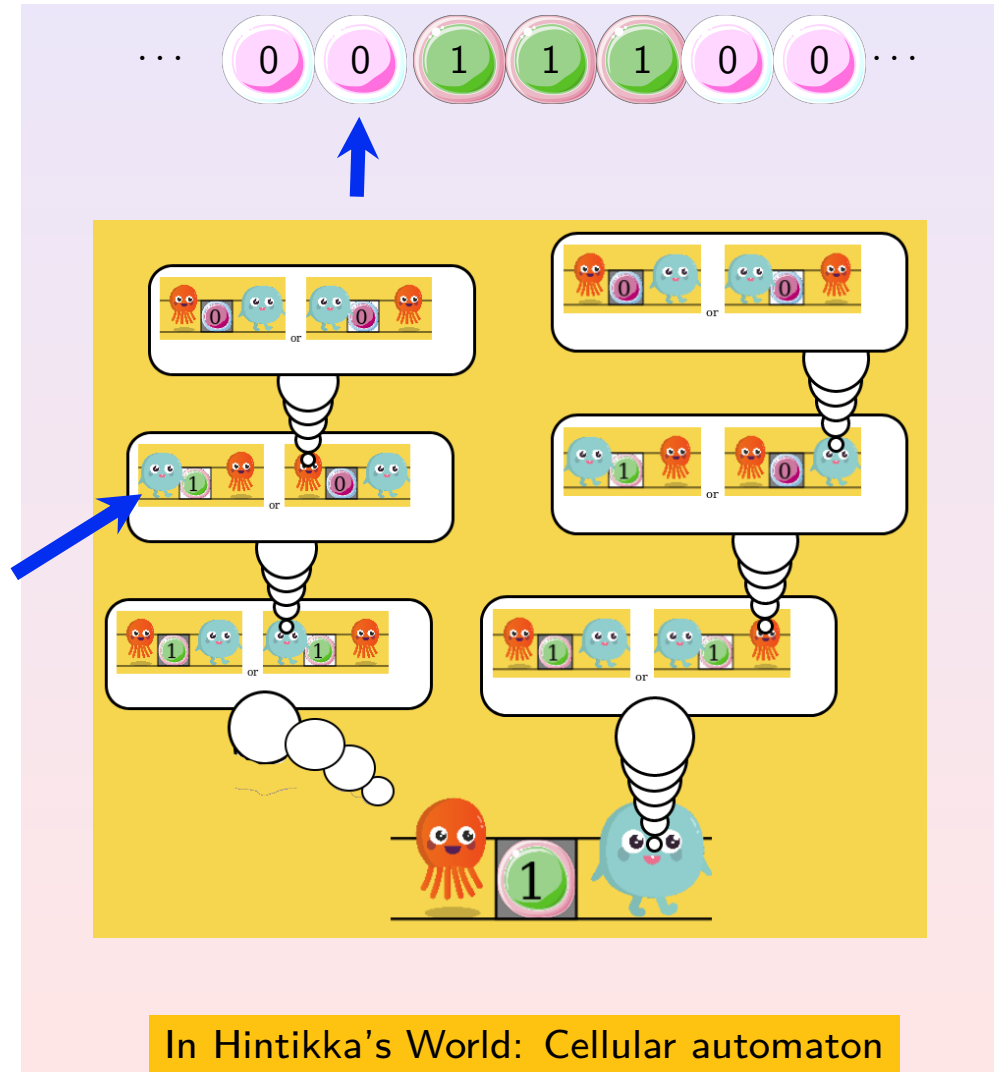
Encoding automaton configuration in a state



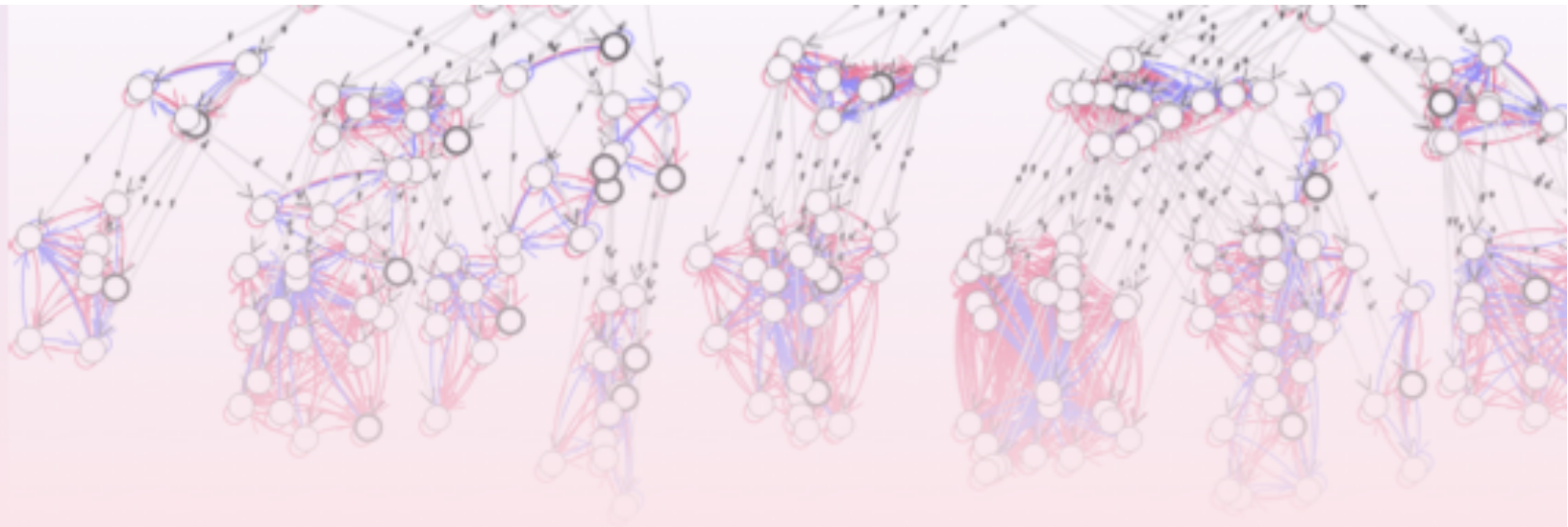
Encoding automaton configuration in a state



Encoding automaton configuration in a state



(Infinite) Epistemic temporal structures



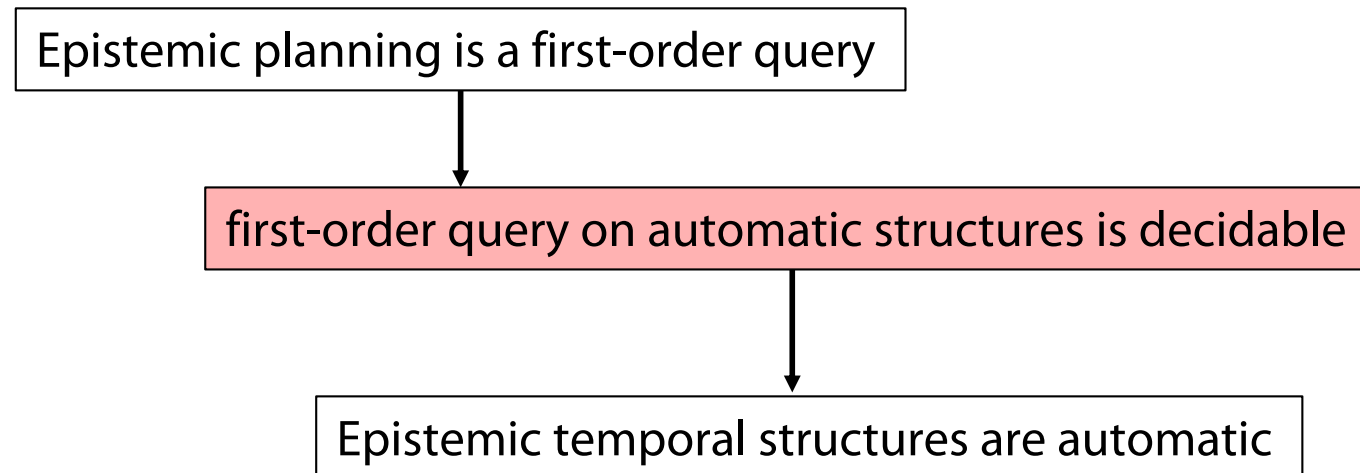
Epistemic planning: first-order query $\exists x, goal(x)$

Epistemic planning: first-order query $\exists x. goal(x)$

Decidability when pre/post are Boolean

Theorem (Yu et al. 13, Aucher et al 14)

When pre/post conditions are Boolean, epistemic planning is decidable



Theorem (Doueneau-Tabot et al., 2018)

Even decidable for goals in epistemic linear μ -calculus¹⁾.

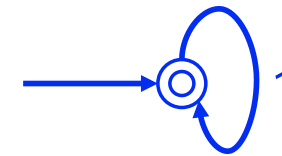
1) That is, for calculus with (minimal) fixed point operator

Automatic **structure** = defined by **automata**

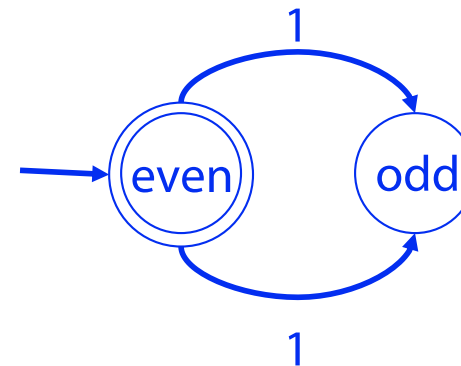
$$(\mathbb{N} , \text{isEven} , \leq) \longrightarrow (\mathcal{A}_{\mathbb{N}} , \mathcal{A}_{\text{isEven}} , \mathcal{A}_{\leq})$$

- $\text{Enc}: \mathbb{N} \rightarrow \{1\}^* ; n \mapsto 1^n;$

- $\mathcal{A}_{\mathbb{N}}$:



- $\mathcal{A}_{\text{isEven}}$



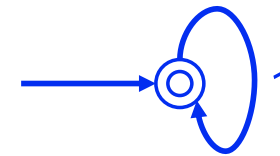
- \mathcal{A}_{\leq}

Automatic **structure** = defined by automata

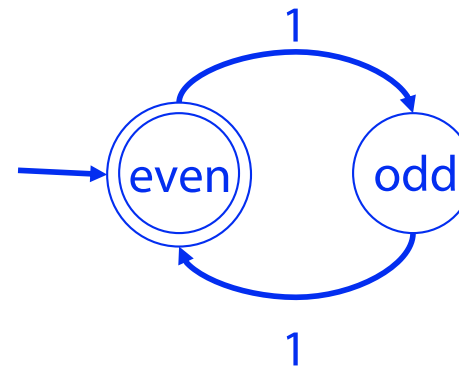
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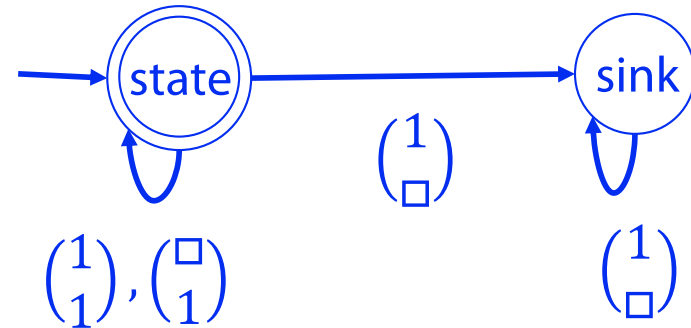


- \mathcal{A}_{\leq}

Automatic **structure** = defined by **automata**

$$(\mathbb{N} , \text{isEven} , \leq) \longrightarrow (\mathcal{A}_{\mathbb{N}} , \mathcal{A}_{\text{isEven}} , \mathcal{A}_{\leq})$$

- \mathcal{A}_{\leq} :



Idea:

- $2 \leq 5$

iff $11 \leq 11111$

- $2 \leq 5$

iff

word $\begin{pmatrix} 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ 1 \end{pmatrix}, \begin{pmatrix} 1 \\ \square \end{pmatrix}, \begin{pmatrix} \square \\ 1 \end{pmatrix}, \begin{pmatrix} \square \\ 1 \end{pmatrix}$ accepted by \mathcal{A}_{\leq}

Generalization to multi-player setting

Definition

A **strategy** for a player a is a function σ that maps any history we_1, \dots, e_n to a deterministic epistemic action in the repertoire of a

Definition

A **uniform strategy** for a player a is a strategy σ such that:
If $we_1 \dots e_n \sim_a ue'_1 \dots e'_n$ then $\sigma(we_1 \dots e_n) = \sigma(ue'_1 \dots e'_n)$

Undecidability even for Boolean pre/post

Theorem (Peterson /Reif 79, Coulombe/Lynch 18, Maubert et al 19)

The existence of uniform strategies for two players against an environment for achieving a goal is undecidable.

Theorem

Decidability of existence of uniform strategies holds when

- Only public actions are allowed
(Belardenelli et al 17) (Maubert et al 19))
- Hierarchical information is assumed
(Maubert/Murano 18), Maubert et al 19)

Complexity results in epistemic planning

	One centralized planner (Bolander et al 2015)	Many players (Maubert et al 2019)
Public announcements	NP-c	PSPACE-c
Public actions	PSPACE-c	EXPTIME-c
Boolean pre/post	Decidable	undecidable
all	Undecidable	Undecidable (Peterson/Reif 79)

Uninformed semantics (not knowing about others' strategies)
in case of many players



Perspectives: DEL and Formal Language theory

Question: Is epistemic planning one agent (pre: md 1, no post) **decidable**?

FOL query
decidable on

FOL query
Is NOT decidable on

Automatic
structures

Pushdown automata?
Causal hierarchy?

Turing-complete
structures

ÖÖ: See also descriptive complexity

- Connections with logics for reasoning about strategies such as Alternating temporal-time logic, Strategy logic et (Maubert et al. 2019)
- Describing protocols/policies

Uhhh, a lecture with a hopefully useful

APPENDIX



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Color Convention in this course

- Formulae, when occurring inline
- Newly introduced terminology and definitions 
- Important **results (observations, theorems)** as well as emphasizing some aspects 
- **Examples** are given with standard orange with possibly light orange frame 
- Comments and notes 
- Algorithms 